# QDFlow: A Python package for physics simulations of quantum dot devices

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#### **Abstract**

Recent advances in machine learning (ML) have accelerated progress in calibrating and operating quantum dot (QD) devices. However, most ML approaches rely on access to large, representative datasets designed to capture the full spectrum of data quality encountered in practice, with both high- and low-quality data for training, benchmarking, and validation, with labels capturing key features of the device state. Collating such datasets experimentally is challenging due to limited data availability, slow measurement bandwidths, and the labor-intensive nature of labeling. QDF1ow is an open-source physics simulator for multi-QD arrays that generates realistic synthetic data with ground-truth labels. QDF1ow combines a self-consistent Thomas-Fermi solver, a dynamic capacitance model, and flexible noise modules to simulate charge stability diagrams and ray-based data closely resembling experiments. With an extensive set of parameters that can be varied and customizable noise models, QDF1ow supports the creation of large, diverse datasets for ML development, benchmarking, and quantum device research.

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#### 16 1 Introduction

Among the various quantum computing platforms, quantum dots (QDs) stand out for their scalability potential, compact size, and long coherence times [1]. Operating QD devices, however, remains a formidable challenge, with complexity growing rapidly—often exponentially—as the number of qubits increases. Recent advances in integrating machine learning (ML) with quantum device operation have begun to mitigate these difficulties, offering promising automated control and calibration strategies. For example, ML algorithms have been developed for the fabrication [2, 3], characterization [4, 5], tuning [6–13], and gate virtualization [14, 15] of QD devices.

Developing robust ML models requires access to large and diverse datasets representative of the multi-dimensional parameter space typical of QD devices. Crucially, for supervised ML applications, these datasets must also include metadata that identifies key features, such as the global state (i.e., the number of QDs formed), the charge configuration, and the type of transition lines present. Unfortunately, large volumes of high-quality experimental data can be challenging to obtain as companies and research groups often keep such data proprietary [16]. Limited measurement bandwidth in real-world experiments also constrains the efficient exploration of the entire high-dimensional parameter space in a reasonable time. Generating accurate feature labels for publicly available data is a labor-intensive and time-consuming task that can produce subjective and potentially erroneous labels. Physics-based simulations offer a practical solution: they enable the generation of arbitrarily large datasets while providing direct access to the ground-truth charge states, thereby simplifying the labeling process needed for ML training.

Here, we introduce QDFlow, an open-source Python package for simulating QD systems and generating synthetic data tailored for ML training and applications. The core physics engine in QDFlow employs the Thomas-Fermi approximation to numerically solve for the semiclassical charge density n(x) along a one-dimensional (1D) nanowire. While the current state-of-the-art devices are typically realized by confining charges (electrons or holes) within a two-dimensional (2D) heterostructure, the QDs are ultimately formed within quasi-1D channels within those heterostructures, motivating our choice of a 1D model. In practice, the simulated data produced by QDFlow closely resembles that of linear QD arrays in 2D heterostructures. ML models trained on QDFlow-generated data have been shown to generalize effectively to larger 2D QD arrays [14].

There are several open-source QD device simulators that rely on the constant capacitance model, treating the array of QDs and their associated electrostatic gates as nodes in a network of fixed capacitors [17–19]. Additionally, Ref. [19] allows the capacitances to vary with respect to the number of charges n by introducing an n-dependent correction to the capacitance matrix. In contrast, in QDF1ow the capacitance parameters are physics-informed, obtained directly from the self-consistent Thomas-Fermi solution rather than imposed heuristically. All key physical observables—such as current, charge states, and sensor readouts—are derived from a capacitance model constructed based on the computed charge density n(x). This ensures that the capacitances evolve dynamically with gate voltages, yielding a more realistic description of device behavior. Furthermore, QDF1ow allows for modeling regions with low barriers between

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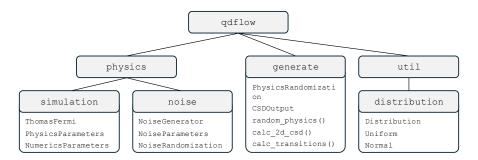


Figure 1: Diagram illustrating the QDFlow library organizational structure. Each of QDFlow's four modules is listed, along with the most important classes or functions within those modules.

dots, leading the dots on either side to combine into a single centralized dot. Finally, QDF1ow incorporates a flexible noise module, enabling the addition of experimentally relevant effects such as thermal broadening, charge offset drift, and voltage fluctuations. These features make the simulated data qualitatively comparable to experimental measurements while maintaining full access to the ground truth labels required for ML applications. Building on QF1ow—a legacy implementation of the QD simulator that applied the Thomas-Fermi approximation to model charge densities and stability diagrams [20,21]—QDF1ow extends these methods into a flexible, open-source framework that integrates physics-informed capacitance modeling with realistic noise processes tailored for ML applications.

QDF1ow has already demonstrated its utility in advancing ML-driven QD research, confirming that ML models trained exclusively on simulated data can be successfully deployed in experimental settings, on samples fabricated in an academic cleanroom as well as on an industrial 300-mm process line, and on 1D and 2D QD arrays. The legacy version of the simulator was used to generate the QFlow-lite dataset [21,22], which enabled the training of several ML models for global state recognition. The utility of these ML models was demonstrated both offline, by navigating the voltage space within pre-measured experimental datasets [13, 20], and in closed-loop experiments [9, 12, 23]. The dataset also supported the development of a novel classification framework for simple high-dimensional geometrical structures, known as the ray-based classification (RBC) framework [24]. The expanded dataset, QFlow 2.0: Quantum dot data for machine learning [22], generated using the Thomas-Fermi solver with integrated realistic noise processes, further advanced ML-based approaches to QD tuning. In particular, models trained with data from the QFlow 2.0 dataset have been successfully applied to tasks such as data quality assessment [25], physics-informed RBC and ray-based navigation in 1D QD arrays [13], and the development of a full virtualization stack for 1D and 2D QD arraysin Ge/SiGe [14] and in Si/SiGe. These successes confirm the compatibility of QFlow 2.0-generated with real-world experiments. They also highlight the value of physics-informed synthetic datasets for accelerating the development of automated control tools for QD systems.

QDF1ow is available for download from the Python Package Index, with the source code released under the GNU General Public License in the QDF1ow GitHub repository [26]. Comprehensive API documentation is provided via docstrings embedded in the source code and as HTML pages hosted on Read the Docs. The library includes type hints for all classes and functions to support clarity, maintainability, and extensibility. Unit and benchmark tests are also distributed with the QDF1ow repository to facilitate validation and performance evaluation.

