

Dark matter, fine-tuning and $(g - 2)_\mu$ in the pMSSM

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April 29, 2021

1 Abstract

2 In this paper we analyze spectra in the phenomenological supersymmetric Stan-
3 dard Model that simultaneously result in the right dark-matter relic density
4 $\Omega_{\text{DM}} h^2$, offer an explanation for the $(g - 2)_\mu$ discrepancy Δa_μ and are minimally
5 fine-tuned. We discuss the LHC phenomenology resulting from these spec-
6 tra and the sensitivity of dark-matter direct detection experiments to these
7 spectra. We find that the latter type of experiments with sensitivity to the
8 spin-dependent dark-matter – nucleon scattering cross section $\sigma_{\text{SD},p}$ will probe
9 all of our found solutions.

10

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26 1 Introduction

27 The Large Hadron Collider (LHC) has been searching for over a decade for signs of physics
 28 that originate from beyond-the-Standard-Model (BSM) scenarios, including searches for
 29 signals that originate from supersymmetric (SUSY) particle production. These high-energy
 30 searches are complemented by low-energy experiments such as dark-matter (DM) exper-
 31 iments, or experiments that search for small deviations in known Standard-Model (SM)
 32 processes from their SM prediction. In the former category, the XENON1T [1, 2], PandaX-
 33 II [3, 4] and PICO [5–7] experiments provide limits on the DM-nucleus scattering cross
 34 section, whereas the Planck collaboration provides a precise measurement of the DM relic
 35 abundance [8]. In the latter category, the anomalous magnetic moment of the muon ($g-2$) _{μ}
 36 plays an important role. There is a long-standing discrepancy between the experimental
 37 result [9–11] and the SM prediction for the muon anomalous magnetic moment. The
 38 latter is composed of quantum-electrodynamic, weak, hadronic vacuum-polarization, and
 39 hadronic light-by-light contributions, and reads [12–33]

$$40 \quad a_{\mu}^{\text{SM}} = \frac{(g-2)_{\mu}}{2} = 116\,591\,810(43) \times 10^{-11}, \quad (1)$$

41 where the value between parentheses represents the theoretical uncertainty. The improved
 42 experimental results obtained at Fermilab [34–37], combined with the Brookhaven result [9–
 11] read

$$43 \quad a_{\mu}^{\text{exp}} = 116\,592\,061(41) \times 10^{-11}, \quad (2)$$

44 showing that the deviation is now

$$45 \quad \Delta a_{\mu} = a_{\mu}^{\text{exp}} - a_{\mu}^{\text{SM}} = 251(59) \times 10^{-11}. \quad (3)$$

46 An independent experiment with different techniques than those employed by the Fermilab
 47 experiment is being constructed at J-PARC [38, 39].
 48 The Minimal Supersymmetric Standard Model (MSSM) with R -parity conservation pre-
 49 dicts a DM candidate and can simultaneously provide an explanation for the ($g-2$) _{μ}
 50 discrepancy¹. Furthermore, the MSSM provides a solution to the fine-tuning (FT) prob-
 51 lem in the Higgs sector that any BSM model introduces, even after taking into account
 52 the constraints on colored sparticles originating from the LHC. It is clear that for a rich
 53 model such as the MSSM, the interplay between the various experimental results is of
 54 crucial importance. In this context, the interplay between the LHC limits and the ($g-2$) _{μ}
 55 discrepancy has been studied in e.g. Ref. [41–48]. DM direct detection (DMDD) searches
 56 are complementary in regions of the MSSM parameter space where the LHC has little
 57 sensitivity, for example in compressed regions. Papers that explore the DM implications of
 58 spectra that explain the ($g-2$) _{μ} discrepancy include Refs. [47–52], where the relic density
 59 requirement is not always taken into account. Likelihood analyses or global fits, where all
 60 experimental data that constrain the MSSM parameter space are taken into account, have
 61 been performed in e.g. Ref. [52–58]. The degree of FT in constrained models that explain
 62 the ($g-2$) _{μ} discrepancy is studied in [59, 60], whereas the role of FT in spectra with the
 63 right DM properties is studied in Ref. [61–65].
 64 In this work we perform for the first time a study of the phenomenology of the MSSM
 65 that simultaneously accounts for the DM relic abundance and the observed discrepancy

¹A simultaneous explanation of the muon and electron anomalous magnetic moments in the MSSM context is provided in Ref. [40].

of $(g - 2)_\mu$, that includes all DMDD and LHC limits, and that constrains the model-parameter space to models that are minimally fine-tuned. The paper is structured as follows. In Section 2 we introduce our notation, the muon anomalous magnetic moment, and the electroweak fine-tuning measure. In Section 3 we explain the set-up of our analysis. In Section 4 we explore the phenomenology of the viable spectra, and in Section 5 we present our conclusions.

