Recent Results from the Long-Baseline (LBL) Neutrino Oscillation Experiments

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Abstract

The results from the current long-baseline neutrino oscillation experiments are reviewed. These experiments are designed to measure the remaining unknown neutrino oscillation parameters via the oscillation of accelerator neutrinos over long distances.
The performance of these experiments and their results are described and discussed, giving a precise picture of the current status of the measurements for the neutrino mass ordering, the value of Δm_{32}^2, the θ_{23} and the lepton CP-violating phase, δ_{CP}.

Contents

1 Introduction

Long-baseline (LBL) neutrino oscillation experiments have provided a great progress in our knowledge of the neutrino properties compared to the experiments measuring neutrinos from natural sources. Thanks to their efficient design and operation, they have been able to get us closer to the measurement of the most challenging neutrino oscillation parameters, those are the θ_{23} mixing angle, the neutrino mass ordering and the CP-violating phase of the lepton sector.

In this conference paper the current status of the LBL neutrino oscillation experiments. First, in section 2, reviewing and summarizing the physics of neutrino oscillations with its main remaining unknowns, and how LBL are built so they can provide the most precise measurements for these unknown parameters. Then in section 3, the current LBL experiments are reviewed and their results discussed to give an overall picture of the current status of neutrino oscillation physics. The T2K, NOνA and MINOS/MINOS+ experiments are described in subsections 3.1, 3.2 and 3.4. The OPERA experiment was covered by a dedicated talk in this same conference, so it is not addressed here.

Finally, the results of all these experiments are summarized in section 4 and the most important measurements from these experiments are highlighted in section 5.

2 Physics of Neutrino Oscillations

The first evidence of neutrino oscillations was provided by the Super-Kamiokande experiment in 1998 and via the analysis of atmospheric neutrinos. This confirmed the theoretical hypothesis of neutrino oscillations done by B. Pontecorvo in 1957.

The neutrino oscillations arise from the fact that neutrinos are not massless as assumed by the Standard Model (SM), making neutrino oscillations the first evidence of physics beyond the SM. The SM predicts the existence of three neutrinos and this is the framework assumed for the rest of this paper.

Neutrinos do not share the same flavor (interaction) and mass (propagation) eigenstates and they are transformed by a non-diagonal unitary matrix with four degrees of freedom, parametrized by three mixing angles θ_{12}, θ_{13} and θ_{23} and a complex CP-violating phase, δ_{CP}. These flavor and mass eigenstates are mixed through the PMNS matrix,

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = U_{PMNS} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix} \tag{1}$$

$$U_{PMNS} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta_{CP}} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta_{CP}} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \tag{2}$$

where $c_{ij} = \cos\theta_{ij}$ and $s_{ij} = \sin\theta_{ij}$.

This means that after neutrinos have propagated freely through space they can be detected with a different flavor from that of their origin. This phenomenon is called neutrino oscillations and the probability of a neutrino to change its flavor after a free propagation in vacuum is given by the following expression:

$$P_{\nu_l \to \nu_{l'}}(L/e) \approx \sum_{ij} U_{PMNS}^{l',i}(U_{PMNS}^{l,i})^*(U_{PMNS}^{l',j})^* U_{PMNS}^{l,j} e^{-i\frac{\Delta m_{ij}^2}{2}\frac{L}{E}} \tag{3}$$

This means that the neutrino oscillation probabilities depend on the four parameters of the PMNS matrix, the ratio between the distance traveled by the neutrinos and their energy and, also, on two independent mass square differences.

In the three flavor neutrino framework, there are six independent oscillation parameters, four from the PMNS matrix and the two neutrino square mass differences.

$$\Delta m_{21}^2 = m_2^2 - m_1^2, \ \Delta m_{31}^2 = m_3^2 - m_1^2 \quad (4)$$

The third mass square difference is just a linear combination of the other two $\Delta m_{32}^2 = \Delta m_{31}^2 - \Delta m_{21}^2$.

Figure 1: Two possible neutrino mass orderings allowed.

This definition allows the existence of two possibilities for the ordering of the neutrino masses, normal (neutrino third mass eigenstate is the heaviest) and inverted (neutrino third mass eigenstate is the lightest), as shown in figure 1.

As LBL experiments mainly produce muon (anti)neutrinos to be propagated to the detector, there are basically two oscillation channels that matter for measuring the oscillation parameters.

The disappearance channel is the survival probability of the produced muon (anti)neutrinos at the accelerator facility. This channel is most sensitive to the θ_{23} and the neutrino mass ordering.

$$P(\overset{(-)}{\nu_\mu} \to \overset{(-)}{\nu_\mu}) \cong 1 - 4\sin^2\theta_{23}\cos^2\theta_{13}^M(1 - \sin^2\theta_{23}^2\cos^2\theta_{13}^M)\sin^2\left(\tilde{\Delta}\frac{L}{E}\right) \quad (5)$$

where,

$$\tilde{\Delta} = \frac{\Delta m_{32}^2 + \Delta m_{21}^2\sin^2\theta_{12} + \Delta m_{21}^2\cos\delta_{CP}\sin 2\theta_{12}\sin\theta_{13}\tan\theta_{23}}{4}$$

$$\sin^2\theta_{13}^M = \frac{\sin^2 2\theta_{13}}{\sin^2 2\theta_{13} + (A - \cos 2\theta_{13})^2}, \ A = \sqrt{2}G_F N_e\frac{2E}{\Delta m_{31}^2} \quad (6)$$

and N_e is the electron density of the Earth.

The appearance channel, on the other hand, is the probability of the muon (anti)neutrinos to be transformed into electron (anti)neutrinos. This channel is most sensitive to the θ_{13} mixing angle, which dominates the expression, the neutrino mass hierarchy and to the CP-violating phase, δ_{CP}.