# 92 Physics simulation

QDFlow has three main modules: simulation, noise, and generate, and one utility module, distribution, as depicted in Fig. 1. The simulation and noise modules are part of the physics package. The core physics-based engine of the simulator is contained in the simulation module. It uses a Thomas-Fermi solver to find the stable charge configuration and sensor output of a particular QD device defined by a set of physical parameters. The QDFlow Thomas-Fermi solver was first introduced in Ref. 21, but has since been refined and extended within QDFlow to improve flexibility, physical relevance, and integration with downstream ML workflows. The PhysicsParameters dataclass, which is used to initialize the simulation, specifies over twenty parameters governing the properties of the QD device. These parameters include both material characteristics and device-specific features such as gate geometry and positioning. Importantly, the gate voltages—experimentally relevant control knobs—are explicitly included among the simulation inputs. By sweeping these voltages, QDFlow produces the final outputs: 2D CSDs and 1D rays, directly mirroring the tuning procedures used in real QD experiments.

The noise module is responsible for adding noise to the final datasets, as well as for applying certain post-processing to the data. The generate module contains high-level functions to assist in generating datasets. It is the module that the user would most often interact with. Finally, the distribution module, contained within the util package, contains classes defining random variable distributions.

To generate data with QDFlow, the user first chooses whether to run the default configuration or adjust the distributions and ranges over which physics parameters are randomized. Next, they create one or more sets of randomized device parameters, and for each device, generate a CSD using the functions in the generate module. Once the physics parameters have been specified, an instance of the ThomasFermi class is instantiated. This class serves two main purposes: first, it solves for the charge density function n(x); and second, it uses n(x) to construct a capacitance model and compute physical quantities such as the device's charge state and sensor response. QDFlow then runs the physics simulation for every pixel in each diagram and compiles the results into a CSDOutput dataclass, which is returned to the user. By repeating this process over a range of gate voltages, QDFlow generates data that can be assembled into CSDs or rays, depending on the application. The output, stored as NumPy arrays, can be directly analyzed and plotted, or optionally augmented with noise to emulate experimental data.

In the following sections, we provide a more detailed account of the nanowire model physics underlying the simulation. We then explain how the Thomas-Fermi approximation is applied to construct the capacitance model that drives the CSD simulation.

#### 2.1 Nanowire model

QDF1ow employs a 1D physics model in which charges are assumed to be confined to a linear nanowire that lies along the x-axis. The ends of the nanowire are connected to electron reservoirs, and a bias voltage can be applied between them. Electrostatic gates are positioned at a height h below the xy-plane, and are modeled as infinite cylindrical conductors with central axis parallel to the y-axis, as shown in Fig. 2(a). The arrangement makes our nanowire model a hybrid between a true nanowire device and other QD device architectures. Gates biased to low potential act as plunger gates, while those biased to high potential act as barrier gates (for positive charge carriers, with the convention reversed for negative carriers).

The plunger and barrier gates define an electrostatic potential V(x), where x is the distance along the nanowire. Note that because we are using a 1D model, we are only concerned with the potential along the x-axis. The potential at a distance r from the center of a single

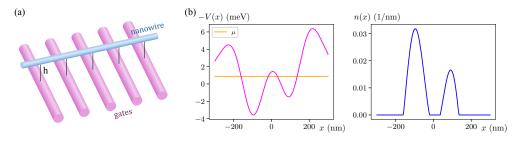


Figure 2: (a) The nanowire model used in QDFlow. (b) The potential V(x) created by the electrostatic gates (left) and the charge density n(x) induced by the potential (right).

cylindrical gate (in the absence of other gates) can be expressed as the potential of a screened line charge:

$$V_{\text{gate}}(r) = V_h \frac{\mathcal{K}_0(r/\lambda)}{\mathcal{K}_0(h/\lambda)} \tag{1}$$

where  $V_h$  is the potential at a reference distance r = h (chosen as the separation between the gate and the nanowire),  $\lambda$  is the screening length, and  $\mathcal{K}_0(z)$  is the modified Bessel function of the second kind. Specifically, we note that  $V_h$  is not the voltage of the gate itself; rather, it is the voltage that the nanowire feels due to the gate (in the absence of other gates). This is essentially the voltage of the gate multiplied by the lever arm of the gate.

Because the presence of nearby gates induces additional charges on each of the gates, and consequently changes Eq. (1), we cannot obtain V(x) by simply summing  $V_{\rm gate}(r)$  over all gates. Determining the exact potential in the presence of multiple gates is a challenging electrostatics problem, even in the purely classical setting. It requires solving the screened Laplace equation with boundary conditions determined by the voltages on each of the gates. While such a calculation can be performed numerically, it must be repeated whenever any gate voltage is changed.

To make the problem tractable, we adopt the simplifying assumption that the induced charges on each gate are rotationally symmetric about the axis of the gate. Under this approximation, the induced charges act as a line charge that lies along the central axis of the gate. Because the gate is rotationally symmetric, the potential  $V_{\text{gate}}(r)$  also acts as a single line charge at the center of the gate, and thus the induced charges effectively rescale  $V_{\text{gate}}(r)$  by a constant factor. Let  $V_i'$  be the rescaled value of  $V_h$  for gate i after including the effects of the induced charges on gate i, and let  $V_i$  be the value of  $V_h$  necessary for  $V_{\text{gate}}(r)$  to give the actual potential of gate i. Then by the superposition principle,  $V_i$  can be determined by adding the potential contributions from each of the gates:

$$V_i = \sum_j A_{ij} V_j' \tag{2}$$

where  $A_{ij}$  denotes the ratio between the contribution from gate j to the potential at gate i and the effective potential  $V'_j$ . In the absence of other gates,  $V_i = V'_i$ , so  $A_{ii}$  is simply 1. The contribution from one gate to another is given by  $V_{\text{gate}}(r)$ , where r is the distance between gates. Thus,  $A_{ij}$  can be expressed as follows:

$$A_{ij} = \begin{cases} 1 & \text{if } i = j \\ V_{\text{gate}}(x_j - x_i) / V_{\text{gate}}(\rho_j) & \text{otherwise,} \end{cases}$$
 (3)

where  $x_j$  is the x-coordinate of the central axis of gate j and  $\rho_j$  is the radius of the gate j.

Calculating and inverting the matrix **A** allows us to determine the effective potentials  $V_i'$  from the applied gate voltages  $V_i$ . We then obtain V(x) by summing  $V_{\text{gate}}\left(\sqrt{(x-x_i)^2+h^2}\right)$  over all gates and using the effective potentials  $V_i'$  in place of  $V_h$  in Eq. (1).

