

SINDRUM II

A. van der Schaaf^{1*}¹ Physik-Institut der Universität Zürich, CH-8057 Zürich, Switzerland

* andries@physik.uzh.ch

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Abstract

In 1987 a collaboration including ETHZ - UZH - PSI - RWTH Aachen - Univ. Tbilisi proposed a new search for μe conversion in muonic atoms. The SINDRUM II spectrometer came into operation in the $\mu E1$ area in 1989, but a dedicated beam line was delayed until 1998 by technical setbacks.

8.1 Introduction

μe -Conversion in muonic atoms would result in the emission of an electron with energy

$$E_{\mu e} = m_{\mu}c^2 - B_{\mu} - R_N, \quad (8.1)$$

with B_{μ} and R_N being the muon binding energy and nuclear recoil energy, respectively. $E_{\mu e}$ is the endpoint energy of muon decay in orbit (MIO) where the energies of the two outgoing neutrinos vanish. For gold $E_{\mu e} = 95.55$ MeV [1]. Around the time of the SINDRUM II proposal, the best limit obtained for a heavy target was $B(\mu^- \text{Pb} \rightarrow e^- \text{Pb}) < 4.9 \times 10^{-8}$ (90% C.L.) [2].

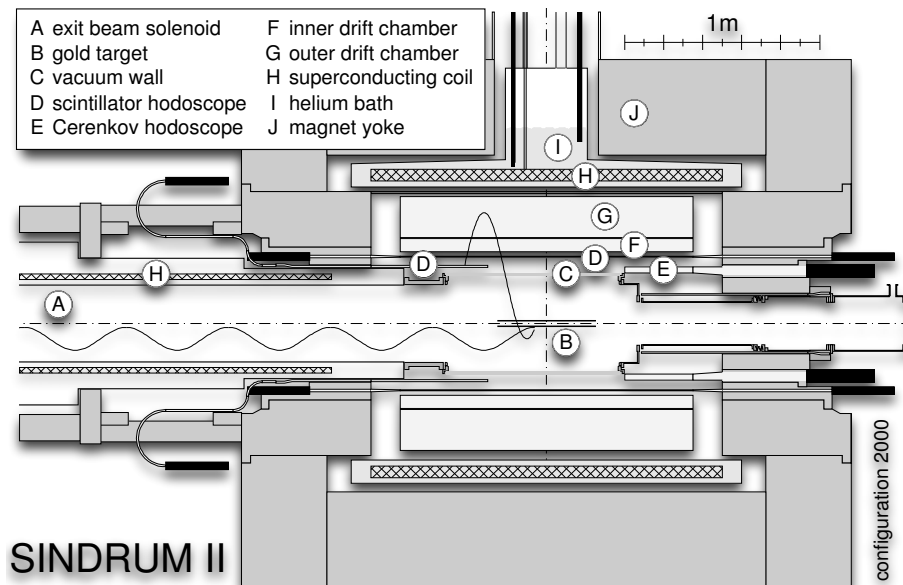


Figure 8.1: The SINDRUM II spectrometer as configured in the year 2000.

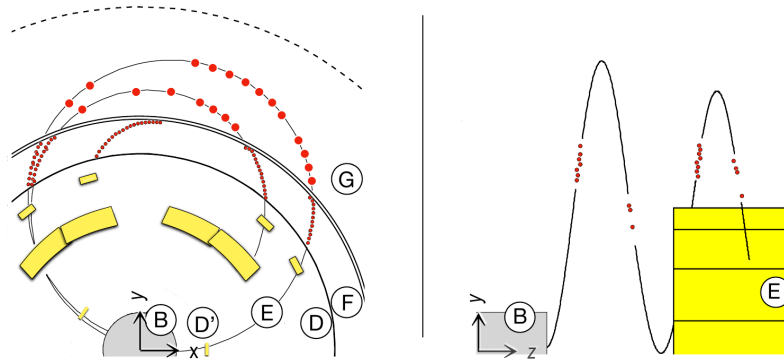


Figure 8.2: Traces of a 100 MeV/c e^- in xy and zy views. The particle shown made 2 1/2 turns before leaving the tracker. Labeling is as in Figure 8.1.