2 The muon anomalous magnetic moment and fine-tuning in the pMSSM

Instead of exploring the full MSSM with 105 free parameters, we focus on the phenomenological MSSM (pMSSM) [66], which has 19 free parameters. In this phenomenologically motivated pMSSM one requires that the first and second generation squark and slepton masses are degenerate, that the trilinear couplings of the first and second generation sfermions are set to zero (leaving only those of the third generation, A_t , A_b and A_τ), and that no new sources of CP violation are introduced. In addition one assumes that all sfermion mass matrices are diagonal. The sfermion soft-masses are then described by the first and second generation squark masses $m_{\tilde{Q}_1}$, $m_{\tilde{u}_R}$ and $m_{\tilde{d}_R}$, the third generation squark masses $m_{\tilde{Q}_3}$, $m_{\tilde{t}_R}$ and $m_{\tilde{b}_R}$, the first and second generation of slepton masses $m_{\tilde{L}_1}$ and $m_{\tilde{e}_R}$, and the third generation of slepton masses $m_{\tilde{L}_3}$ and $m_{\tilde{\tau}_R}$. The Higgs sector is described by the ratio of the Higgs vacuum expectation values $\tan \beta$ and the soft Higgs masses m_{H_u} and m_{H_d} . Instead of these parameters, it is customary to use the higgsino mass parameter μ and the mass m_A of the pseudoscalar Higgs boson as free parameters. The gaugino sector consists of the bino (\tilde{B}), wino (\tilde{W}) and gluino with their mass parameters $M_1 (= |M_1|)$, $M_2 (= |M_2|)$ and $M_3 (= |M_3|)$.

As a result of electroweak symmetry breaking (EWSB), the gaugino and the higgsino interaction eigenstates mix into mass eigenstates, called neutralinos and charginos. The neutralinos, denoted by $\tilde{\chi}_i^0$ with $i = 1, \dots, 4$, are the neutral mass eigenstates of the bino, wino and higgsino interaction eigenstates. The neutralinos are ordered by increasing mass, with $\tilde{\chi}_1^0$ the lightest neutralino. Given the constraints from DMDD experiments on sneutrino DM, we take the lightest neutralino as lightest-supersymmetric particle (LSP), which makes it our DM candidate. Depending on the exact values of M_1 , M_2 and $|\mu|$, this lightest mass eigenstate can be mostly bino-like (if M_1 is smallest), wino-like (if M_2 is smallest) or higgsino-like (if $|\mu|$ is smallest). The amount of bino, wino and higgsino mixing of the lightest neutralino is given by N_{11} , N_{12} and $\sqrt{N_{13}^2 + N_{14}^2}$, where N_{ij} are the entries of the matrix that diagonalizes the neutralino mass matrix. In the basis of $(\tilde{B}, \tilde{W}^0, \tilde{H}_d^0, \tilde{H}_u^0)$, this mass matrix is given by

$$M_{\tilde{\chi}^0} = \begin{pmatrix} M_1 & 0 & -c_\beta s_{\theta_W} M_Z & s_\beta s_{\theta_W} M_Z \\ 0 & M_2 & c_\beta c_{\theta_W} M_Z & -s_\beta c_{\theta_W} M_Z \\ -c_\beta s_{\theta_W} M_Z & c_\beta c_{\theta_W} M_Z & 0 & -\mu \\ s_\beta s_{\theta_W} M_Z & -s_\beta c_{\theta_W} M_Z & -\mu & 0 \end{pmatrix}, \quad (4)$$

with $s_x \equiv \sin x$, $c_x \equiv \cos x$, and the ratio of the SM W - and Z -boson masses being denoted by $\cos \theta_W = M_W/M_Z$.

The charginos, denoted by $\tilde{\chi}_i^\pm$ with $i = 1, 2$, are the charged mass eigenstates of the wino and higgsino interaction eigenstates, with $\tilde{\chi}_1^\pm$ the lightest chargino. In the basis of

¹⁰³ $(\widetilde{W}^\pm, \widetilde{H}_{u/d}^\pm)$, their mass matrix at tree level reads

$$M_{\tilde{\chi}^\pm} = \begin{pmatrix} M_2 & \sqrt{2}c_\beta c_{\theta_W} M_Z \\ \sqrt{2}s_\beta c_{\theta_W} M_Z & \mu \end{pmatrix}. \quad (5)$$

¹⁰⁴ The composition of the lightest chargino is predominantly higgsino when $|\mu| < M_2$, pre-
¹⁰⁵ dominantly wino when $M_2 < |\mu|$, or a mixture when the two gaugino parameters are close
¹⁰⁶ in value.