#### 2.2 Thomas-Fermi solver

Having established how to compute the effective gate potentials and construct V(x), we now turn to the resulting charge distribution along the nanowire. Define n(x) to be the linear charge density at a point x along the nanowire, which is determined in response to the potential V(x), as illustrated in Fig. 2(b). However, due to the Coulomb interaction between charges, the presence of an induced charge in the nanowire will create a correction to V(x). This self-interaction results in the following integral equations, which must be solved self-consistently:

$$n(x) = \int_{\epsilon'(x)}^{\infty} \frac{g_0}{1 + e^{\beta(\epsilon - \mu)}} d\epsilon = \frac{g_0}{\beta} \operatorname{sp} \left[ \beta(\mu - \epsilon'(x)) \right]$$
 (4)

$$\epsilon'(x) = qV(x) + \int_{\mathbb{R}} K(x, x') n(x') dx'$$
 (5)

The physical parameters  $\mu$ ,  $g_0$ , and  $\beta$  in Eq. (4) indicate the Fermi level, the density of states in the conduction band (which is constant in 2D), and the inverse temperature, respectively, and  $\operatorname{sp}(z) = \ln(1 + e^z)$  is the softplus function. Parameter q in Eq. (5) controls the sign of the charge carriers, with -1 indicating electrons and +1 indicating holes, while K(x, x') gives the strength of the Coulomb interaction between points x and x', and is defined as follows:

$$K(x, x') = \frac{K_0}{\sqrt{(x - x')^2 + \sigma^2}}$$
 (6)

where  $K_0$  defines the energy scale of the interaction and  $\sigma$  is a softening parameter added to prevent a numerical singularity at x = x', which occurs due to the 1D model breaking down at scales less than the radius of the nanowire. The value of  $\sigma$  can be chosen to be  $3\pi r/8$ , where r is the nanowire radius, to maintain consistency with the potential energy of two uniformly charged disks as the spacing between them approaches zero [27], or alternatively, a custom interaction K(x, x') can be provided.

The Coulomb integral in Eq. (5) is formally taken over the entire nanowire. Because K(x,x') scales for large x' as 1/|x'|, this introduces concerns that the integral might diverge. At the same time, the integrand is weighted by n(x'), which becomes exponentially small for  $V(x')-\mu\gg\beta^{-1}$ . This condition is satisfied at the external barriers, see Fig. 2(b), provided that the external barrier voltages are sufficiently high. In addition, it is assumed that at distances far away from the nanowire, the system is connected to an electron reservoir where n(x') is large. However, the Coulomb interaction in semiconductors tends to include a screening term that suppresses contributions past a certain range. Thus, in practice, it is sufficient to evaluate the integral between the two external barrier gates.

For convenience, we define a linear operator  $\mathbf{K}$  to be the result of evaluating the Coulomb integral as follows:

$$\mathbf{K}f(x) = \int_{\mathbb{R}} K(x, x') f(x') dx'$$
 (7)

This allows us to combine Eqs. (4) and (5) to obtain:

$$n(x) = \frac{g_0}{\beta} \operatorname{sp}[\beta(\mu - qV(x) - Kn(x))]. \tag{8}$$

The basic method we employ to solve Eq. (8) is successive iteration. Starting from an initial guess  $n_0(x)$ , the right-hand side of Eq.(8) is evaluated with  $n(x) = n_0(x)$ , yielding an updated function  $n_1(x)$ . This procedure is then repeated until n(x) converges, if at all. The convergence tolerance and the maximum number of allowed iterations are specified through the

NumericsParameters dataclass, which can be provided when instantiating the ThomasFermi class. If the iteration does not converge to the specified tolerance within the allowed number of iterations, a ConvergenceWarning is issued.

The convergence can be problematic for certain parameter regimes. For example, if we define  $\Delta(x)$  to be the difference between an initial guess  $n_0(x)$  and the true value n(x):

$$n_0(x) = n(x) + \Delta(x),\tag{9}$$

then evaluating the right-hand side of Eq. (8) yields:

$$n_1(x) = \frac{g_0}{\beta} \operatorname{sp} \left[ \beta (\mu - qV(x) - \mathbf{K}n(x) - \mathbf{K}\Delta(x)) \right]$$
 (10)

We now use the approximation  $sp(z) \approx z$ , which is valid for  $z \gg 1$ . Although this assumption does not always hold (particularly for small  $\beta$ ), it is useful for analyzing certain convergence issues that may arise. Under this approximation, Eq. (10) simplifies to:

$$n_1(x) \approx n(x) - g_0 \mathbf{K} \Delta(x) \tag{11}$$

If all eigenvalues of  $g_0\mathbf{K}$  are smaller than 1, the error term  $-g_0\mathbf{K}\Delta(x)$  will be smaller in magnitude than the initial error  $\Delta(x)$ , and successive iterations will therefore converge to n(x). Conversely, if  $g_0\mathbf{K}$  possesses eigenvalues greater than 1, the iterative scheme will generally diverge. Physically, this divergence corresponds to strong coupling between charges, a regime that is well known to cause convergence difficulties in condensed matter systems [28]. Fortunately, this issue can be partially mitigated by solving Eq. (9) for  $\Delta(x)$ , substituting the result into Eq. (11), and solving for n(x), yielding the following expression:

$$n(x) \approx (1 + g_0 \mathbf{K})^{-1} [g_0 \mathbf{K} n_0(x) + n_1(x)]$$
 (12)

If we discretize the x-axis, the operator  $(1+g_0\mathbf{K})^{-1}$  can be computed through direct matrix inversion. This expression can then be incorporated into the successive iteration scheme by applying Eq. (12) after each iteration. Although there are still parameter regimes where the process diverges, this modified approach drastically enlarges the domain of convergence. In the weak-interaction limit, where the eigenvalues of  $g_0\mathbf{K} \ll 1$ , the right-hand side of Eq. (12) simplifies to  $n_1(x)$  to leading order in  $g_0\mathbf{K}$ . Thus, in this limit, the method naturally recovers the standard successive iteration procedure.

#### 2.3 Capacitance model

After calculating n(x), QDF1ow employs a capacitance model to determine the stable charge configuration and other properties. Similar techniques have been implemented in other QD simulations [17–19]. In most of those approaches, the capacitance matrix is assumed to be constant, i.e., the interdot capacitances remain fixed as the gate voltages are swept. The simulation introduced in Ref. 19 allows for variable capacitances by applying a correction to the capacitance matrix based on the particle number. In contrast, QDF1ow derives the capacitance matrix directly from the charge density n(x), which depends explicitly on the gate voltages. This feature enables charge-transition slopes and spacings to vary across a single CSD. Moreover, constructing the capacitance model from n(x) naturally captures transitions between a double dot and a merged single dot as the interdot barrier is lowered.

The first step in creating the capacitance model is determining the regions of the nanowire where significant amounts of charge are induced. This is achieved by applying a threshold to n(x), configurable through the NumericsParameters dataclass, and identifying continuous intervals of points that lie above the threshold. This will result in a set of intervals of the form

 $[a_i, b_i]$ , which we call "charge islands." The thresholding is also responsible for determining whether or not adjacent QDs should be handled as individual dots. Specifically, if n(x) exceeds the threshold throughout the region between the two QDs, they are merged and treated as a single dot. Otherwise, they are considered to be two separate QDs with a potential barrier between them

Once the charge islands are identified, the energy *E* of the resulting capacitance model is defined as follows:

$$E = \sum_{i,j} E_{ij} (Q_i - Z_i) (Q_j - Z_j)$$
(13)

$$Z_i = \int_{a_i}^{b_i} n(x) dx \tag{14}$$

$$E_{ij} = \frac{1}{Z_i Z_j} \left[ c_k \delta_{ij} \int_{a_i}^{b_i} n(x)^2 dx + \frac{1}{2} \int_{a_i}^{b_i} \int_{a_j}^{b_j} K(x, x') n(x) n(x') dx dx' \right]$$
(15)

where  $Z_i$  is the (potentially noninteger) charge induced by the gates on island i under the Thomas-Fermi approximation, and  $Q_i$  is the integer number of charges on island i under a specific charge configuration  $\vec{Q}$ . The  $c_k$  term of Eq. (15) incorporates the kinetic energy of the charges. Since, for our purposes, the energy matrix fully characterizes the system, we do not compute the capacitances explicitly and instead work directly with the energy matrix. If desired, the capacitance matrix  $\mathbf{C}$  can be obtained from the energy matrix via the relationship  $\mathbf{C} = (2\mathbf{E})^{-1}$ .

