

SINDRUM II

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Abstract

In 1987 a collaboration including ETHZ - UZH - PSI - RWTH Aachen - Univ. Tbilisi proposed a new search for μe conversion in muonic atoms. The SINDRUM II spectrometer came into operation in the $\mu E1$ area in 1989, but a dedicated beam line was delayed until 1998 by technical setbacks.

8.1 Introduction

μe -Conversion in muonic atoms would result in the emission of an electron with energy

$$E_{\mu e} = m_{\mu}c^2 - B_{\mu} - R_N, \quad (8.1)$$

with B_{μ} and R_N being the muon binding energy and nuclear recoil energy, respectively. For gold $E_{\mu e} = 95.55$ MeV [10]. The energy of electrons would be at the endpoint of the allowed muon decay in orbit (MIO) where the energies of the two neutrinos vanish.

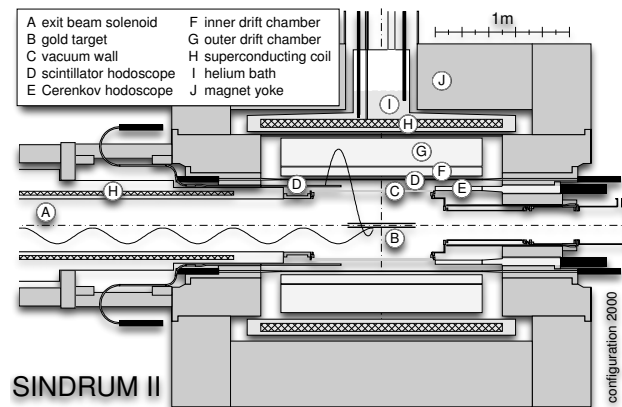


Figure 8.1: The SINDRUM II spectrometer as configured during measurements in 2000.

8.2 SINDRUM II

To distinguish conversion electrons from MIO background at the planned sensitivity level, the spectrometer was designed with an energy resolution around 1% FWHM. SINDRUM II used a superconducting solenoid [7], formerly operated at the CERN ISR (see Figure 8.1). Two

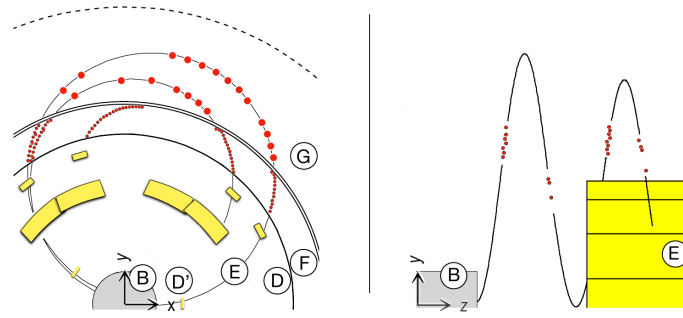


Figure 8.2: Traces of a 100 MeV/c e^- in xy and zy views. The particle shown made 2 1/2 turns before leaving the tracker. Labeling is as in Figure 8.1.

21 plastic scintillator hodoscopes (D) and a lucite Cerenkov hodoscope (E) are used for timing
 22 and triggering. The electron momentum is determined from the tracks recorded in the inner
 23 radial drift chamber (F), filled with CO₂/iC₄H₁₀ (70/30), a slow drift gas that results in a
 24 6° Lorentz deflection. The geometric acceptance for conversion electrons, when requiring the
 25 particle to completely cross drift chamber F before reaching an endcap detector, is 44% of 4π
 26 sr. The axial sense wires are located close to the outer cathode foil which is subdivided into
 27 4.4 mm wide strips oriented 72° relative to the wires. Correlated signals from wires and strips
 28 allow a 3d track reconstruction. The outer radial drift chamber (G) used a He/iC₄H₁₀ (88/12)
 29 gas mixture, that has a large radiation length to reduce multiple scattering. Figure 8.2 shows
 30 the online display of a multi-turn event recorded in 1989 with beam on. Note the energy loss
 31 along the spiralling path through the spectrometer. As can be seen in Figure 8.3, consecutive
 32 turns are always well separated so later tracks do not interfere with the first, main turn. The left
 33 side of the peak allows sensitive checks of the material budget and the momentum resolution.