¹⁰⁷ 2.1 Electroweak fine-tuning in the pMSSM

¹⁰⁸ The EWSB conditions link M_Z to the input parameters via the minimization of the scalar
¹⁰⁹ potential of the Higgs fields. The resulting equation at one loop is [67, 68]

$$\frac{M_Z^2}{2} = \frac{m_{H_d}^2 + \Sigma_d^d - (m_{H_u}^2 + \Sigma_u^u) \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2, \quad (6)$$

¹¹⁰ where the two effective potential terms Σ_u^u and Σ_d^d denote the one-loop corrections to
¹¹¹ the soft SUSY breaking Higgs masses (explicit expressions are shown in the appendix of
¹¹² Ref. [68]). In order to obtain the observed value of $M_Z = 91.2$ GeV, one needs some degree
¹¹³ of cancellation between the SUSY parameters appearing in Eq. (6). If small relative changes
¹¹⁴ in the SUSY parameters will result in a distinctly different value of M_Z , the considered
¹¹⁵ spectrum is said to be fine-tuned, as then a large degree of cancellation is needed to obtain
¹¹⁶ the right value of M_Z . FT measures aim to quantify this sensitivity of M_Z to the SUSY
¹¹⁷ input parameters.

¹¹⁸ The electroweak (EW) FT measure [69, 70] is an agnostic approach to the computation of
¹¹⁹ fine-tuning. We take this approach because a generic broken minimal SUSY theory has
¹²⁰ two relevant energy scales: a high-scale one at which SUSY breaking takes place, and a
¹²¹ low-scale one (M_{SUSY}) where the resulting SUSY particle spectrum is situated and the
¹²² EWSB conditions must be satisfied. We do not know which and how many fundamental
¹²³ parameters exist for a possible high-scale theory. The EW FT measure does not take such
¹²⁴ underlying high-scale model assumptions into account for its computation. The EW FT
¹²⁵ measure (Δ_{EW}) parameterizes how sensitive M_Z is to variations in each of the coefficients
¹²⁶ C_i , which are evaluated at M_Z . It is defined as

$$\Delta_{\text{EW}} \equiv \max_i \left| \frac{C_i}{M_Z^2/2} \right|, \quad (7)$$

¹²⁷ where the C_i are

$$C_{m_{H_d}} = \frac{m_{H_d}^2}{\tan^2 \beta - 1}, \quad C_{m_{H_u}} = \frac{-m_{H_u}^2 \tan^2 \beta}{\tan^2 \beta - 1}, \quad C_\mu = -\mu^2,$$

$$C_{\Sigma_d^d} = \frac{\max(\Sigma_d^d)}{\tan^2 \beta - 1}, \quad C_{\Sigma_u^u} = \frac{-\max(\Sigma_u^u) \tan^2 \beta}{\tan^2 \beta - 1}.$$

¹²⁸ The tadpole contributions Σ_u^u and Σ_d^d contain a sum of different contributions. These
¹²⁹ contributions are computed individually and the maximum contribution is used to compute
¹³⁰ the $C_{\Sigma_u^u}$ and $C_{\Sigma_d^d}$ coefficients. We will use an upper bound of $\Delta_{\text{EW}} < 100$ (implying no
¹³¹ worse than $\mathcal{O}(1\%)$ fine-tuning on the mass of the Z -boson) to determine whether a given
¹³² set of MSSM parameters is fine-tuned, and use the code from Ref. [63] to compute the
¹³³ measure.

¹³⁴ Using this measure, one generically finds that minimally fine-tuned scenarios have low

values for $|\mu|$, where $\Delta_{\text{EW}} = 100$ is reached at $|\mu| \simeq 800$ GeV [63, 65, 69, 71–75]. The masses of the gluino, sbottom, stop and squarks are allowed to get large for models with low Δ_{EW} [64, 76, 77]. Therefore, we assume that the masses of these sparticles are above 2.5 TeV (for the gluino), above 1.2 TeV (for the stops and bottoms) and above 2 TeV (for the squarks), such that they evade the ATLAS and CMS limits ².

2.2 The muon anomalous magnetic moment

In the pMSSM, one-loop contributions to a_μ arise from diagrams with a chargino-sneutrino or neutralino-smuon loop [78]. The expressions for these one-loop corrections read [79]

$$\delta a_\mu^{\tilde{\chi}_i^0} = \frac{m_\mu}{16\pi^2} \sum_{i=1}^4 \sum_{m=1}^2 \left[-\frac{m_\mu}{12m_{\tilde{\mu}_m}^2} (|n_{im}^L|^2 + |n_{im}^R|^2) F_1^N \left(\frac{m_{\tilde{\chi}_i^0}^2}{m_{\tilde{\mu}_m}^2} \right) + \frac{m_{\tilde{\chi}_i^0}}{3m_{\tilde{\mu}_m}^2} \text{Re} [n_{im}^L n_{im}^R] F_2^N \left(\frac{m_{\tilde{\chi}_i^0}^2}{m_{\tilde{\mu}_m}^2} \right) \right], \quad (8)$$