After calculating the energy matrix, the next step is to determine the charge configuration  $\vec{Q}$  that minimizes the total energy E, subject to the constraint that all  $Q_i$  must be nonnegative integers. This is an instance of an integer optimization problem, which in general is NP-complete. However, for a moderate number of gates, a brute-force search is sufficient to find the minimum. In particular, we first locate the minimum in the continuous space, which occurs at  $\vec{Z}$ , and then evaluate  $E(\vec{Q})$  over all  $\vec{Q}$  such that for each integer  $Q_i$ ,  $|Q_i - Z_i| < 1$ . Once a stable charge configuration is identified, the potential at each of the sensors is calculated under the assumption that each island i hosts a line of charge with total charge  $qQ_i$  and charge density proportional to n(x). The Coulomb potential at each of the sensors arising from these charge islands is calculated, and the result is normalized by dividing by the potential of a single point charge located at a point on the nanowire closest to the sensor in question. This means that a single transition should have a height of no more than 1 after normalization.

Finally, QDF1ow allows the current across the nanowire to be found. For this calculation, the left and right sides of the nanowire are assumed to be connected to electron baths with potentials  $V_L$  and  $V_R$ , respectively. The dynamics of the charges are modeled using a semi-classical approach, treating them as particles that travel at the Fermi velocity. Each time they collide with a barrier, the particles have a chance to either tunnel through it or be reflected back. The tunneling probability across each barrier is determined by the transmission coefficient, which we calculate using the WKB approximation. This allows the tunneling rates between islands and the tunneling rates to and from the external charge baths to be obtained. These tunnel rates are then used to define a Markov graph which encodes the dynamics of the transitions between charge states. The current through the nanowire is obtained by evaluating the net rate at which charges enter and leave the charge baths at the steady state of this Markov graph.

# 3 Data generation

The data generation is carried out within the generate module. A single instance of the ThomasFermi class calculates quantities of interest for a single point in voltage-space only based on the device configuration specified in the physics module. To generate a complete CSD, a new simulation instance must be created for each pixel. However, since the gate voltages of neighboring pixels vary only slightly, it follows that the corresponding charge density n(x) will also not change significantly between adjacent pixels. To optimize QDFlow performance, the result of the n(x) calculation at one pixel is used as an initial condition when calculating n(x) at adjacent pixels. This means that n(x) must only be calculated from scratch once for each diagram.

QDF1ow contains convenience functions for generating CSDs and rays in the generate module. Since the primary purpose of QDF1ow is to generate data for training specialized ML models, it is essential that the resulting dataset captures the full range of variability observed in contemporary QD devices. To achieve this, QDF1ow includes functionality to randomize nearly all physics parameters and to control the distributions from which each parameter is drawn. This capability is implemented via the PhysicsRandomization dataclass, which specifies each physics parameter as either a fixed value (when no randomization is desired, e.g., to allow regeneration of the same QD device), or a Distribution from which to draw the random values. A code example in Listing 1 shows how to import QDF1ow and how to initialize a random configuration of physical parameters, with  $\mu$  drawn from a distribution provided by the user.

The Distribution, defined in the distribution module, is an abstract base class that encodes how a given parameter should be randomized. Several standard distributions, including Uniform, Normal, and LogNormal, are implemented in QDFlow as wrappers to the NumPy random generator functions of the same name. In addition, user-defined distributions can be easily created by extending the Distribution class and implementing the draw() method to generate random values in an arbitrary manner. The CorrelatedDistribution class handles cases where it is desired or necessary for multiple random variables to be related to one another in some way.

This randomization framework, along with the dozens of configurable physics parame-

```
from qdflow import generate
1
    from qdflow.util import distribution
2
3
    # Create a new dataclass instance that contains the default
    # randomization distributions for each physics parameter
5
    phys_rand = generate.PhysicsRandomization.default()
    # Change the range from which mu can be drawn
8
    phys_rand.mu = distribution.Uniform(0, 1.2)
    # Generate a list of 6 sets of random device parameters
11
    n_{devices} = 6
12
    phys_params = generate.random_physics(phys_rand, n_devices)
13
```

Listing 1: Example code to generate a list of 6 randomized sets of device parameters. First, a PhysicsRandomization object is created, which defines the ranges and distributions, as appropriate, from which the physics parameters should be randomized. Distributions for each parameter can then be set as desired.

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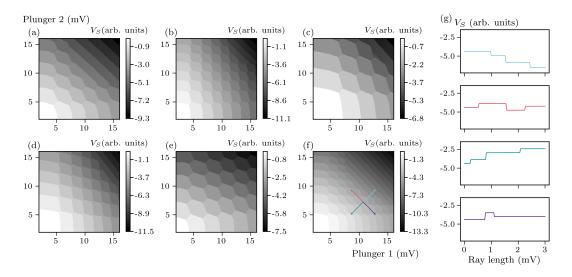


Figure 3: (a)-(f) Examples of CSDs generated with randomized physics parameters. (g) Examples of ray data generated along the rays shown on the CSD in panel (f).

ters, enables QDFlow to generate a highly diverse set of CSDs. Figure 3 shows six examples of CSDs generated with QDFlow. A snippet of code allowing to generate CSD data from a PhysicsParameters object is shown in Listing 2.

While CSDs are extremely useful for visualizing charge states, they require extensive data collection. In practice, only a relatively small subset of points—the charge transitions—are of primary importance. As the number of dots grows, so does the dimensionality of the gate voltage space, rapidly making the exploration of the complete, multidimensional voltage space infeasible. This challenge is typically handled by measuring multiple 2D CSDs, each defined by a different pair of gates.