$$P(\overset{(-)}{\nu_\mu} \to \overset{(-)}{\nu_e}) \cong \underbrace{\sin^2\theta_{23}\frac{\sin^2 2\theta_{13}}{(A-1)^2}\sin^2\left((A-1)\Delta\frac{L}{E}\right)}_{\text{leading term, } \theta_{13}} + \alpha^2\cos^2\theta_{23}\frac{\sin^2 2\theta_{12}}{A^2}\sin^2\left(A\Delta\frac{L}{E}\right)$$

$$+ \frac{\alpha J_{CP}}{A(1-A)}\sin\left(A\Delta\frac{L}{E}\right)\sin\left(\Delta(1-A)\frac{L}{E}\right)\left(\underbrace{\cot\delta_{CP}\cos\left(\Delta\frac{L}{E}\right)}_{\text{CP conserving term}} \underbrace{\pm\sin\left(\Delta\frac{L}{E}\right)}_{\text{CP violating term}}\right)$$
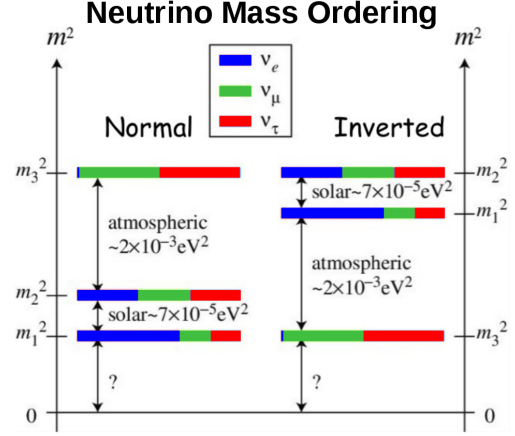
$$(7)$$

where,

$$\alpha = \frac{\Delta m_{21}^2}{\Delta m_{31}^2}, \ \Delta = \frac{\Delta m_{31}^2}{4}, \ J_{CP} = \cos\theta_{13}\sin 2\theta_{12}\sin 2\theta_{23}\sin 2\theta_{13}\sin\delta_{CP} \tag{8}$$

The expressions above differ from those obtained from equation 3 as they contain additional terms due to the fact that neutrinos do not travel through vacuum, but through the Earth's crust. In terms of oscillation probabilities, this only affects to the electron neutrinos and antineutrinos as they are the only ones able to interact via coherent forward scattering with the electrons present in matter, as seen in equation 6.

3   LBL Neutrino Oscillation Experiments

The basic setup of current LBL neutrino experiments consists of near and far detectors to which (anti)neutrinos produced at accelerators are thrown.

Since the neutrino probabilities are modulated by L/E (baseline over neutrino energy) ratio, LBL experiments are designed so this ratio is such that the disappearance and appearance channels are optimized.

The goal of long-baseline neutrino experiments is to measure the remaining neutrino unknown parameters, with special focus on the CP phase due to its implications, being a potential explanation for the matter-antimatter imbalance in our universe.

3.1   The T2K Experiment

The T2K experiment is located in Japan and its focus is in the measurement of the θ_{23}, θ_{13} and δ_{CP}. It uses the J-PARC neutrino facility at Tokai, which produces mainly ν_μ and $\bar{\nu}_\mu$, depending on the beam mode. These neutrinos are then detected at the ND280 near detector facility and the Super-Kamiokande far detector.

Figure 2: Geographical view of the T2K experiment layout.

The T2K beam

The J-PARC neutrino beam has been operating this year with a mean power of 485 kW, achieving maxima of more than 500 kW. The total amount of protons-on-target (POT) accumulated during the T2K operation is $3.2 \cdot 10^{21}$, $1.51 \cdot 10^{21}$ in neutrino mode and $1.65 \cdot 10^{21}$ in antineutrino mode.
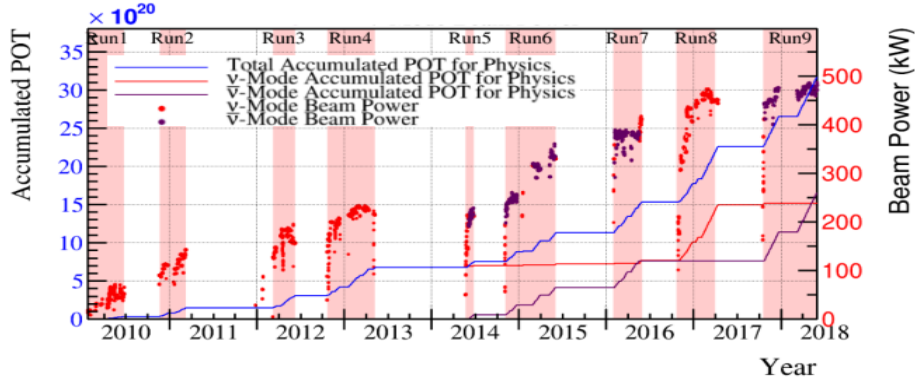
Figure 3: Accumulated POT and neutrino beam power output during the T2K operation.

The direction of the beam is not aligned with the ND280 near detector and the Super-Kamiokande far detector, but 2.5^0 off-axis. T2K was the first experiment to implement this technique due to its advantages. As shown in figure 4, with the 2.5^0 off-axis setup, the neutrino spectrum is narrower than for other configurations peaking at 0.7 GeV, just where the maximum of the appearance channel and the minimum of the disappearance channels are.

Given to the enormous success during the T2K operation, it has been agreed to extend the operation of the J-PARC neutrino beam until 2026 with the aim of achieving $2 \cdot 10^{22}$ POT. This will suppose the extension of the T2K experiment, T2K phase-II.
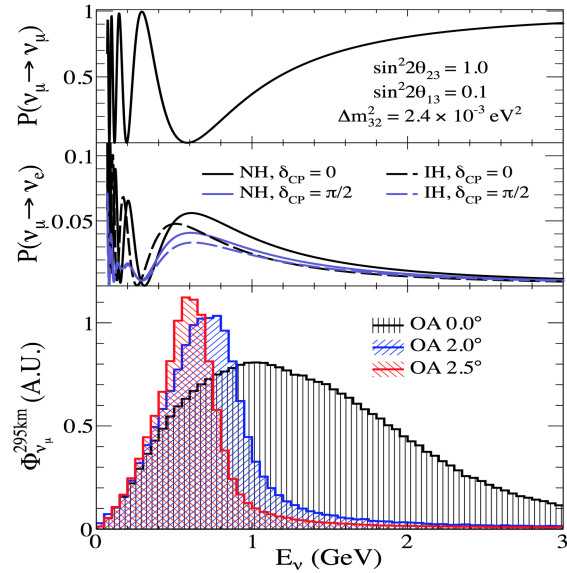

Figure 4: The plots show the T2K disappearance and appearance channel probabilities as well as the neutrino spectrum at the far detector assuming different off-axis configurations.
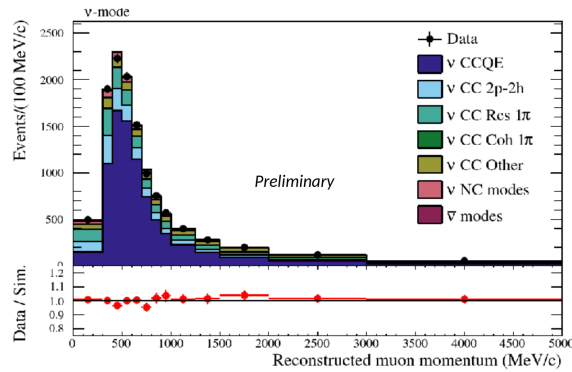
The T2K detectors

T2K has a near detector as well, which performs cross-section, energy spectrum and flux studies of the neutrino beam. This provides great knowledge about the neutrino characteristics, decreasing the associated systematic errors. ND280 is a compendium of various facilities, placed 280 m from J-PARC. It is formed by INGRID and ND280.