$$\delta a_\mu^{\tilde{\chi}_k^\pm} = \frac{m_\mu}{16\pi^2} \sum_{k=1}^2 \left[\frac{m_\mu}{12m_{\tilde{\nu}_\mu}^2} (|c_k^L|^2 + |c_k^R|^2) F_1^C \left(\frac{m_{\tilde{\chi}_k^\pm}^2}{m_{\tilde{\nu}_\mu}^2} \right) + \frac{2m_{\tilde{\chi}_k^\pm}}{3m_{\tilde{\nu}_\mu}^2} \text{Re} [c_k^L c_k^R] F_2^C \left(\frac{m_{\tilde{\chi}_k^\pm}^2}{m_{\tilde{\nu}_\mu}^2} \right) \right] \quad (9)$$

with m_μ the muon mass, $m_{\tilde{\mu}_m}$ the first or second smuon mass, $m_{\tilde{\nu}_\mu}$ the muon sneutrino mass, i, m and k the indices for the neutralinos, smuons and charginos and the couplings

$$n_{im}^R = \sqrt{2}g_1 N_{i1} X_{m2} + y_\mu N_{i3} X_{m1}, \quad n_{im}^L = \frac{1}{\sqrt{2}} (g_2 N_{i2} + g_1 N_{i1}) X_{m1}^* - y_\mu N_{i3} X_{m2}^*, \quad (10)$$

$$c_k^R = y_\mu U_{k2}, \quad c_k^L = -g_2 V_{k1}. \quad (11)$$

The down-type muon Yukawa coupling is denoted by $y_\mu = g_2 m_\mu / (\sqrt{2} M_W \cos \beta)$, and the SU(2) and U(1) gauge couplings are g_2 and g_1 . The matrices N and U, V diagonalize the neutralino and chargino mass matrices (Eq. (4), (5)), while the unitary matrix X diagonalizes the smuon mass matrix M_μ^2 , which reads for the pMSSM in the $(\tilde{\mu}_L, \tilde{\mu}_R)$ basis

$$M_\mu^2 = \begin{pmatrix} m_{\tilde{L}_1}^2 + (s_{\theta_W}^2 - \frac{1}{2}) M_Z^2 \cos(2\beta) & -m_\mu \mu \tan \beta \\ -m_\mu \mu \tan \beta & m_{\tilde{e}_R}^2 - s_{\theta_W}^2 M_Z^2 \cos(2\beta) \end{pmatrix}. \quad (12)$$

The loop functions $F_{1,2}^N$ and $F_{1,2}^C$ can be found in Ref. [79]. They are normalized such that $F_{1,2}^{N,C}(x=1) = 1$, and go to zero for $x \rightarrow \infty$.

At two-loop, the numerical values of the various contributions differ considerably. The photonic Barr-Zee diagrams are the source of the largest possible two-loop contribution. Here a Higgs boson and a photon connect to either a chargino or sfermion loop [80] ³.

As one can see in the expressions above, the chargino-sneutrino and neutralino-smuon contributions are controlled by $M_1, M_2, \tan \beta$ and μ (through $m_{\tilde{\chi}_i^0}$ and $m_{\tilde{\chi}_k^\pm}$), as well as $m_{\tilde{L}_1}$ and $m_{\tilde{e}_R}$ (through $m_{\tilde{\mu}_m}$ and $m_{\tilde{\nu}_\mu}$). They are enhanced when $\tan \beta$ grows large and when simultaneously light ($\mathcal{O}(100)$ GeV) neutralinos/charginos and smuons/sneutrinos exist in the sparticle spectrum. The Barr-Zee diagrams are enhanced by large values of $\tan \beta$, small values of m_A and large Higgs-sfermion couplings. In general, the one-loop chargino-sneutrino contribution dominates over the neutralino-slepton contribution [79],

²Note that those limits are shown to be significantly less stringent for MSSM spectra with rich sparticle decays, see e.g. Ref. [58].

³Two-loop corrections from sfermion loops contribute with a few percent here as well, since we assume heavy squark masses [81, 82].

162 unless there is a large smuon left-right mixing induced by a sizable value for μ [83]. These
163 latter spectra will however result in slightly higher FT values, which is a direct consequence
164 of a higher value of $|\mu|$.