In Ref. 12, an alternative method for assessing the charge state in QD devices, with 1D rays measured in multiple directions in the voltage space used in place of the 2D CSDs. This method greatly reduces the amount of data required for assessing the charge state of the device, but

```
from qdflow import generate
    import numpy as np
2
3
    # Create a set of physics parameters
    phys = generate.default_physics(n_dots=2)
6
    # Set ranges (in mV) and resolution of plunger gate sweeps
    V_x = np.linspace(2., 16., 100)
8
    V_y = np.linspace(2., 16., 100)
10
    # Generate a charge stability diagram
11
    csd = generate.calc_2d_csd(phys, V_x, V_y)
12
13
    # Obtain the sensor readout in the form of a numpy array
14
    sensor_num = 0
15
    sensor_readout = csd.sensor[:, :, sensor_num]
```

Listing 2: Example code demonstrating how to generate a CSD from a PhysicsParameters object.

```
from qdflow import generate
    import numpy as np
2
    from scipy.stats import qmc
    # Create a set of physics parameters
    phys = generate.default_physics(n_dots=2)
6
    # Generate quasirandom points inside a given area
8
    v_{min}, v_{max} = 2., 16.
    point_generator = qmc.Halton(d=2, scramble=False)
10
    initial_points = qmc.scale(point_generator.random(n=50), v_min, v_max)
11
12
    # Define a list of rays that will extend out from each point
13
    ray_length = 3. # length of rays in mV
14
    num_rays = 8
15
    rays = ray_length * np.array([[np.cos(2*np.pi*i/num_rays),
16
        np.sin(2*np.pi*i/num_rays)] for i in range(num_rays)])
17
18
    # Generate ray data
19
    resolution = 100 # points per ray
20
    ray_data = generate.calc_rays(phys, initial_points, rays, resolution)
```

Listing 3: Example code demonstrating how to generate ray data from a PhysicsParameters object.

sacrifices some of the intuitive human interpretability provided by CSDs, necessitating the use of ML tools. To support the development of ML methods for ray-based analysis, QDFlow includes functionality for generating ray-based datasets, as shown in Listing 3.

#### 326 4 Noise

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The simulations described thus far capture many essential physical features of QD devices but omit one critical ingredient: noise. In experimental data, noise strongly influences both the visibility of charge transitions and the reliability of automated analysis.

To more faithfully emulate experimental conditions, QDF1ow includes the noise module, which contains functionality for adding noise to both CSDs and rays, as well as several postprocessing functions designed to mimic effects of experimental measurements. The module implements several types of noise, including the white noise, pink (1/f) noise, telegraph noise, and latching effects, as well as stray transitions arising from nearby unintended dots [25,29]. Postprocessing functions include adding gate-sensor coupling, adding a  ${\rm sech}^2 x$  blur, and adding Coulomb peak effects. Each noise in QDF1ow can be controlled individually, with its magnitude defined relative to the scale of the CSD data, or as a predefined mixture. Similar to the physical parameter randomization discussed in Sec. 3, QDF1ow supports designating the distributions from which each noise parameter is drawn via the NoiseRandomization dataclass.

Figure 4(a) shows an example of a noiseless CSD simulated with QDF1ow. CSDs with noise implementations adapted from QF1ow—white, pink, and telegraph noise and Coulomb peak—are depicted in panels (b), (c), (d), and (e), respectively. CSDs with latching, sech² blur, unintended QD, and sensor-gate coupling—new to QDF1ow—are presented in panels (f), (g), (h), and (i), respectively.

The simplest, white noise, is implemented by adding to each pixel a value drawn from a

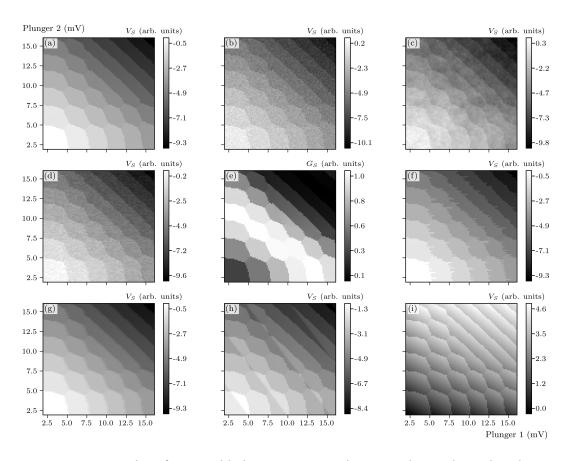


Figure 4: Examples of noise added to a CSD. (a) The original CSD data, (b) white noise, (c) pink noise, (d) telegraph noise, (e) Coulomb peak, (f) latching, (g) Sech blur, (h) unintended QD, and (i) sensor-gate coupling.

normal distribution with standard deviation given by the magnitude of the white noise. Pink noise is implemented by generating white noise in Fourier space with a uniform random phase and magnitude proportional to  $1/\sqrt{f_x^2+f_y^2}$ , where  $f_x$  and  $f_y$  are the components of each point in Fourier space, and then applying an inverse Fourier transform. This configuration allows for greater variability compared to telegraph noise. Alternatively, QDFlow also provides the option to add pink noise correlated along only the primary measurement axis, which corresponds to the more physical model of pink noise correlated in time.

Telegraph noise is applied along an axis corresponding to the primary measurement direction in experimental data. It consists of adding a value (drawn from a normal distribution with nonzero mean) to a line of several contiguous pixels. The length of the added line is randomly drawn from a geometric distribution. This allows the distribution of lengths of the telegraph noise to follow an exponential, as expected for two-level systems with finite excited-state lifetimes. This process is then repeated across the CSD, alternating the sign of the value added each time.

Transitions from spurious QDs are emulated by adding functions of the form  $\tanh((\vec{x}-\vec{x}_0)\cdot\vec{a})$ , where  $\vec{x}$  gives the coordinates of each pixel,  $\vec{x}_0$  is the location on the CSD of the transition, and  $\vec{a}$  determines how strongly each of the gates plotted on the x- and y-axes are coupled to the unintended dot. Values of  $\vec{x}_0$  and  $\vec{a}$  are randomized, but a single  $\vec{a}$  is used if multiple unintended transitions appear on a single diagram.

The latching noise implemented in QDF1ow can be controlled using one of two methods. The first and simpler legacy method to simulate latching is to shift each row of pixels by a ran-

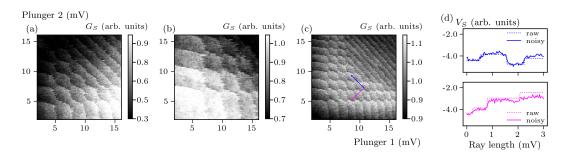


Figure 5: (a)-(c) Examples of CSDs with all noise types combined. (d) Ray data without noise (dotted line) and with noise added (solid line).

dom number of pixels drawn from a geometric distribution. This process produces a latching-like effect along the charge transitions; however, it is somewhat unrealistic since all transitions on the same row are shifted by the same amount, and because pixels far away from transitions are also displaced. A more physically realistic method relies on the nanowire simulation to calculate the sensor readout for both an excited charge state and a stable state at each pixel, similar to what is implemented in Ref. 18. The excited state chosen corresponds to the charge configuration most recently occupied prior to the most recent transition when sweeping the gate voltages. When latching noise is added, the sensor readout from the excited state replaces the stable-state readout for the first few pixels after each transition, with the number of pixels randomized each instance. In general, the second method is preferable as it more accurately reflects the experimental conditions; however, the first, legacy method is provided as a fall-back when excited-state data are unavailable or computationally inconvenient, or impossible to obtain.

In addition to noise, several postprocessing functions can be applied to the data. A sensorgate coupling in the form of a linear gradient along a random direction can be added. Convolving with a  $\operatorname{sech}^2 x$  kernel along the measurement axis introduces smoothing of the sharp transitions.