Figure 5: Comparison of data and simulated muon reconstructed spectrum at the T2K near detector, ND280.

- ND280: This is placed 2.5^0 off-axis and composed of π^0 detector and calorimeter, an electromagnetic calorimeter, a muon detector, fine grained detectors (FGD) and argon time projection chambers (TPCs). It will be upgraded for phase-II to reduce systematics up to 4%.

- INGRID: This detector is on-axis and is a scintillation light detector made up by sixteen modules of iron plates and and eleven tracking scintillators each.

Due to the high neutrino flux at the near detector, its data is very useful to carry out studies concerning neutrino cross-section and studies to reduce the systematic errors related to the neutrino flux and interactions at the far detector.

Super-Kamiokande is the far detector, a water-Cherenkov detector with 50 kton of ultra-pure water located in the Kamioka mine under 1000 m of rock (2700 m.w.e.). It is located 295 km from the neutrino beam and optically divided into inner and outer detector.

- The inner detector is used for physics analysis and composed by 11,129 20"-PMT facing inwards with 40% photo-coverage

- The outer detector is used as veto for cosmic rays and made up of 1,884 8"-PMT facing outwards

Super-Kamiokande is currently being upgraded and refurbished for dissolving gadolinium (Gd) into the ultra-pure water (SuperK-Gd), enhancing hugely its neutron-tagging capabilities. SuperK-Gd will operate during T2K phase-II.

In addition, the NA61/SHINE hadron production experiment at CERN provides input for reducing the T2K flux uncertainties to $\sim 5\%$.
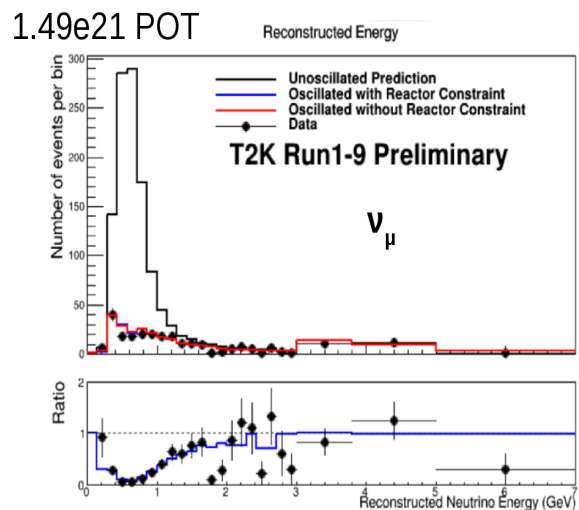

Figure 6: Comparison of reconstructed neutrino flux at the far detector of data and oscillated and unoscillated simulations.

T2K neutrino oscillation results

The analysis strategy for the oscillation parameters is to compare the observed event rates at SK with the predictions under oscillation hypothesis with inputs from the near detectors. The next table shows the rate prediction for different values of δ_{CP}.

Sample	Prediction				Data
	$\delta_{CP} = -\pi/2$	$\delta_{CP} = 0$	$\delta_{CP} = \pi/2$	$\delta_{CP} = \pi$	
FHC 1R(ing) μ	268.5	268.2	268.5	268.9	243
RHC 1R(ing) μ	95.5	95.3	95.5	95.8	102
FHC 1R e 0 decay-e	73.8	61.6	50.0	62.2	75
FHC 1R e 1 decay-e	6.9	6.0	4.9	5.8	15
RHC 1R e 0 decay-e	11.8	13.4	14.9	13.2	9

The results for the θ_{23} and Δm_{32}^2 from T2K with reactor data constraints are shown in figure 7. These results show a preference for the θ_{23} second octant, although lower values are less than 2σ away. Since the neutrino mass ordering is yet to be determined, the fit is done for both, normal and inverted, orderings.
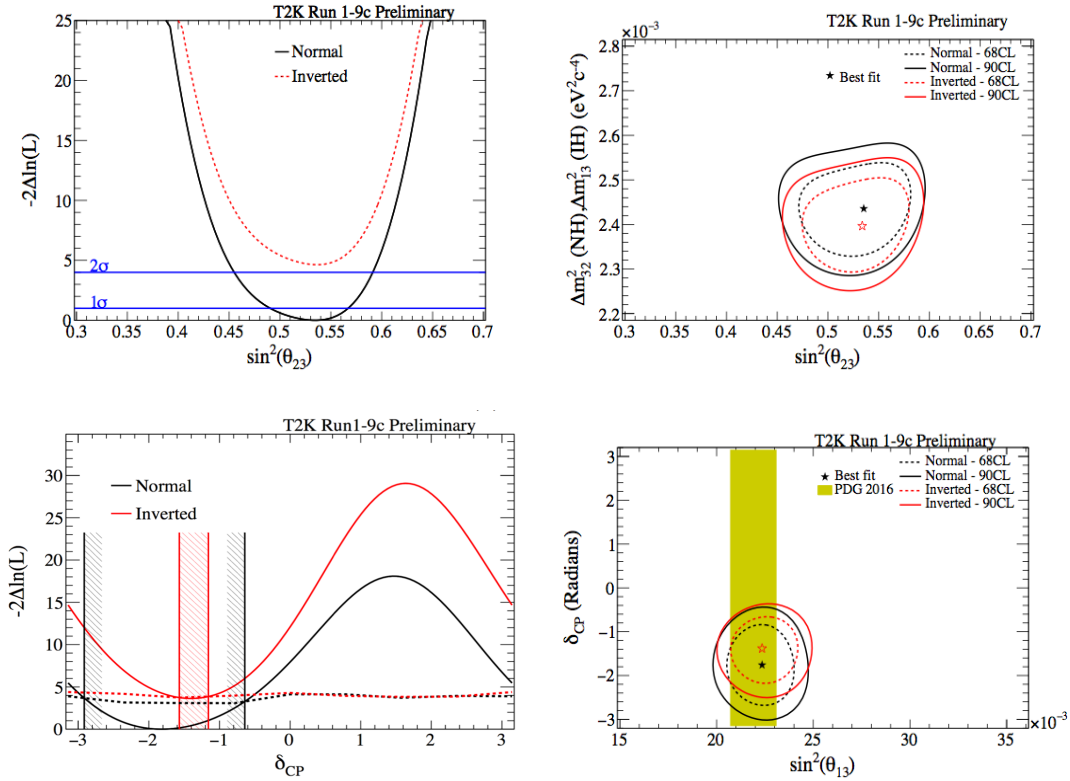