165 3 Analysis setup

166 To create the SUSY spectra we use SOFTSUSY 4.0 [84], the Higgs mass is calculated using
167 FeynHiggs 2.14.2 [85–89], and SUSYHIT [90] is used to calculate the decay of the SUSY
168 and Higgs particles. Vevacious [91–93] is used to check that the models have at least a
169 meta-stable minimum state that has a lifetime that exceeds that of our universe and that
170 this state is not color/charge breaking⁴. We use SUSY-AI [94] and SMODELS [95–99]
171 to determine the LHC exclusion of a model point. LHC cross sections for sparticle pro-
172 duction at NLO accuracy are calculated using Prospino [100]. HIGGSBOUNDS 5.1.1 is
173 used to determine whether the SUSY models satisfy the LEP, Tevatron and LHC Higgs
174 constraints [101–108]. MICROMEGAs 5.2.1 [109–114] is used to compute the DM relic
175 density ($\Omega_{\text{DM}} h^2$), the present-day velocity-weighted annihilation cross section ($\langle \sigma v \rangle$) and
176 the spin-dependent and spin-independent dark-matter–nucleon scattering cross sections
177 ($\sigma_{\text{SD},p}$ and $\sigma_{\text{SI},p}$). For DM indirect detection we only consider the limit on $\langle \sigma v \rangle$ stemming
178 from the observation of gamma rays originating from dwarf galaxies, which we implement
179 as a hard cut on each of the channels reported on the last page of Ref. [115]. The current
180 constraints on the dark-matter–nucleon scattering cross sections originating from various
181 dark matter direct detection (DMDD) experiments are determined via MICROMEGAs,
182 while future projections of constraints are determined via DDCALC 2.0.0 [116]. Flavor ob-
183 servables are computed with SuperIso 4.1 [117, 118], while the muon anomalous magnetic
184 moment and its theoretical uncertainty is determined with GM2Calc [81, 119–121].
185 We use the Gaussian particle filter [122] to search the pMSSM parameter space for in-
186 teresting areas. The lightest SM-like Higgs boson is required to be in the mass range of
187 $122 \text{ GeV} \leq m_h \leq 128 \text{ GeV}$. Spectra that do not satisfy the LHC bounds on sparticle
188 masses, branching fractions of B/D -meson decays, the DMDD, or DM indirect detection
189 bounds are removed. Our spectra are furthermore required to satisfy the LEP limits on
190 the masses of the charginos, light sleptons and staus ($m_{\tilde{\chi}_1^\pm} > 103.5 \text{ GeV}$, $m_{\tilde{l}^\pm} > 90 \text{ GeV}$
191 and $m_{\tilde{\tau}^\pm} > 85 \text{ GeV}$) [123, 124], and the constraints on the invisible and total width of the
192 Z -boson ($\Gamma_{Z,\text{inv}} = 499.0 \pm 1.5 \text{ MeV}$ and $\Gamma_Z = 2.4952 \pm 0.0023 \text{ GeV}$) [125].

193 4 Phenomenology

194 We assume that the DM abundance is determined by thermal freeze-out and require that
195 the lightest neutralino saturates $\Omega_{\text{DM}} h^2$ with the observed value of 0.12 [8] within 0.03 to
196 allow for a theoretical uncertainty on the relic-density calculation. As shown above, the
197 mass eigenstate of the DM particle is a mixture of bino, wino and higgsino interaction
198 eigenstates. To obtain the correct relic density in the pMSSM with a pure state, one
199 can either have a higgsino with a mass of $m_{\tilde{\chi}_1^0} \simeq 800 \text{ GeV}$ or a wino with $m_{\tilde{\chi}_1^0} \simeq 2.5 \text{ TeV}$.
200 Spectra that saturate the relic density with lower DM masses necessarily are predominantly
201 bino-like, mixed with higgsino/wino components. Negligible higgsino/wino components are
202 found in so-called funnel regions [126, 127], i.e. regions where the mass of the DM particle is
203 roughly half of the mass of the Z boson, SM-like Higgs boson or heavy Higgs boson. In such

⁴These scenarios appear in the $(g - 2)_\mu$ context for large $\mu \tan \beta$, see e.g. Ref. [83].