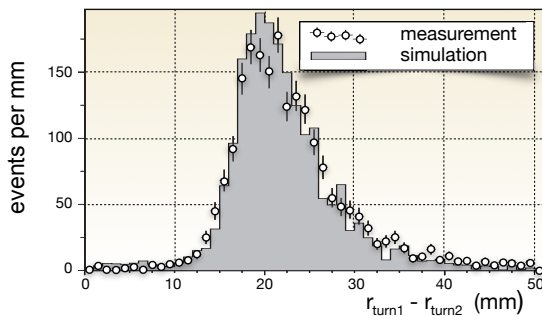


Figure 8.3: Change in radius of the first two turns of a multi-turn trajectory resulting from the energy loss in the plastic hodoscope in particular. Thanks to this loss, the turns don't overlap, which otherwise might have confused the trajectory reconstruction.

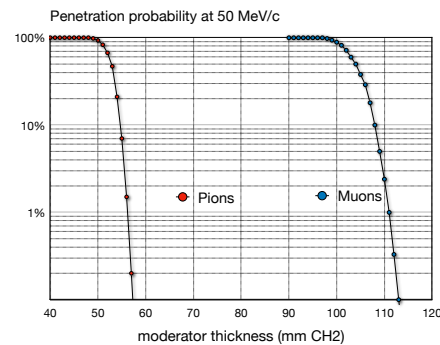


Figure 8.4: Simulated penetration probabilities of pions and muons in CH₂ at 50 MeV/c.

34 8.3 The beam line

35 Beam pions reaching the target produce background with a probability of 10^{-5} . Thus, no more
 36 than 10^4 pions may reach the target during the entire data-taking period. Muons penetrate

37 twice as deep into matter as pions of the same momentum (see Figure 8.4). This was utilized
 38 to eliminate beam pions: the fraction eliminated is limited by the high-momentum tail of the
 39 beam.

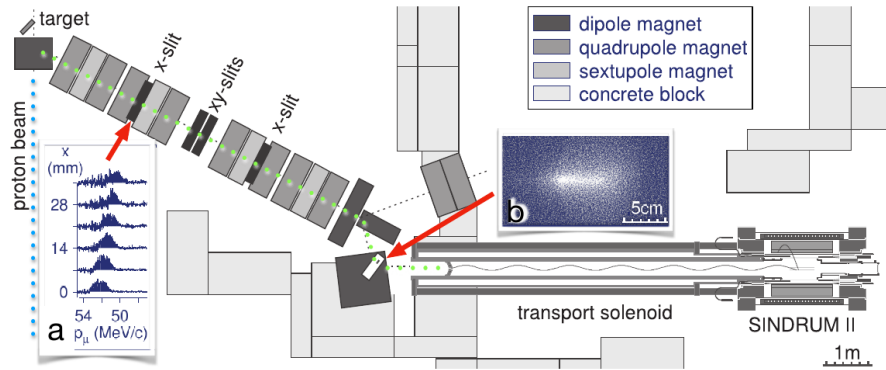


Figure 8.5: Plan view of the experiment. A quadrupole channel extracted a beam with a similar amount of π 's and μ 's in the backward direction from the production target. Inset **a** shows the impact of the momentum slit in the first dispersive focus. The momentum was determined by time of flight, based on the 50 MHz cyclotron rf signal. Inset **b** shows a CCD image of the beam spot. From here muons were guided to the target by a 9 m transport solenoid.

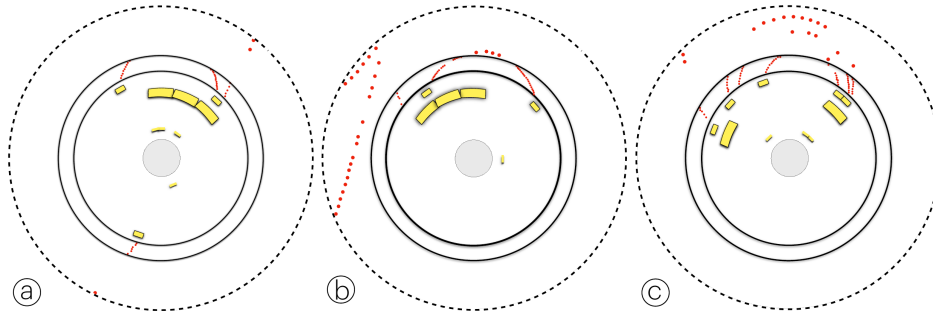


Figure 8.6: Three cosmic-ray events in the $r\phi$ projection. Signals recorded in the drift chambers (red), the plastic hodoscopes and Čerenkov counters (yellow) are indicated: a) a high momentum muon knocking an e^- out of a Čerenkov counter, b) a high momentum muon creating an e^+e^- pair in the magnet coil and c) an e^- (most likely from the decay of a distant cosmic muon) spiraling in from outside.