Figure 7: T2K latest results for the relevant oscillation parameters assuming the constraints given by reactor experiments and for both mass orderings. From left to right and from top to bottom: χ^2 curve for θ_{23}, 2D contours for Δm_{32}^2 and θ_{23}, χ^2 curve for δ_{CP} and 2D contours for δ_{CP} and θ_{13}.

	Normal Ordering	**Inverted Ordering**
$\sin^2\theta_{23}$	$0.536^{+0.031}_{-0.046}$	$0.536^{+0.031}_{-0.041}$
Δm^2_{32} $(10^{-3}eV^2)$	2.434 ± 0.064	$2.410^{+0.062}_{-0.063}$

Table 1: Best fit values of the T2K experiment oscillation analysis for $\sin^2\theta_{23}$ and Δm^2_{32} in both mass ordering scenarios.

	Mass Ordering	δ_{CP} (rad)
Best Fit	NH (2.0σ)	-0.57π

Table 2: Best fit values of the T2K experiment oscillation analysis for the neutrino mass ordering and the CP-pahse.

The results for the δ_{CP} parameter show that the best fit is placed at large and negative values for both neutrino mass orderings, disfavouring CP-conserving values by more than the 2σ.

3.2 The NOνA Experiment

The NOνA experiment is located in the US. It is also composed by near and far detectors and uses the Fermilab main injector as neutrino source.

The NOνA beam

The Fermilab neutrino main injector (NuMI) produces muon neutrinos and antineutrinos and can also run in neutrino or antineutrino mode. This is the most powerful neutrino beam in the world, it has been running at the nominal 700 kW power since January 2017. Since the start of the NOνA experiment, $8.85 \cdot 10^{20}$ POT in neutrino mode and $6.91 \cdot 10^{20}$ POT in antineutrino mode have been accumulated.
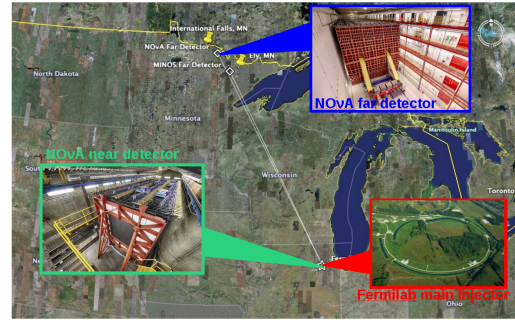

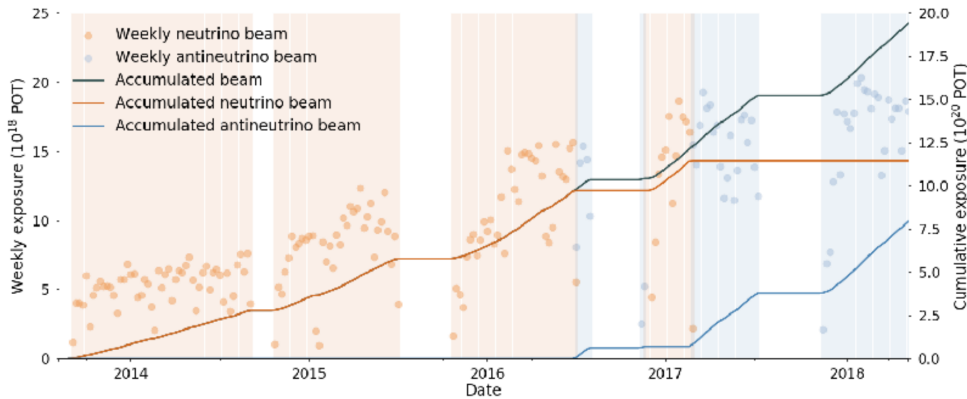Figure 8: Geographical view of the NOνA experiment layout.

Figure 9: Accumulated POT of the NOνA experiment with time in both, neutrino and antineutrino beam modes.
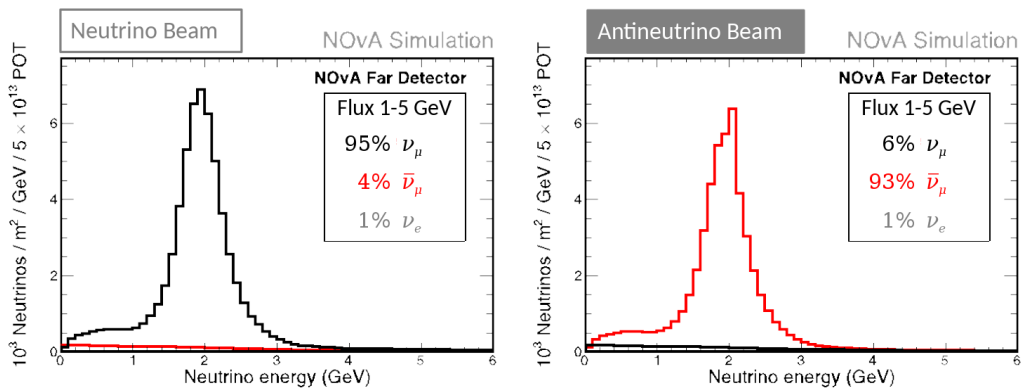
Figure 10: Neutrino spectrum simulation as seen by the NOνA far detector assuming no oscillations.

The mean neutrino energy is $\langle E_\nu \rangle \sim 1.9$ GeV and directed 14.6 mrad ($\sim 0.84^0$) off-axis with respect to the far and near detectors. As in T2K, this technique provides a narrow neutrino spectrum at the appearance maximum and disappearance minimum, optimizing the measurement of the neutrino oscillation parameters.

The NOνA detectors

The NOνA experiment is composed by two identical, except for the size, detectors and located 1 km (near detector) and 810 km (far detector) from the neutrino production point.
These detectors are tracking calorimeters made up of 344,000 cells of extruded and highly reflective plastic PVC filled with liquid scintillator. Each cell of the detectors is 3.9 cm wide, 6.0 cm deep.