18 8.2 SINDRUM II

19 To distinguish conversion electrons from MIO background at the planned sensitivity level, the
 20 spectrometer was designed with an energy resolution around 1% FWHM. SINDRUM II used
 21 a superconducting solenoid [3], formerly operated at the CERN ISR (see Figure 8.1). Two
 22 plastic scintillator hodoscopes (D) and a lucite Cerenkov hodoscope (E) are used for timing
 23 and triggering. The electron momentum is determined from the tracks recorded in the inner
 24 radial drift chamber (F), filled with CO₂/iC₄H₁₀ (70/30), a slow drift gas that results in a
 25 6° Lorentz deflection. The geometric acceptance for conversion electrons, when requiring the
 26 particle to completely cross drift chamber F before reaching an endcap detector, is 44% of 4π
 27 sr. The axial sense wires are located close to the outer cathode foil which is subdivided into
 28 4.4 mm wide strips oriented 72° relative to the wires. Correlated signals from wires and strips
 29 allow a 3d track reconstruction. The outer radial drift chamber (G) used a He/iC₄H₁₀ (88/12)
 30 gas mixture, that has a large radiation length to reduce multiple scattering. Figure 8.2 shows
 31 the online display of a multi-turn event recorded in 1989 with beam on. Note the energy loss
 32 along the spiralling path through the spectrometer. As can be seen in Figure 8.3, consecutive
 33 turns are always well separated so later tracks do not interfere with the first, main turn. The left
 34 side of the peak allows sensitive checks of the material budget and the momentum resolution.

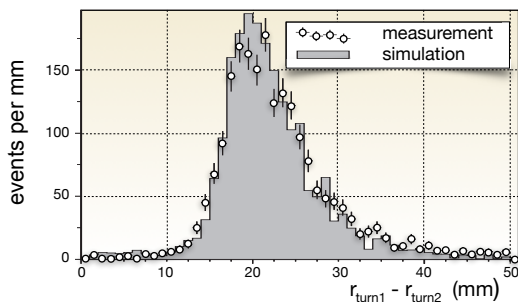


Figure 8.3: Change in radius of the first two turns of a multi-turn path caused by energy loss in the plastic hodoscope in particular. Thanks to this loss, the turns don't overlap, which otherwise might have confused the reconstruction.

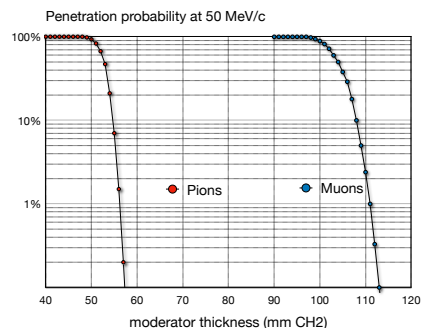


Figure 8.4: Simulated penetration probabilities of pions and muons in CH₂ at 50 MeV/c.