40 The pion contamination was reduced in three steps (see Figure 8.5). First a momentum-
 41 selected beam was focused on a wedge-shaped degrader inside a final bending magnet. The
 42 few pions that penetrate do so with a wide momentum spread and have little chance to reach
 43 a second degrader in a collimator at the entrance of the transport solenoid. The beam was
 44 studied in great detail with dedicated diagnostic tools to tune the settings of the magnets and
 45 the slits. In this process the high-momentum tail of the beam was reduced by two orders
 46 of magnitude. Muons crossed the degraders but only very few pions emerged to enter the

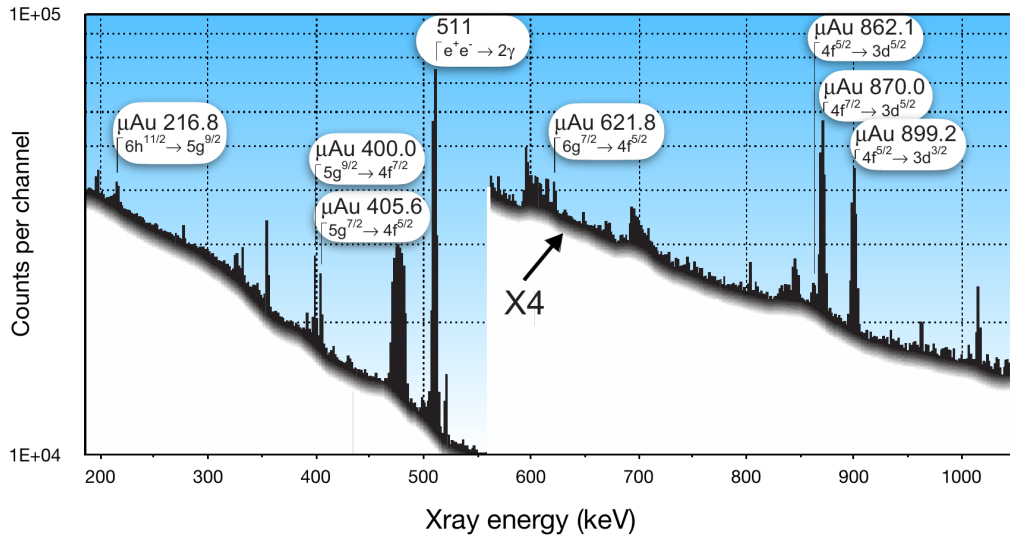


Figure 8.7: X-ray spectrum recorded with a Ge(Li) detector during data taking to monitor the number of muons stopping in the gold target.

47 solenoid. These pions are slow and 99.99% decayed before reaching the target.

48 8.4 Background

49 Data was acquired even with the beam off as there are no beam counters in the final configu-
 50 ration. When requiring a circular track crossing drift chamber F, the trigger rate without beam
 51 was typically one per second. Figure 8.6 shows three examples.

52 Cosmic-ray background was collected for more than a year with beam off: it can be recog-
 53 nized by the presence of additional signals in various detectors or by requiring the trajectory
 54 to originate in the target. What remains is associated with photons in cosmic-ray showers that
 55 enter through the cryogenic supply tower (see Figure 8.1). This background component was
 56 removed by an angular cut at the cost of a 5% loss in acceptance.

57 Another source of electrons with momenta around 100 MeV/c were beam pions, mostly
 58 through intermediate photons producing asymmetric e^+e^- pairs in the target. Electrons from
 59 radiative pion capture in the moderator may easily reach the target and scatter into the detector
 60 solid angle. This background can be recognized as it is strongly peaked in the forward direction
 61 and it has a characteristic time correlation with the cyclotron rf signal.

62 8.5 The 2000 data set

63 In the final 81-day period of data-taking in 2000 with a gold target,

$$N_{\mu stop} = (4.30 \pm 0.3_{stat} \pm 0.3_{sys}) \times 10^{13} \quad (8.2)$$

64 muons stopped in the target, as deduced from the muonic X-rays escaping the setup (see
 65 Figure 8.7). The monitor was calibrated with radioactive sources.

66 The analysis is based on the momentum spectrum of electrons originating in the target.
 67 A cut is made on the position coordinates at the point of closest approach of the track to the
 68 central axis and is illustrated in Figure 8.8 for events surviving the cosmic-ray background
 69 checks.