- Near detector: Each cell is 3.9 m long and contains a total mass of 290 ton. To enhance muon containment, the downstream end has an additional ten layers of 10-cm-thick steel plates.

- Far detector: Each cell is 15.5 m long and it contains 14 kton.

The signal from each liquid scintillator cell is read out through a wavelength-shifting fiber (WLS). The fiber-end readout consists of a single pixel of a 32 pixel avalanche photo diode (APD) array.

The near detector is located about 100 m underground, serving for reducing the systematic uncertainties related to the flux predictions and also conducts cross-section studies. The fact that near and far detectors share the same technology and setup is crucial for the understanding and cancellation of the systematic errors.
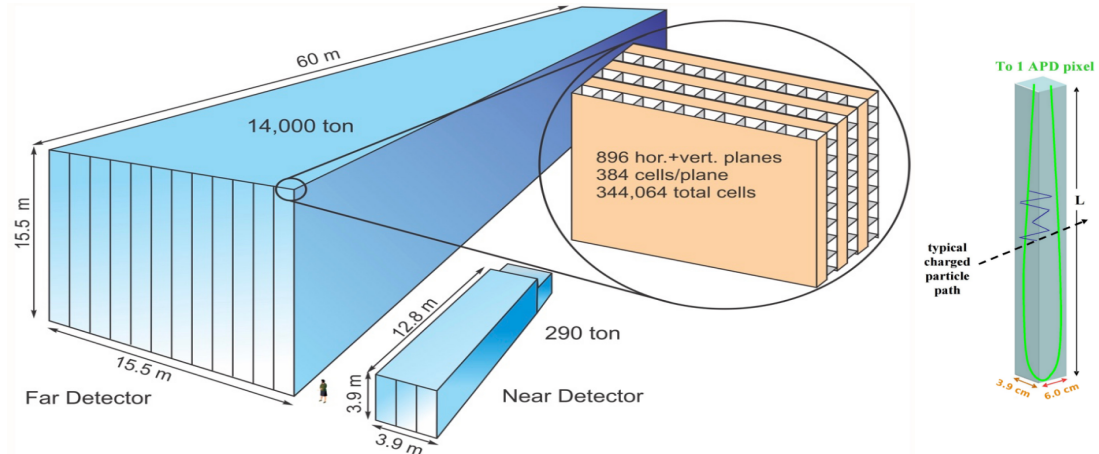
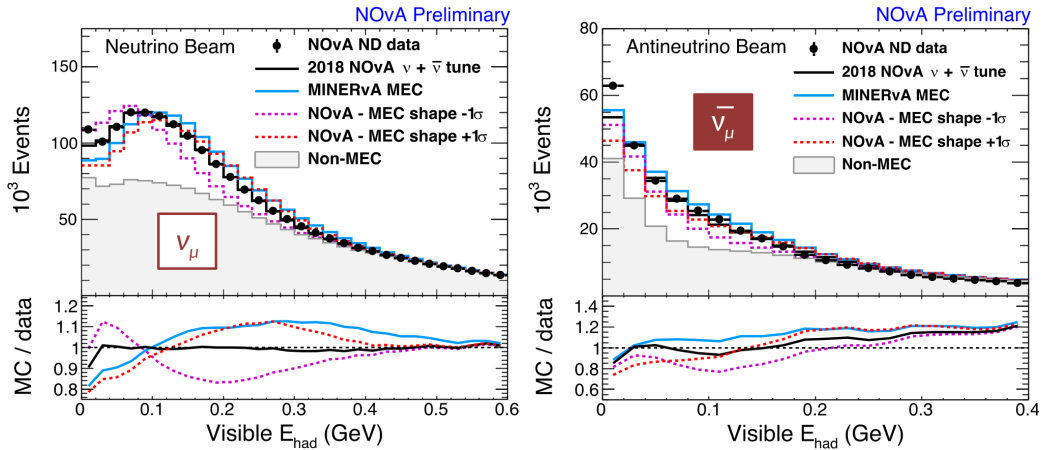Figure 11: Schematic view of the NOνA near and far detectors with their components.

Figure 12: NOνA neutrino spectrum at the near detector for both beam configurations. The Monte Carlo simulation is tuned according to the inputs from the data in order to obtain a more accurate simulation for the far detector neutrino flux and cross-section.

The far detector is placed on the surface under a concrete and barite overburden, which stops a significant fraction of the cosmic rays.

NOνA neutrino oscillation results

Despite being very different experiments, the NOνA and T2K analysis strategies are the same. The far detector event rates are compared with the oscillation predictions, and near detector data is used to reduce uncertainties related to the beam flux and the cross-section interactions.

Figure ?? shows different predictions for the NOνA assuming different values of the neutrino oscillation parameters together with the actual data point in terms of the neutrino and antineutrino events rates. Data agrees with simulation showing a preference for the normal mass ordering and the second octant of θ_{23}.
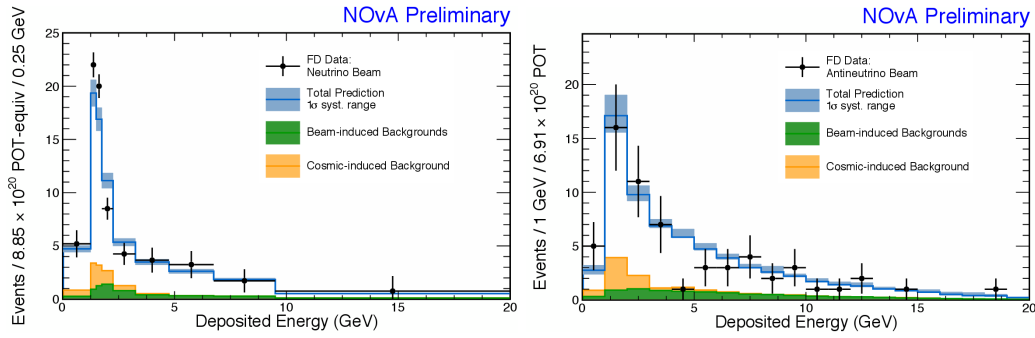
Figure 13: Simulation and data reconstructed neutrino spectrum at the far detector.
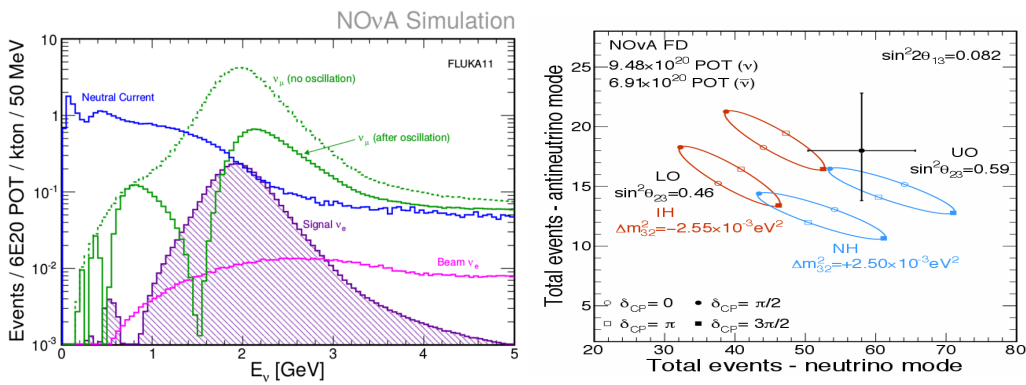