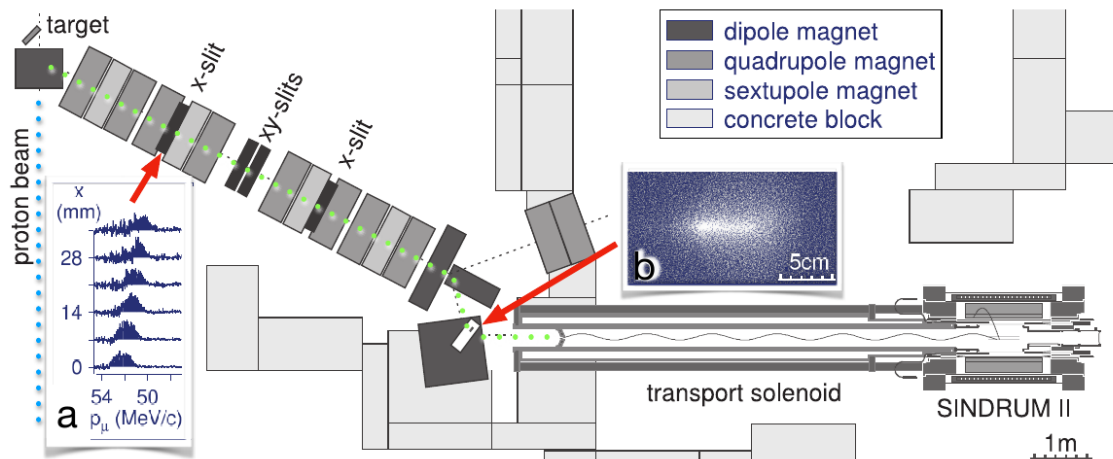


Figure 8.5: Plan view of the experiment at the $\pi E5$ secondary beam line during the final measuring period in the year 2000. A quadrupole channel extracted a beam with a similar amount of π 's and μ 's in the backward direction from the production target. Inset **a** shows the impact of the momentum slit in the first dispersive focus. The momentum was determined by time of flight, based on the 50 MHz cyclotron rf signal. Inset **b** shows a CCD image of the beam spot. From here muons were guided to the target by a 9 m long transport solenoid.

35

36 8.3 The beam line

37 A beam pion stopping in the target produces isotropic background through radiative pion
 38 capture, followed by asymmetric internal and external e^+e^- pair production, with a probability
 39 around 10^{-5} (see Section 8.5). Thus, no more than 10^4 pions may reach the target during
 40 the entire data-taking period. Muons penetrate twice as deep into matter as pions of the
 41 same momentum (see Figure 8.4). This was utilized to eliminate beam pions: the fraction
 42 eliminated is limited by the high-momentum tail of the beam. The pion contamination was
 43 reduced in three steps (see Figure 8.5). First a momentum-selected beam was focused on a
 44 wedge-shaped degrader inside a final bending magnet. The few pions that penetrate do so with
 45 a wide momentum spread and have little chance to reach a second degrader in a collimator at
 46 the entrance of the transport solenoid. The beam was studied in great detail with dedicated
 47 diagnostic tools to tune the settings of the magnets and the slits. In this process the high-
 48 momentum tail of the beam was reduced by two orders of magnitude. Muons crossed the
 49 degraders but only very few pions emerged to enter the solenoid. These pions are slow and
 50 99.99% decayed before reaching the target.

51 Data was acquired even with the beam off as there are no beam counters in the final
 52 configuration. When requiring a circular track crossing drift chamber F, the trigger rate without
 53 beam was typically one per second. Figure 8.6 shows three examples.

54 8.4 Background

55 Cosmic-ray background was collected for more than a year with beam off: it can be recognized
 56 by the presence of additional signals in various detectors or by requiring the trajectory to
 57 originate in the target. What remains is associated with photons in cosmic-ray showers that
 58 enter through the cryogenic supply tower (see Figure 8.1). This background component was
 59 removed by an angular cut at the cost of a 5% loss in acceptance.

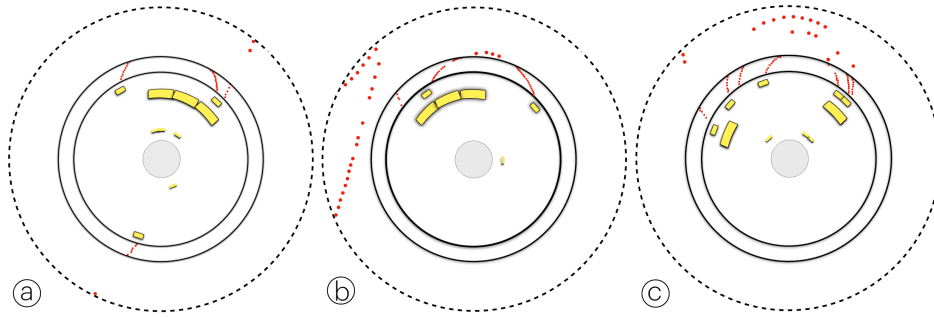


Figure 8.6: Three cosmic-ray events in the $r\phi$ projection. Signals recorded in the drift chambers (red), the plastic hodoscopes and Čerenkov counters (yellow) are indicated: a) a high momentum muon knocking an e^- out of a Čerenkov counter, b) a high momentum muon creating an e^+e^- pair in the magnet coil and c) an e^- (most likely from the decay of a distant cosmic muon) spiraling in from outside.

60 Another potential source of electrons with momenta around 100 MeV/c is radiative pion
 61 capture, mostly through intermediate photons producing asymmetric e^+e^- pairs, in the target.
 62 Pion capture is much more likely in the moderator inside the collimator at the entrance of
 63 the transport solenoid (see Figure 8.5) and the resulting electrons and positrons may easily
 64 reach the target where they may scatter into the detector solid angle. This background can
 65 be recognized as it is strongly peaked in the forward direction and it has a characteristic time
 66 correlation with the cyclotron rf signal.