Finally, it is important to note that the physics simulation returns the value of the potential at each of the sensors; however, experimentally, the conductance of the sensor is the quantity that is measured. Therefore, we convert from potential to conductance by using a Coulomb peak lineshape of the form  $G \propto \operatorname{sech}^2[A(V-V_0)]$ , where G is the conductance of the sensor, A is a parameter that determines the width of the Coulomb peak, V is the potential at the sensor (the simulation output), and  $V_0$  is the peak center [30].

CSDs with a mixture of noises optimized for compatibility with experimental data are presented in Fig. 5(a)-(c). Figure 5(d) shows two rays with added noise. The exact amounts of each type of noise are randomized for each diagram. A code example showing how to generate noisy CSD data for a previously simulated sample CSD is shown in Listing 4.

Given the computational complexity of Thomas-Fermi calculations, the noise module is configured to assume that a complete noiseless CSD (or a ray-based data) has already been generated using the generate module. This approach gives us several advantages. First, it significantly reduces the computational overhead since multiple noise realizations with different relative noise strengths can be generated from a single noiseless CSD. Secondly, the modular approach adopted in QDF1ow provides flexibility that cannot be achieved experimentally, where it is not possible to calibrate individual noise sources to the desired level. Additionally, it allows us to specify the magnitudes of each of the noise types relative to the local scale of the surrounding data points, which is important since the scale of the data points can vary across large CSDs. Finally, it allows for systematic benchmarking of ML algorithms since the noise level and type can be modified independently of the underlying physical configuration.

```
from qdflow.physics import noise
    from qdflow.util import distribution
2
    import numpy as np
    # Use data from previous example
5
    data = np.load("sensor_readout.npy")
6
    # Create a new dataclass instance that contains the default
8
    # randomization distributions for each noise type
g
    noise_rand = noise.NoiseRandomization.default()
10
11
    # How much noise to add, relative to the transition height upper bound
12
    noise_amount = 0.15
13
14
    # Use a CorrelatedDistribution to randomize the white, pink, and
15
    # telegraph noise in such a way that the total always equals noise_amount
16
    num_dists = 3
17
    dists = distribution.SphericallyCorrelated(num_dists,
18
            noise_amount).dependent_distributions()
19
    noise_rand.white_noise_magnitude = dists[0].abs()
20
    noise_rand.pink_noise_magnitude = dists[1].abs()
21
    noise_rand.telegraph_magnitude = dists[2].abs()
22
    # Generate a random set of noise parameters
24
    noise_params = noise.random_noise_params(noise_rand)
25
26
    # Add noise to the data
27
    noisy_data = noise.NoiseGenerator(noise_params).calc_noisy_map(data)
28
```

Listing 4: Example code to add noise to a charge stability diagram. First, a NoiseRandomization object is created, which defines the ranges and distributions, as appropriate, from which the noise parameters should be randomized. A CorrelatedDistribution is used to randomize the different noise types while ensuring that the total noise amount is constant.

For example, one can generate a single noiseless dataset and then apply different realizations of noise to study the robustness of a given algorithm under varying experimental conditions, as was done in Ref. 13.

## 5 Benchmarking and limitations

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To benchmark QDF1 ow, we find the mean runtime of the physics simulation for 10,000 randomly generated sets of physics parameters. Each simulation is run with at most 1,000 iterations and a relative convergence tolerance of  $10^{-3}$ . We are interested in comparing the contribution to the overall runtime from calculating n(x) with the remaining portion of the simulation as the number of QDs increases. For each number of dots N, we obtain two runtimes: (i) the time required to compute the charge density profile n(x), and (ii) the remaining time to construct the capacitance model, minimize Eq. (13), and evaluate the sensor output. The results for small- and mid-sized QD arrays are shown in Fig. 6(a) and Fig. 6(b), respectively. For a small number of dots ( $N \le 20$ ), the main bottleneck is the initial part of the simulation

where n(x) is calculated. However, as the number of dots N is increased, the minimization of

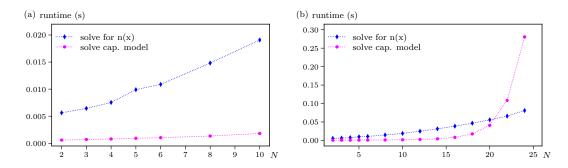


Figure 6: Average runtime versus number of dots N for (a) Thomas-Fermi solver and (b) capacitance model solver. Benchmarks were performed on a 2.8 GHz AMD Ryzen 5 7520U processor.

Eq. (13) over integer charge configurations  $\vec{Q} \in \mathbb{Z}^N$  for which the runtime scales exponentially in N begins to dominate. In practice, we expect most use cases to involve no more than ten QDs, as long-range interactions tend to be negligible due to screening from the material and the nearby gates; thus, we focus attention on the cost of computing n(x) in this regime.

Because QDF1ow calculates the capacitance model at each point in the CSD by explicitly solving for n(x), it requires several orders of magnitude more runtime to generate CSDs than simulations based on constant capacitance models. Thus, for applications that require real-time data, faster simulations such as QDsim [17] or QArray [18] may be more suitable. On the other hand, for applications such as generating datasets for training and validation of ML models for autonomous control of QD systems, the higher-fidelity data provided by QDF1ow—including effects such as QDs merging across low barriers—often justifies the additional computational cost.

In addition to its relatively long runtime, QDF1ow has several modeling limitations. While QDF1ow is based on an underlying physical nanowire model, it is designed only to produce qualitatively realistic behavior. For example, gates are modeled as infinite cylinders arranged in a simple, idealized geometry, whereas in real devices the shapes and arrangements of gates can be considerably more complex. Furthermore, the electron density n(x) is calculated only in 1D, an approximation that can introduce errors for systems with non-negligible transverse extent. Finally, the simulation uses a semiclassical approach and therefore does not include correlation effects captured by, for example, the Hubbard model. Taken together, these approximations prevent QDF1ow from generating quantitatively accurate data.

QDF1ow also lacks certain capabilities present in other simulators. For example, it cannot currently model closed systems with a fixed number of charges isolated from the source and drain contacts—a functionality available in QArray [18]. Finally, QDF1ow is configured to model the state that minimizes the energy of the capacitance model, implicitly assuming that the system can transition freely between charge configurations. However, this assumption can break down for large arrays of QDs. For example, if a charge must transition between non-neighboring QDs passing through an intermediate QD that forms a large barrier, it may get "stuck" on one side even if it is energetically favorable to move to the other side. This will result in much more extreme latching effects than QDF1ow can model.

QDFlow has been tested both modularly and holistically, through extensive unit testing and by comparing its output to experimental data. The QDFlow repository includes unit tests for every function in the package, ensuring coverage of all lines of code. The validity of QDFlow has been confirmed by performance of multiple specialized ML models trained on QDFlow-generated data and deployed in real-world applications, as we discuss in Sec. 1 and in Sec. 6.