Figure 14: Left plot shows the reconstructed neutrino spectrum from simulation and data at the far detector. Right plot shows a comparison of oscillated event rates between data and Monte Carlo simulation.

Next, the results of the NOνA experiment are summarized in figures 15 and 16. These results are in agreement with the previous ones from T2K, this results in more complete scenario of the remaining unknowns of the neutrino oscillation parameters.
The normal mass ordering and the upper (second) octant of θ_{23} are preferred, and there is also a slight preference for values of δ_{CP} close to $\pi/4$.
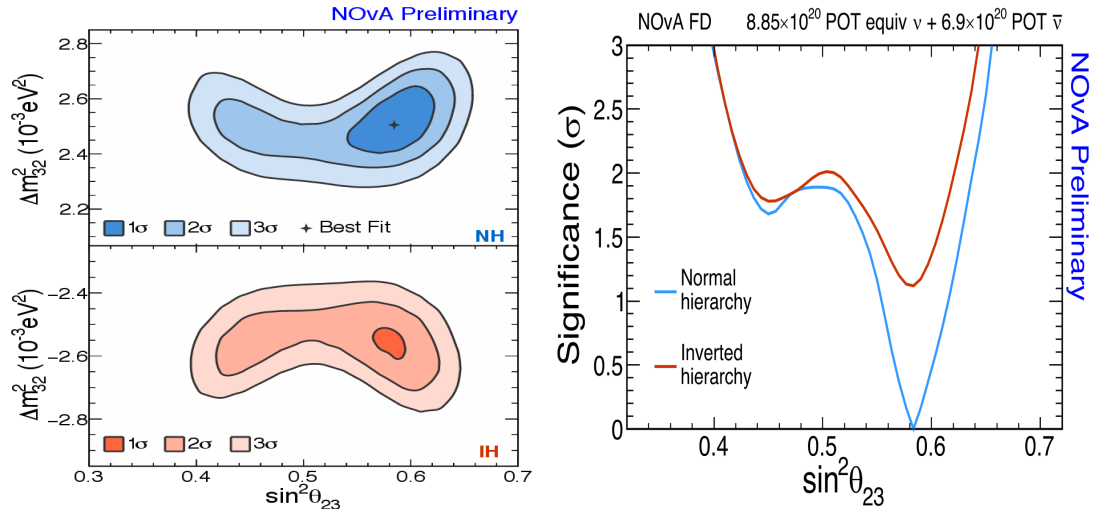Table 3 shows the best fit values given by the current NOνA data.

Figure 15: NOνA latest results for Δm_{32}^2 and θ_{23}. Left plot shows the 2D contours for the Δm_{32}^2 and θ_{23} parameters and assuming both neutrino mass orderings. Right plot shows the χ^2 curve for θ_{23}.
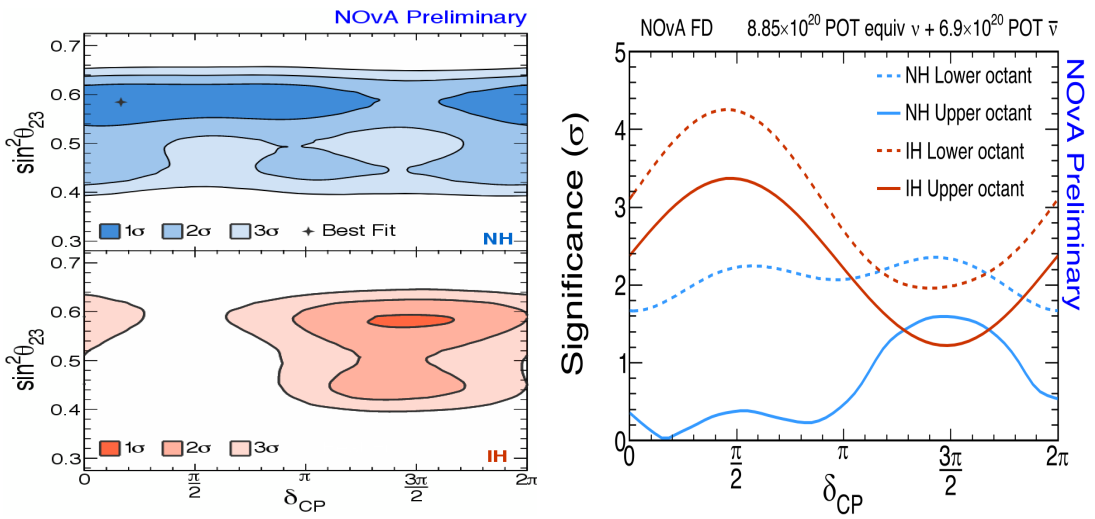

Figure 16: NOνA latest results for θ_{23} and δ_{CP}. Left plot shows the 2D contours for the θ_{23} and the δ_{CP} parameters and assuming both neutrino mass orderings. Right plot shows the χ^2 curve for δ_{CP}.

	Mass Ordering	$\sin^2\theta_{23}$	Δm^2_{32} (10^{-3} eV^2)	δ_{CP}
Best Fit	NH (1.8σ)	0.58 ± 0.03	$2.51^{+0.12}_{-0.08}$	0.17π

Table 3: Best fit values of the NOνA experiment oscillation analysis.

3.3   T2K and NOνA Joint Neutrino Oscillation Analysis

Given the huge success of the T2K and NOνA experiments, it has been agreed, by the two collaborations, the formation of a working group to perform a combined analysis of their data in order to enhance the measurements of neutrino oscillation parameters made by each experiment individually. This joint analysis is foreseen for 2021.