67 8.5 The 2000 data set

68 In the final 81-day period of data-taking in 2000 with a gold target,

$$N_{\mu stop} = (4.30 \pm 0.3_{stat} \pm 0.3_{sys}) \times 10^{13} \quad (8.2)$$

69 muons stopped in the target, as deduced from the muonic X-rays escaping the setup (see
 70 Figure 8.7). The monitor was calibrated with radioactive sources.

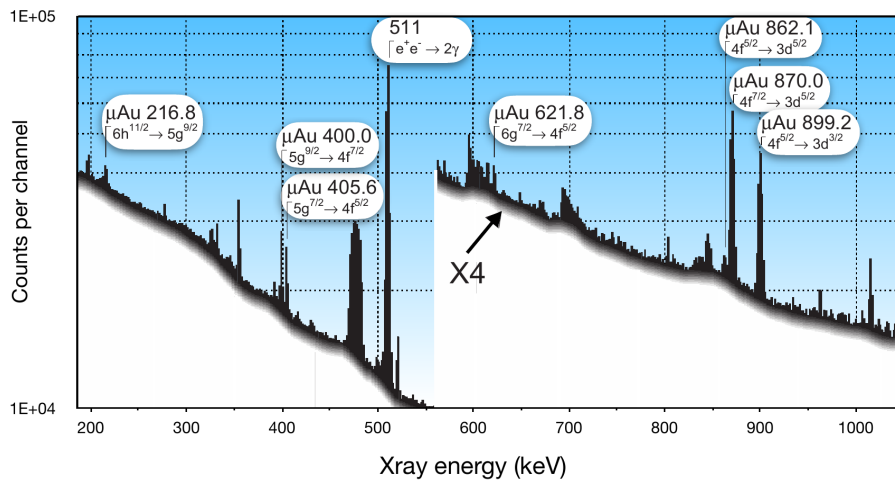


Figure 8.7: X-ray spectrum recorded with a Ge(Li) detector during data taking to monitor the number of muons stopping in the gold target.

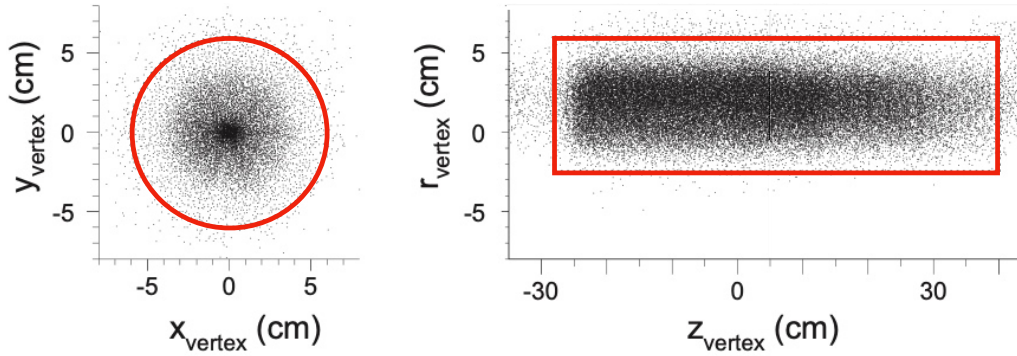


Figure 8.8: Reconstructed point of closest approach to the z axis in the xy and zy projections. The contours indicate the selected target region.

71 The analysis is based primarily on the momentum spectrum of electrons originating in the
 72 target. A cut is made on the position coordinates at the point of closest approach of the track to
 73 the central axis and is illustrated in Figure 8.8 for events surviving the cosmic-ray background
 74 checks.

75 The vast majority of the selected events are muon decays in orbit (MIO). Following Shanker,
 76 the MIO spectrum used as input for the GEANT simulation has been approximated by [4]

$$N(E)dE \propto \left(\frac{E}{m_\mu c^2}\right)^2 \left(\frac{E_{\mu e} - E}{m_\mu c^2}\right)^5 dE + h.c. \quad (8.3)$$

77 The rate is proportional to E^2 at the low energy end, as is known from the Michel spectrum.
 78 At the high energy end, the rate falls proportional to the missing (neutrinos) energy to the
 79 fifth power. As shown in Figure 8.9 there is fair agreement between measurement and MIO
 80 simulation.