## 6 Conclusion

Progress toward scalable quantum information technologies based on QD systems depends critically on overcoming the complexity of device operation and calibration with increasing number of QDs. Novel ML-based methods have emerged as powerful tools to address these challenges, but their effectiveness relies on access to large, diverse, and accurately labeled datasets. QDFlow was developed precisely to meet this need.

QDF1ow differs from existing QD simulations in that it fully simulates the charge density function n(x). By integrating a self-consistent Thomas-Fermi solver with a dynamic capacitance model, QDF1ow provides a physics-informed simulation framework that goes beyond constant-capacitance approximations. This enables the generation of CSDs and ray-based data with features that evolve naturally with gate voltages, mimicking experimental behavior such as dot merging and transition slope variation.

The modular data generation tools allow for extensive randomization over physical parameters, yielding highly diverse synthetic datasets suitable for ML applications, while the noise module introduces experimentally relevant effects—including thermal broadening, telegraph noise, latching, and unintended transitions—in a controllable fashion. Together, these features make QDF1ow uniquely positioned to support both the development and benchmarking of ML algorithms implemented in a wide range of tuning procedures, device architectures, and material platforms. Early use cases, such as the QF1ow-lite and QF1ow 2.0 datasets, have already demonstrated QDF1ow's ability to accelerate the training of ML models for global state recognition [9,20], ray-based navigation and charge tuning [12,13], data quality assessment [25], detection of spurious QDs [31], and virtualization of QD arrays [13,14]. As an open-source, extensible platform with comprehensive documentation, QDF1ow is designed to serve as both a research tool and a community resource.

QDF1ow represents a paradigm shift among QD simulators. Whereas other simulations typically rely on constant-capacitance models that impose static couplings regardless of device state, QDFlow ties these parameters directly to the underlying physics through its self-consistent charge density, producing capacitances and observables that evolve dynamically with gate voltages. This distinction not only improves the connection with the experiment but also allows for the capture of nontrivial behaviors—such as QDs merging, fluctuating slopes, and disorder-induced effects—that are inaccessible to static-capacitance approaches.

As QD systems advance toward larger arrays and integration into functional quantum processors, the need for such realism will only grow. QDF1ow package is currently being used to generate datasets for multiple ongoing research projects and we intend to support it for the foreseeable future. Although the current release is stable, we anticipate adding further modules and functionality to the package. Possible future extensions of QDF1ow, including multi-dimensional modeling, adding additional quantum effects, hybridization with experimental feedback loops, and systematic studies of robustness under different noise and disorder regimes, could establish it as a cornerstone for bridging theory, experiment, and ML in the quest for scalable quantum technologies. We have designed the core class structure to allow for seamless addition of new physical parameters and functions, and plan to update the generate module to provide support for parallelization. By releasing QDF1ow as an opensource package, we aim to foster a shared foundation for accelerating progress in quantum dot technologies. We anticipate that the package will not only continue to advance automated QD control but also provide a flexible testbed for exploring broader questions at the intersection of condensed matter physics, quantum information, and machine learning.

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Code availability QDFlow is available on the Python Package Index, with the source code released under the GNU General Public License, and can be installed using pip install QDFlow command. The associated GitHub repository is https://github.com/QDFlow/QDFlow-solver. Documentation is available at https://qdflow-sim.readthedocs.io/. Any discovered bugs should be reported using GitHub issues. If you find this package useful, please star the repository and cite this paper.

# 516 References

- [1] G. Burkard, T. D. Ladd, A. Pan, J. M. Nichol and J. R. Petta, *Semiconductor spin qubits*, Rev. Mod. Phys. **95**(2), 025003 (2023), doi:10.1103/RevModPhys.95.025003.
- [2] A. B. Mei, I. Milosavljevic, A. L. Simpson, V. A. Smetanka, C. P. Feeney, S. M. Seguin, S. D. Ha, W. Ha and M. D. Reed, *Optimization of quantum-dot qubit fabrication via machine learning*, Appl. Phys. Lett. **118**(20), 204001 (2021), doi:10.1063/5.0040967.
- [3] C. Shen, W. Zhan, K. Xin, M. Li, Z. Sun, H. Cong, C. Xu, J. Tang, Z. Wu, B. Xu, Z. Wei, C. Xue et al., Machine-learning-assisted and real-time-feedback-controlled growth of inas/gaas quantum dots, Nat. Commun. 15(1), 2724 (2024), doi:10.1038/s41467-024-47087-w.
- [4] D. Schug, T. J. Kovach, M. A. Wolfe, J. Benson, S. Park, J. P. Dodson, J. Corrigan, M. A. Eriksson and J. P. Zwolak, Automation of quantum dot measurement analysis via explainable machine learning, Mach. Learn.: Sci. Technol. 6(1), 015006 (2025), doi:10.1088/2632-2153/ada087.
- [5] E. Corcione, F. Jakob, L. Wagner, R. Joos, A. Bisquerra, M. Schmidt, A. D. Wieck, A. Ludwig, M. Jetter, S. L. Portalupi, P. Michler and C. Tarín, *Machine learning enhanced evaluation of semiconductor quantum dots*, Sci. Rep. 14(1), 4154 (2024), doi:10.1038/s41598-024-54615-7.
- [6] J. D. Teske, S. S. Humpohl, R. Otten, P. Bethke, P. Cerfontaine, J. Dedden, A. Ludwig, A. D.
   Wieck and H. Bluhm, A machine learning approach for automated fine-tuning of semicon ductor spin qubits, Appl. Phys. Lett. 114(13), 133102 (2019), doi:10.1063/1.5088412.
- [7] R. Durrer, B. Kratochwil, J. Koski, A. Landig, C. Reichl, W. Wegscheider, T. Ihn and E. Greplova, *Automated tuning of double quantum dots into specific charge states using neural net*works, Phys. Rev. Appl. **13**(5), 054019 (2020), doi:10.1103/PhysRevApplied.13.054019.