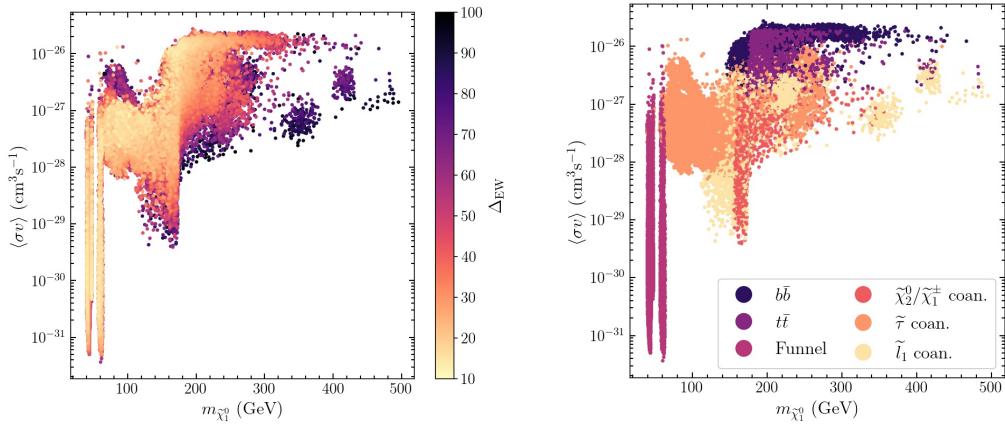


Figure 1: The mass of the DM particle ($m_{\tilde{\chi}_1^0}$) vs the velocity-weighted annihilation cross section ($\langle \sigma v \rangle$). The value of Δ_{EW} is shown as a color code on the left, where the points are ordered such that spectra with lower values of Δ_{EW} lie on top of those with higher values of Δ_{EW} . On the right we show the dominant early-universe annihilation process that contributes to the value of $\Omega_{DM} h^2$. In both plots, we only show points that satisfy all experimental constraints, and have $133 \times 10^{-11} < \Delta a_\mu < 369 \times 10^{-11}$, allowing for a 2σ uncertainty.

204 a scenario, the mass of the neutralino can even get below 100 GeV with $M_1 < 100$ GeV, and
 205 in particular the early-universe DM annihilation cross section is enhanced for $m_{\tilde{\chi}_1^0} \simeq m_h/2$
 206 and $M_Z/2$. Moreover, spectra with another particle close in mass to the LSP can satisfy
 207 the relic density constraint without having a large wino/higgsino component too, due to
 208 the co-annihilation mechanism [128].

209 The case where the lightest neutralino is predominantly wino-like results in a fine-tuned
 210 spectrum: to obtain the right relic density $M_2 \simeq 2.5$ TeV for a pure wino, so $|\mu| >$
 211 2.5 TeV in that scenario. Secondly, such high LSP neutralino masses do not give a large
 212 enough contribution to Δa_μ , since the other sparticle masses have to exceed this LSP
 213 mass. The pure-higgsino solutions do not allow for an explanation of Δa_μ [51] either.
 214 Therefore our solutions, as shown in Fig. 1, feature predominantly bino-like LSPs. Due to
 215 the combined Δa_μ constraint (requiring high $\tan \beta$), DMDD limits and the FT requirement,
 216 the composition has a small higgsino component (< 20%) and a negligible wino component.
 217 The second-to-lightest neutralino and the lightest chargino are either wino-like, higgsino-
 218 like, or mixed wino-higgsino states. It might be surprising to see that spectra with bino-
 219 higgsino LSPs are allowed to have wino-like $\tilde{\chi}_2^0/\tilde{\chi}_1^\pm$. Such configurations can however be
 220 found in spectra for which M_1 , M_2 and $|\mu|$ are all of $\mathcal{O}(100)$ GeV with M_2 being smaller
 221 than $|\mu|$, and that have moderate to large values of $\tan \beta$ ($10 \lesssim \tan \beta \lesssim 20$). From Eq. (4)
 222 one may infer that for such spectra, little mixing can take place between the bino and
 223 wino. This results in negligible wino components of the LSP, whereas $\tilde{\chi}_1^\pm$ and $\tilde{\chi}_2^0$ can be
 224 predominantly wino-like. Moreover, decreasing $|\mu|$ for such models will not only result in
 225 a higher higgsino-component, but counter-intuitively also in a *higher* wino component of
 226 the LSP, while the wino component of $\tilde{\chi}_1^\pm$ and $\tilde{\chi}_2^0$ then *decreases*. Because of these higher
 227 wino/higgsino components of the LSP, such scenarios result in larger values of $\sigma_{SI,p}$ and
 228 $\sigma_{SD,p}$. Therefore, decreasing $|\mu|$ for these scenarios is limited by the constraints imposed
 229 by the DMDD experiments. The spectra where $\tilde{\chi}_1^\pm$ and $\tilde{\chi}_2^0$ are predominantly higgsino-like
 230 are typically difficult to probe at the LHC due to low production cross sections compared
 231 to the pure wino $\tilde{\chi}_1^\pm/\tilde{\chi}_2^0$ case.

232 In Fig. 1 we show the spectra that survive all constraints and have $\Delta_{EW} < 100$. Lower
 233 values for Δ_{EW} are generally found for lower DM masses. The mass of the DM particle
 234 does not exceed 500 GeV, which is a direct result of the combined requirements of having