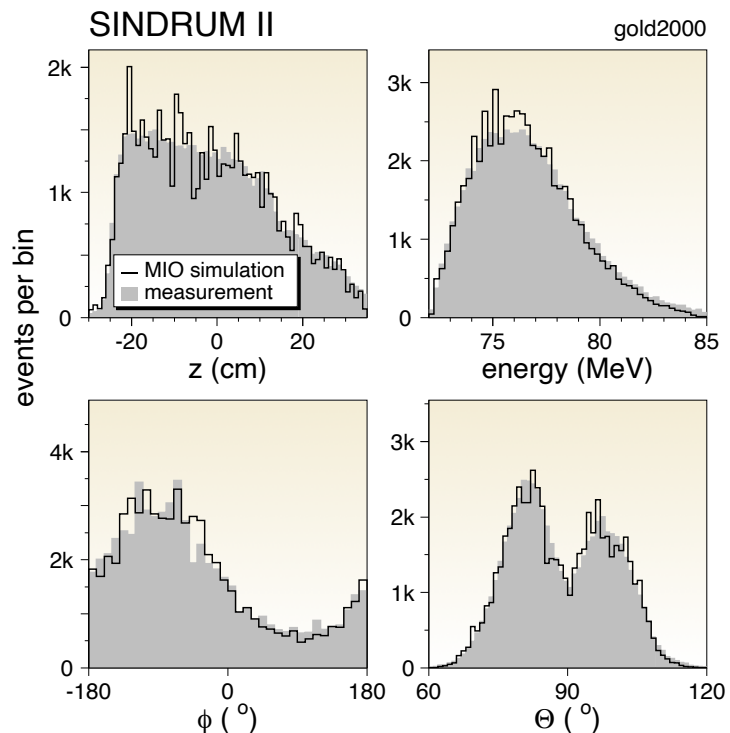


Figure 8.9:
 Comparison of measurement
 and MIO simulation for four
 kinematic quantities.

81 The following comments may be helpful to explain some features:

- 82 • Muons come from $z < 0$ and follow helical trajectories. Thus the stopping distribution
83 falls from upstream to downstream.
- 84 • The fall of the rate at the low side of the energy distribution reflects the requirement
85 that the electron crosses the inner drift chamber. This results in a transverse momentum
86 threshold of around 70 MeV/c.
- 87 • There is a large ϕ anisotropy that is, however, antisymmetric about 0° , as expected for
88 the up-down symmetry of the beam line (horizontal bending plane).
- 89 • The dip at $\theta = 90^\circ$ results from e^- 's that need too many turns to reach an endcap.

90 The θ and ϕ distortions are threshold effects that disappear towards $E_{\mu e}$.

91 The upper end of the electron momentum distribution, measured with a 53 MeV/c stopped
92 μ^- beam, is compared with distributions from simulations of bound muon decay and coherent
93 μe conversion in Figure 8.10. The rate falls steeply towards $E_{\mu e}$ in agreement with the simu-
94 lation, both in shape and in the number of events. Also shown are the results with 63 MeV/c
95 stopped π^- showing the enormous background reaching up to the pion mass, and the familiar
96 Michel spectrum taken with 48 MeV/c μ^+ beam. The μ^+ data were taken at reduced spec-
97 trometer field for increased acceptance at the lower momenta and give an independent check
of the momentum calibration and resolution.