- [8] J. Darulová, S. J. Pauka, N. Wiebe, K. W. Chan, G. C. Gardener, M. J. Manfra, M. C. Cassidy
   and M. Troyer, Autonomous tuning and charge-state detection of gate-defined quantum dots,
   Phys. Rev. Appl. 13(5), 054005 (2020), doi:10.1103/PhysRevApplied.13.054005.
- [9] J. P. Zwolak, T. McJunkin, S. S. Kalantre, J. Dodson, E. R. MacQuarrie, D. Savage,
   M. Lagally, S. Coppersmith, M. A. Eriksson and J. M. Taylor, Autotuning of double dot devices in situ with machine learning, Phys. Rev. Appl. 13(3), 034075 (2020),
   doi:10.1103/PhysRevApplied.13.034075.
- [10] N. M. van Esbroeck, D. T. Lennon, H. Moon, V. Nguyen, F. Vigneau, L. C. Camenzind, L. Yu, D. M. Zumbühl, G. A. D. Briggs, D. Sejdinovic and N. Ares, *Quantum device* fine-tuning using unsupervised embedding learning, New J. Phys. **22**(9), 095003 (2020), doi:10.1088/1367-2630/abb64c.
- [11] H. Moon, D. T. Lennon, J. Kirkpatrick, N. M. van Esbroeck, L. C. Camenzind, L. Yu, F. Vigneau, D. M. Zumbühl, G. A. D. Briggs, M. A. Osborne, D. Sejdinovic, E. A. Laird et al., Machine learning enables completely automatic tuning of a quantum device faster than human experts, Nat. Commun. 11(1), 4161 (2020), doi:10.1038/s41467-020-17835-9.
- J. P. Zwolak, T. McJunkin, S. S. Kalantre, S. F. Neyens, E. R. MacQuarrie, M. A. Eriksson and J. M. Taylor, *Ray-based framework for state identification in quantum dot devices*, PRX Quantum 2(2), 020335 (2021), doi:10.1103/PRXQuantum.2.020335.
- [13] J. Ziegler, F. Luthi, M. Ramsey, F. Borjans, G. Zheng and J. P. Zwolak, *Tuning arrays with rays: Physics-informed tuning of quantum dot charge states*, Phys. Rev. Appl. 20(3), 034067 (2023), doi:10.1103/PhysRevApplied.20.034067.
- [14] A. S. Rao, D. Buterakos, B. van Straaten, V. John, C. X. Yu, S. D. Oosterhout, L. Stehouwer,
   G. Scappucci, M. Veldhorst, F. Borsoi and J. P. Zwolak, Modular Autonomous Virtualization System for Two-Dimensional Semiconductor Quantum Dot Array, Phys. Rev. X 15(2),
   021034 (2025), doi:10.1103/PhysRevX.15.021034.
- 566 [15] G. A. Oakes, J. Duan, J. J. L. Morton, A. Lee, C. G. Smith and M. F. G. Zalba, *Auto-matic virtual voltage extraction of a 2x2 array of quantum dots with machine learning*, doi:10.48550/arXiv.2012.03685 (2024).
- [16] J. P. Zwolak, J. M. Taylor, R. W. Andrews, J. Benson, G. W. Bryant, D. Buterakos, A. Chatterjee, S. Das Sarma, M. Eriksson, E. Greplová, M. J. Gullans, F. Hader et al., Data needs and challenges for quantum dot devices automation, npj Quantum Inf. 10(1), 105 (2024), doi:10.1038/s41534-024-00878-x.
- [17] V. Gualtieri, C. Renshaw-Whitman, V. Hernandes and E. Greplova, *Qdsim: A user-friendly* toolbox for simulating large-scale quantum dot devices, SciPost Phys. Codebases p. 46 (2025), doi:10.21468/SciPostPhysCodeb.46.
- [18] B. van Straaten, J. Hickie, L. Schorling, J. Schuff, F. Fedele and N. Ares, *Qarray: A gpu-accelerated constant capacitance model simulator for large quantum dot arrays*, SciPost Phys. Codebases p. 35 (2024), doi:10.21468/SciPostPhysCodeb.35.
- 579 [19] J. A. Krzywda, W. Liu, E. van Nieuwenburg and O. Krause, *QDarts: A quantum dot array* 580 transition simulator for finding charge transitions in the presence of finite tunnel couplings, 581 non-constant charging energies and sensor dots, SciPost Phys. Codebases p. 43 (2025), 582 doi:10.21468/SciPostPhysCodeb.43.

- [20] S. S. Kalantre, J. P. Zwolak, S. Ragole, X. Wu, N. M. Zimmerman, M. D. Stewart and J. M. Taylor, *Machine learning techniques for state recognition and auto-tuning in quantum dots*, npj Quantum Inf. **5**(1), 6 (2019), doi:10.1038/s41534-018-0118-7.
- J. P. Zwolak, S. S. Kalantre, X. Wu, S. Ragole and J. M. Taylor, *QFlow lite dataset: A machine-learning approach to the charge states in quantum dot experiments*, PLoS ONE
   13(10), e0205844 (2018), doi:10.1371/journal.pone.0205844.
- National Institute of Standards and Technology, *Qflow 2.0: Quantum dot data for machine* learning, Database: data.nist.gov, https://doi.org/10.18434/T4/1423788 (2022).
- <sup>591</sup> [23] A. Zubchenko, D. Middlebrooks, T. Rasmussen, L. Lausen, F. Kuemmeth, A. Chatterjee and J. P. Zwolak, *Autonomous bootstrapping of quantum dot devices*, Phys. Rev. Appl. <sup>593</sup> **23**(1), 014072 (2025), doi:10.1103/PhysRevApplied.23.014072.
- J. P. Zwolak, S. S. Kalantre, T. McJunkin, B. J. Weber and J. M. Taylor, Ray-based classification framework for high-dimensional data, In Third Workshop on Machine Learning and the Physical Sciences (NeurIPS 2020), pp. 1–7. Vancouver, Canada, ArXiv:2010.00500 (2020).
- 598 [25] J. Ziegler, T. McJunkin, E. S. Joseph, S. S. Kalantre, B. Harpt, D. E. Savage,
  599 M. G. Lagally, M. A. Eriksson, J. M. Taylor and J. P. Zwolak, *Toward robust au-*600 totuning of noisy quantum dot devices, Phys. Rev. Appl. 17(2), 024069 (2022),
  601 doi:10.1103/PhysRevApplied.17.024069.
- [26] D. L. Buterakos, S. S. Kalantre, J. Ziegler, J. M. Taylor and J. P. Zwolak, QDF1ow: *A Python package for physics simulations of quantum dot devices*, GitHub (2025).
- 604 [27] O. Ciftja, Electrostatic interaction energy between two coaxial parallel uniformly charged disks, Results Phys. **15**, 102684 (2019), doi:10.1016/j.rinp.2019.102684.
- [28] A. Alexandradinata, N. P. Armitage, A. Baydin, W. Bi, Y. Cao, H. J. Changlani, E. Chertkov,
   E. H. da Silva Neto, L. Delacretaz, I. E. Baggari, G. M. Ferguson, W. J. Gannon et al.,
   The future of the correlated electron problem, SciPost Phys. Comm. Rep. p. 8 (2025),
   doi:10.21468/SciPostPhysCommRep.8.
- [29] J. Darulová, M. Troyer and M. C. Cassidy, Evaluation of synthetic and experimental training data in supervised machine learning applied to charge-state detection of quantum dots,
   Mach. Learn.: Sci. Technol. 2(4), 045023 (2021), doi:10.1088/2632-2153/ac104c.
- [30] C. W. J. Beenakker, *Theory of coulomb-blockade oscillations in the conductance of a quantum dot*, Phys. Rev. B **44**, 1646 (1991), doi:10.1103/PhysRevB.44.1646.
- [31] J. Ziegler, F. Luthi, M. Ramsey, F. Borjans, G. Zheng and J. P. Zwolak, Automated extraction
   of capacitive coupling for quantum dot systems, Phys. Rev. Appl. 19(5), 054077 (2023),
   doi:10.1103/PhysRevApplied.19.054077.