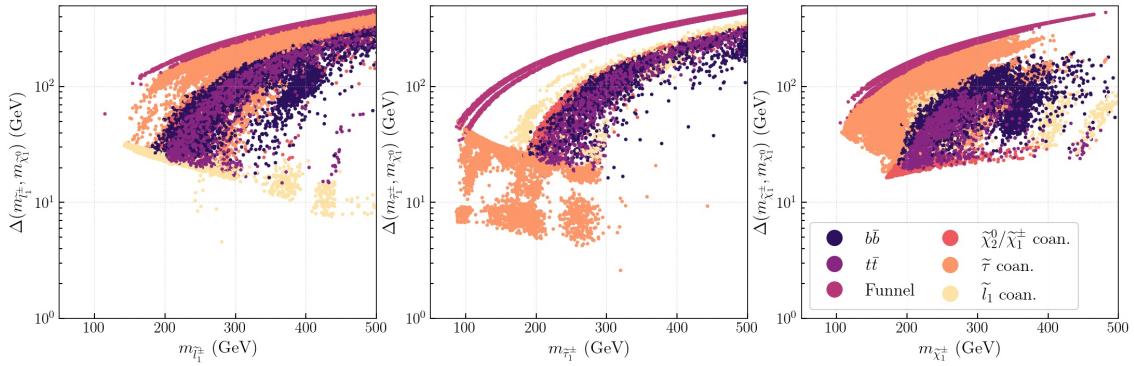


Figure 2: The mass difference between the DM particle and the lightest chargino (left), lightest smuon (middle) and lightest stau (right) versus the mass of the heavier particle. The color code represents the dominant early-universe annihilation channel.

235 $\Delta_{EW} < 100$ and a sufficiently high contribution to Δa_μ . The lowest-obtained value is
 236 $\Delta_{EW} = 12.3$. From the right-hand side of Fig. 1, we can distinguish three different type of
 237 DM early-universe annihilation mechanisms: the funnel regions, the coannihilation regions
 238 and the bino-higgsino solution (indicated with $b\bar{b}$ and $t\bar{t}$). As the LHC phenomenology of
 239 these three early-universe annihilation regimes can be quite different, we now discuss them
 240 one-by-one.

241 4.1 LHC phenomenology for the funnel regimes

242 We start with the funnel regions, of which there are two in our spectra⁵. The first one
 243 centers around $m_{\tilde{\chi}_1^0} \simeq 40$ GeV, which is slightly less than $M_Z/2$. This can be explained
 244 as follows. The velocities of the DM particles were much higher in the early universe
 245 than what they are in the present-day universe. This means that DM annihilations via
 246 s-channel Z exchanges could happen on-resonance in the early universe, whereas in the
 247 present-day universe these exchanges only happen off-resonance. This also explains the
 248 fact that the value for $\langle\sigma v\rangle$ is allowed to get orders of magnitude smaller than the value
 249 that one usually expects for a thermal relic (around $\langle\sigma v\rangle = 3 \cdot 10^{-26} \text{ cm}^3 \text{s}^{-1}$ for a DM mass
 250 of 100 GeV). These models are characterized by small wino/higgsino components of the
 251 LSP - otherwise the early-universe annihilation would be too efficient, resulting in a too-
 252 low value of $\Omega_{\text{DM}} h^2$. The second funnel region is centered around $m_{\tilde{\chi}_1^0} \simeq 60$ GeV, slightly
 253 less than $m_h/2$. These DM particles annihilated in the early universe predominantly via
 254 s-channel SM-like Higgs exchanges. No solutions are found for spectra with DM masses
 255 in-between the two funnel regions. Here, the wino/higgsino component necessarily needs
 256 to increase to satisfy the $\Omega_{\text{DM}} h^2$ requirement, and these spectra are excluded by DMDD
 257 experiments. The minimal value of Δ_{EW} for these spectra is 13.2.

258 The two funnel regimes are characterized by light ($m_{\tilde{\chi}_1^0} < 100$ GeV) bino-like LSPs. The $\tilde{\chi}_1^\pm$
 259 and $\tilde{\chi}_2^0$ are degenerate in mass. They are wino mixtures for masses around 100 – 200 GeV,
 260 while they become higgsino-like for heavier $\tilde{\chi}_1^\pm / \tilde{\chi}_2^0$ (up to $m_{\tilde{\chi}_1^\pm / \tilde{\chi}_2^0} \simeq 500$ GeV). The
 261 mass gap between $\tilde{\chi}_1^0$ and $\tilde{\chi}_2^0$ or $\tilde{\chi}_1^\pm$ ($\Delta(m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_1^0})$ or $\Delta(m_{\tilde{\chi}_1^\pm}, m_{\tilde{\chi}_1^0})$) is at least around
 262 50 GeV, and exceeds 100 GeV for $m_{\tilde{\chi}_1^\pm} \gtrsim 150$ GeV (see Fig. 2, left panel). The masses
 263 of the sleptons are heavier than (at least) the masses of $\tilde{\chi}_2^0$ and $\tilde{\chi}_1^\pm$. Therefore, three
 264 different sorts of decays for $\tilde{\chi}_2^0$ can be identified: 1. $\tilde{\chi}_2^0 \rightarrow h\tilde{\chi}_1^0$ when $\Delta(m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_1^0}) > m_h$,
 265 2. $\tilde{\chi}_2^0 \rightarrow Z\tilde{\chi}_1^0$ when $\Delta(m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_1^0}) > M_Z$, and 3. off-shell decays when $\Delta(m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_1^0}) < M_Z$.