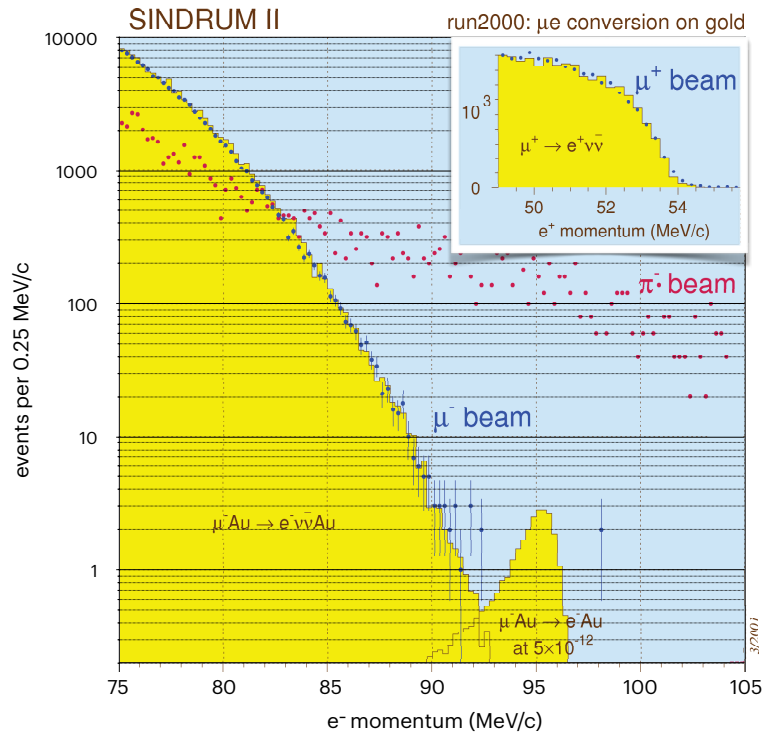


Figure 8.10: Momentum distributions for three different beam momenta and polarities: (i) 53 MeV/c negative muons, optimized for μ^- stops, (ii) 63 MeV/c negative pions, optimized for π^- stops, and (iii) 48 MeV/c positive muons, optimized for μ^+ stops. The 63 MeV/c data were normalized to the same measuring time. The measurement with the stopped μ^- beam is compared with GEANT simulations of decay in orbit and μe conversion.

98

99 No convincing signal events are observed in the main e^- momentum spectrum shown in
100 Figure 8.10 and a maximum likelihood analysis of that spectrum results in a lowering of our

101 own 90% C.L. upper limit by one and a half orders of magnitude. This result is included in
 102 Table 8.1 with all upper limits on μ^-e^- and μ^-e^+ conversion obtained by SINDRUM II.

| beam line | year meas. | process | beam MeV/c | days | stops | upper limit 90 % C.L. | Ref. |
|--------------|---------------|-----------------------------|---------------|------|---------------------------|--------------------------|------|
| | 1989 | $\mu^-Ti \rightarrow e^-Ti$ | 100 | 25 | $4.28(32) \times 10^{12}$ | 4.2×10^{-12} | [5] |
| $\mu E1$ | 1992 | $\mu^-Pb \rightarrow e^-Pb$ | 86 | 10 | $1.72(34) \times 10^{12}$ | 4.6×10^{-11} | [6] |
| | 1993 | $\mu^-Ti \rightarrow e^+Ca$ | 86 | 60 | $2.76(21) \times 10^{13}$ | 7.3×10^{-13} | [7] |
| $\pi E5$ | 1997 | $\mu^-Au \rightarrow e^-Au$ | 20 | 24 | 7.6×10^{11} | 1.91×10^{-11} | [8] |
| | 2000 | $\mu^-Au \rightarrow e^-Au$ | 53 | 81 | $4.37(32) \times 10^{13}$ | 7×10^{-13} | [9] |

Table 8.1: SINDRUM II results over the years.

102

103 8.6 Conclusions and outlook

104 After a decade long campaign, SINDRUM II took its final data in 2000. The resulting upper
 105 limits on μe conversion were pushed below 10^{-12} . The effort took longer and brought us not
 106 quite as far as was promised in the proposal but now, almost twenty years later, the SINDRUM
 107 limits still stand. The new more ambitious experiments are simply getting bigger, more com-
 108 plex, more expensive, require more manpower and often rely on new detector concepts and
 109 thus time consuming R&D.

110 There are two new efforts planning to continue where SINDRUM II ended: COMET (J-
 111 PARC, Japan) [10] and MU2E (Fermilab, U.S.A) [11]. Both use a pulsed beam and a delayed
 112 time window to fight prompt (pion) background which excludes heavy targets such as gold,
 113 with their correspondingly short decay times. Both use a staged approach, so with a bit of
 114 luck, new territory may be reached before the end of the decade.

115 The "search for nothing" keeps moving on!

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