3.4   The MINOS/MINOS+ Experiment

MINOS was mainly dedicated to measure the atmospheric oscillation parameters and MINOS+ is more focused on the additional sterile neutrinos search.

The MINOS and MINOS+ beam

They use the NuMI beam, the same as the NOνA experiment:

- MINOS period: The neutrino mean energy is ~ 3 GeV and has accumulated during its operation $10.56 \cdot 10^{20}$ POT in ν-mode and $3.36 \cdot 10^{20}$ POT in $\bar{\nu}$-mode.

- MINOS+ period: The neutrino mean energy is ~ 7 GeV and, so far, has accumulated $9.69 \cdot 10^{20}$ POT in ν-mode.
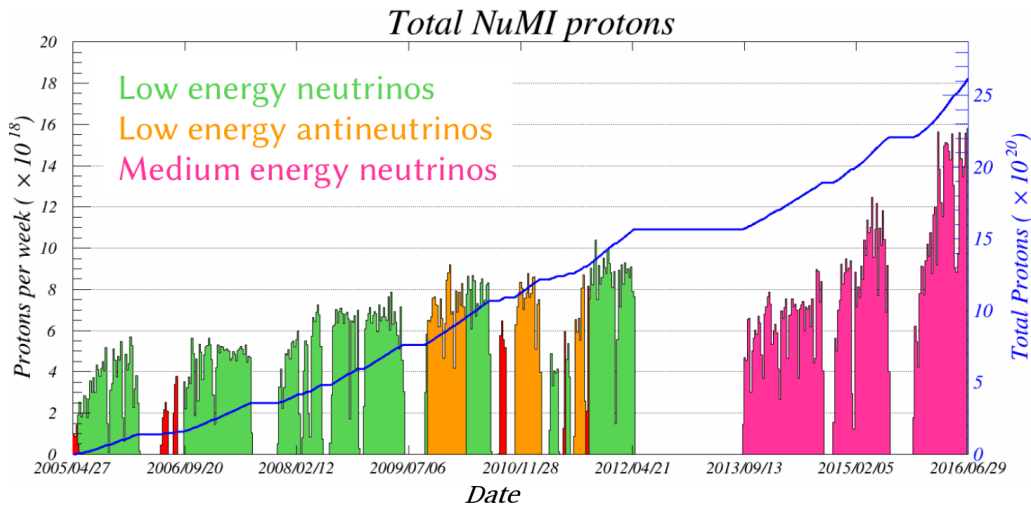

Figure 17: Accumulation of POT by the MINOS and MINOS+ experiments during their operation.

The MINOS and MINOS+ detectors

As happens for the NOνA detector, both, near and far, detectors share the same technology, but in this case they are aligned with the beam axis, do not use the previously

explained off-axis layout.

The two MINOS detectors are iron-scintillator tracking calorimeters which consist of planes of steel and planes of 1 cm thick plastic scintillator. Both detectors are magnetized with a ~1.3 T magnetic field, allowing the identification of the charged particles and improving their energy reconstruction.
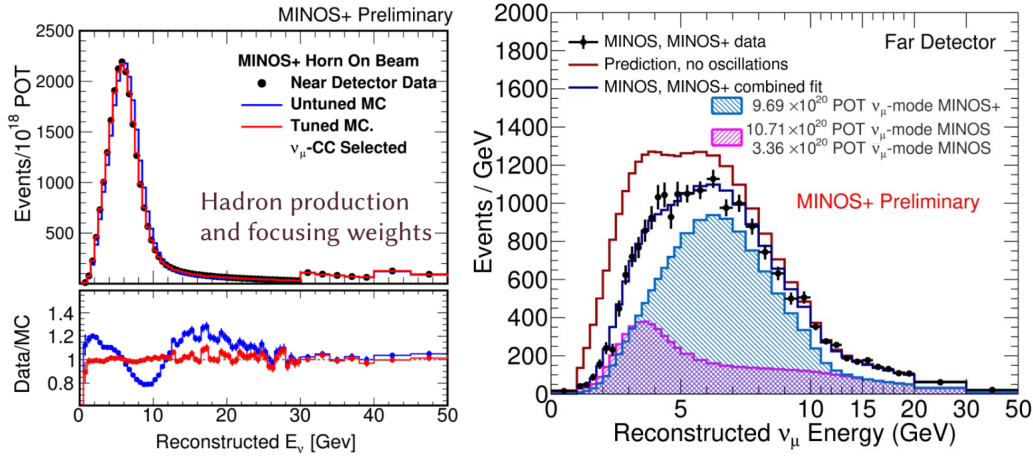

Figure 18: Comparison plots of the reconstructed neutrino spectrum at near and far detectors.

- Near Detector: It is located 1 km from the neutrino target and 100 m underground, containing 1 kton of mass.

- Far Detector: Located 735 km from the neutrino target in the Soudan mine, 716 m underground and has 5.4 kton mass.

As in the previous experiments, the near detector has a crucial role in reducing the systematic uncertainties at the far detector, particularly in this case, where both detectors share the same technology.

MINOS and MINOS+ neutrino oscillation results

The analysis strategy of MINOS and MINOS+ for the measurement of neutrino oscillation parameters is similar to T2K and NOνA experiments.

Figure 19 shows the current results from the combined analysis of MINOS and MINOS+.

The value of Δm^2_{32} is consistent with the best fit values of the previous experiments and the results show a preference for the first octant of the θ_{23}, but values in the second octant are less than the 1σ away from the best fit point.