70 The vast majority of the remaining events are from muon decay in orbit (MIO). Following
 71 Shanker [9], the MIO spectrum used as input for the GEANT simulation has been approximated

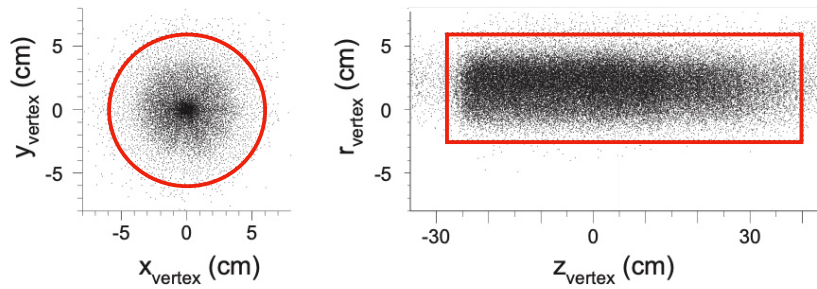


Figure 8.8: Reconstructed point of closest approach to the z axis in the xy and zy projections. The contours indicate the selected target region.

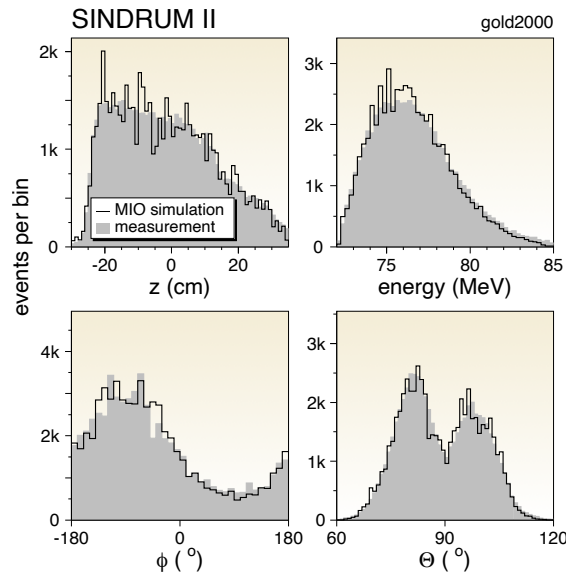


Figure 8.9: Comparison of measurement and MIO simulation for four kinematic quantities.

72 by

$$N(E)dE \propto \left(\frac{E}{m_\mu c^2}\right)^2 \left(\frac{E_{\mu e} - E}{m_\mu c^2}\right)^5 dE + h.c. \quad (8.3)$$

73 The rate is proportional to E^2 at the low energy end, as is known from the Michel spectrum. At
 74 the high energy end, the rate falls proportional to the missing (neutrinos) energy to the fifth
 75 power.

76 As shown in Figure 8.9 there is fair agreement between measurement and simulation. The
 77 following comments may be helpful to explain some features:

- 78 • Muons come from $z < 0$ and follow helical trajectories. Thus the stopping distribution
 79 falls from upstream to downstream.
- 80 • The fall of the rate at the low side of the energy distribution reflects the requirement
 81 that the electron crosses the inner drift chamber. This results in a transverse momentum
 82 threshold of around 70 MeV/c.
- 83 • There is a large ϕ anisotropy that is, however, antisymmetric about 0° , as expected for
 84 the up-down symmetry of the beam line (horizontal bending plane).
- 85 • The dip at $\theta = 90^\circ$ results from e^- 's that need too many turns to reach an endcap.