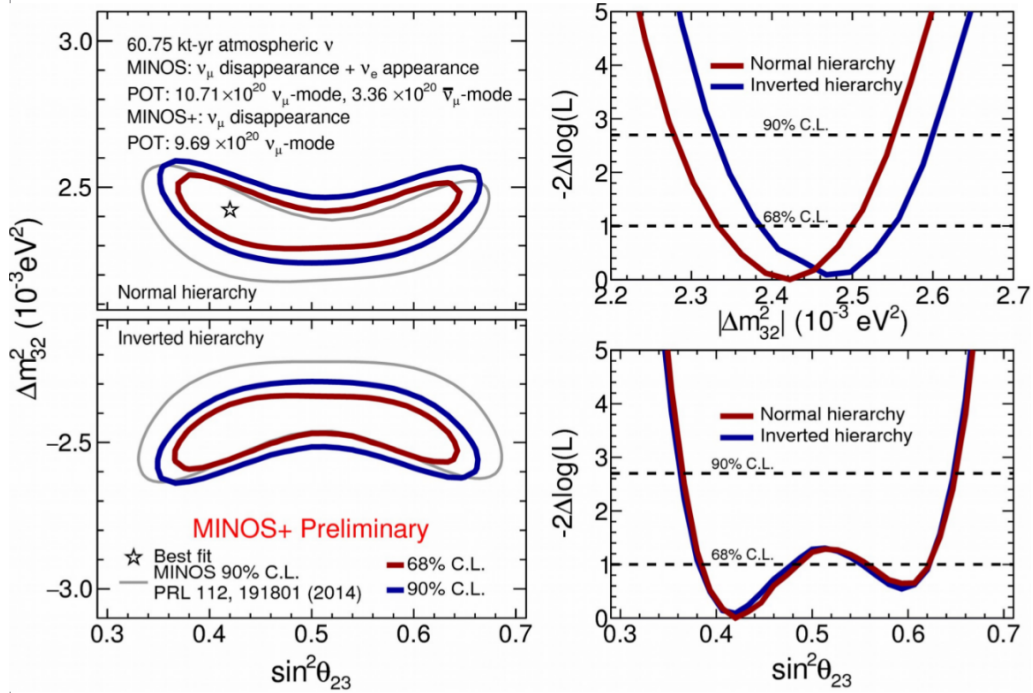Finally, results also show a very slight preference for the normal neutrino mass ordering.

Figure 19: MINOS and MINOS+ latest combined results for θ_{23} and Δm_{32}^2. Left plot shows the 2D contours and best fit point for the Δm_{32}^2 and the θ_{23} assuming both neutrino mass orderings. Right plots show the χ^2 curves for the Δm_{32}^2 (top) and θ_{23} (bottom).

	Mass Ordering	$\sin^2 \theta_{23}$	Δm_{32}^2 (10^{-3} eV^2)
Best Fit	NH (slight pref.)	0.42	2.42

Table 4: Best fit values of the MINOS and MINOS+ experiments oscillation analysis.

4 Results from Current LBL Neutrino Oscillation Experiments

Figure 20 summarizes the the results from all the reviewed experiments for the Δm_{32}^2 and θ_{23} oscillation parameters.

All the described experiments show a preference for the normal ordering of neutrino masses for which the data is becoming more compelling. As for the CP phase, T2K shows a preference for values close to $3\pi/2$ ($-\pi/2$), whereas the NOνA experiment prefer smaller values, both disfavouring CP-conserving values.

These results show the need for the T2K and NOνA joint analysis because it will provide a more clear picture of the remaining neutrino oscillation parameters.
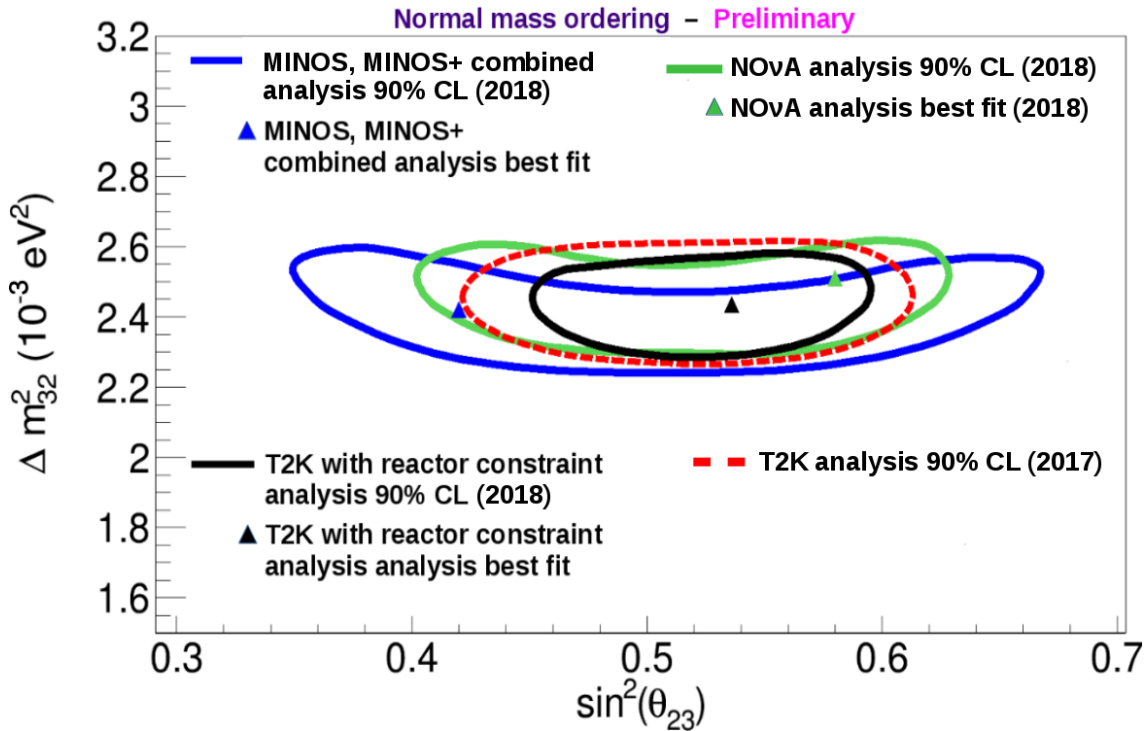
Figure 20: 90% confidence level 2D contours and best fit points for the Δm_{32}^2 and θ_{23} for the T2K (dashed red), the T2K with reactor constraints (black), the NOνA experiment and the MINOS and MINOS+ experiments.

5 Conclusions

The three main, currently operating, LBL neutrino experiments, T2K, NOνA and MI-NOS/MINOS+ have been reviewed and their most important results for the three neutrino oscillations shown.

In terms of neutrino oscillation results, all three experiments show a preference for normal neutrino mass ordering and NOνA and T2K data prefer the second octant of θ_{23} and disfavour CP-conserving values of δ_{CP}. MINOS and MINOS+ best fit is at the first octant of θ_{23}, although compatible with the second octant preference from the other experiments at $< 1\sigma$.

T2K will keep taking data until 2026 with improved neutrino beam and near and far detectors with the goal of $20 \cdot 10^{21}$ POT accumulated. In addition, a proposed joint fit of NOνA and T2K data will improve the sensitivity for the neutrino oscillation parameters, with special emphasis for the CP phase.

All these experiments are currently running and will continue to acquire data until the next generation experiments become operational, setting the basis to achieve precise measurements of all the neutrino oscillation parameters.

Acknowledgments

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