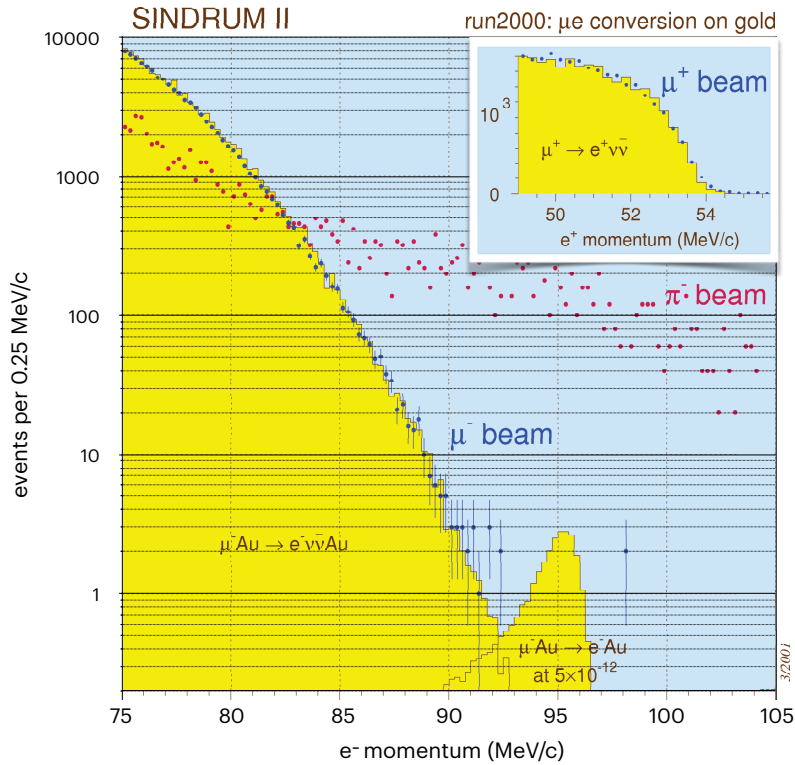


Figure 8.10: Momentum distributions for three different beam momenta and polarities: (i) 53 MeV/c negative muons, optimized for μ^- stops, (ii) 63 MeV/c negative pions, optimized for π^- stops, and (iii) 48 MeV/c positive muons, optimized for μ^+ stops. The 63 MeV/c data were normalized to the same measuring time. The measurement with the stopped μ^- beam is compared with GEANT simulations of decay in orbit and $\mu - e$ conversion.

86 The θ and ϕ distortions are threshold effects that disappear towards $E_{\mu e}$. The upper end of the
 87 electron momentum distribution, measured with a 53 MeV/c stopped μ^- beam, is compared
 88 with distributions from simulations of bound muon decay and coherent $\mu - e$ conversion in
 89 Figure 8.10. The rate falls steeply towards $E_{\mu e}$ in agreement with the simulation, both in
 90 shape and in the number of events. Also shown are the results with 63 MeV/c stopped π^-
 91 showing the enormous background reaching up to the pion mass, and the familiar Michel
 92 spectrum taken with 48 MeV/c μ^+ beam. The μ^+ data were taken at reduced spectrometer
 93 field for increased acceptance at the lower momenta and give an independent check of the
 94 momentum calibration and resolution.

95 No candidate events are found and the measurement results in an improvement of our
 96 own upper limit by one and a half orders of magnitude. This result is included in Table 8.1
 97 with all upper limits on $\mu^- e^-$ and $\mu^- e^+$ conversion obtained by SINDRUM II.

98 8.6 Conclusions and outlook

99 After a decade long campaign, SINDRUM II took its final data in 2000. The resulting upper
 100 limits on $\mu - e$ conversion were pushed below 10^{-12} . The effort took longer and brought us
 101 not quite as far as was promised in the proposal but now, almost twenty years later, the SIN-
 102 DRUM limits still stand. The new more ambitious experiments are simply getting bigger, more
 103 complex, more expensive, require more manpower and often rely on new detector concepts

beam line	year meas.	process	beam MeV/c	days	stops	upper limit 90 % C.L.	Ref.
	1989	$\mu^- \text{Ti} \rightarrow e^- \text{Ti}$	100	25	$4.28(32) \times 10^{12}$	4.2×10^{-12}	[4]
$\mu E1$	1992	$\mu^- \text{Pb} \rightarrow e^- \text{Pb}$	86	10	$1.72(34) \times 10^{12}$	4.6×10^{-11}	[5]
	1993	$\mu^- \text{Ti} \rightarrow e^+ \text{Ca}$	86	60	$2.76(21) \times 10^{13}$	7.3×10^{-13}	[6]
$\pi E5$	1997	$\mu^- \text{Au} \rightarrow e^- \text{Au}$	20	24	7.6×10^{11}	1.91×10^{-11}	[8]
	2000	$\mu^- \text{Au} \rightarrow e^- \text{Au}$	53	81	$4.37(32) \times 10^{13}$	7×10^{-13}	[3]

Table 8.1: SINDRUM II results over the years.

104 and thus time consuming R&D.

105 There are two new efforts planning to continue where SINDRUM II ended: COMET (J-
106 PARC, Japan) [1] and MU2E (Fermilab, U.S.A) [2]. Both use a staged approach, so with a bit
107 of luck, new territory may be reached before the end of the decade.

108 The "search for nothing" keeps moving on!

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