⁵The heavy Higgs funnel is not identified here, and will be left for future study.

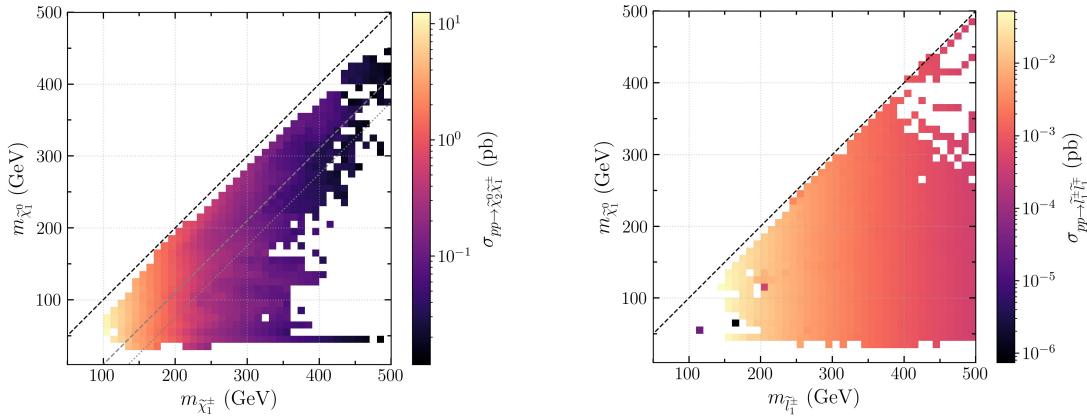


Figure 3: The mass of the DM particle versus the mass of the lightest chargino (left) and smuon (right), combined in 10 by 10 GeV bins. The average production cross section of $\sigma_{pp \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_1^\pm}$ (left) and $\sigma_{pp \rightarrow \tilde{l}_1^\pm \tilde{l}_1^\mp}$ (right) is shown in color code for each bin. The dashed black line in the plot on the left-hand side shows the limit where $m_{\tilde{\chi}_1^0} = m_{\tilde{\chi}_1^\pm}$, whereas the gray dashed (dotted) lines show $m_{\tilde{\chi}_1^\pm} = m_{\tilde{\chi}_1^0} + M_Z$ ($m_{\tilde{\chi}_1^\pm} = m_{\tilde{\chi}_1^0} + m_h$). The dashed black line in the plot on the right-hand side shows $m_{\tilde{\chi}_1^0} = m_{\tilde{l}_1^\pm}$.

For $\tilde{\chi}_1^\pm$, there are only two sorts of decays: 1. $\tilde{\chi}_1^\pm \rightarrow W^\pm \tilde{\chi}_1^0$ when $\Delta(m_{\tilde{\chi}_1^\pm}, m_{\tilde{\chi}_1^0}) > M_W$, and 2. off-shell decays when $\Delta(m_{\tilde{\chi}_1^\pm}, m_{\tilde{\chi}_1^0}) < M_W$. Searches for $\tilde{\chi}_2^0 \tilde{\chi}_1^\pm$ production with on-shell decays of $\tilde{\chi}_2^0 \rightarrow Z \tilde{\chi}_1^0$ are most sensitive to our spectra [129–131]. In our models, whenever $\Delta(m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_1^0}) > m_h$, there exists a mixture between $\tilde{\chi}_2^0 \rightarrow h \tilde{\chi}_1^0$ and $\tilde{\chi}_2^0 \rightarrow Z \tilde{\chi}_1^0$ decays. The sensitivity of the experiments drops when $\tilde{\chi}_2^0$ can decay into the SM-like Higgs boson [130, 132]. The simplified limits of the searches mentioned above assume a wino-like $\tilde{\chi}_2^0 \tilde{\chi}_1^\pm$ pair, whereas we deal with mixed wino-higgsino pairs. To recast their analysis, we show in the left panel of Fig. 3 the average cross section per 10 by 10 GeV bin for $\tilde{\chi}_2^0 \tilde{\chi}_1^\pm$ production. We find that our cross sections in the regime where $M_Z < \Delta(m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_1^0}) < m_h$ do not exceed the 95% confidence level (CL) limits of Ref. [130, 131]. The models with off-shell decays are slightly more constrained by the LHC experiments. Particularly Ref. [133] excludes some of our spectra in this regime that have $m_{\tilde{\chi}_1^\pm}$ up to 210 GeV and $\Delta(m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_1^0}) < 55$ GeV.

4.2 LHC phenomenology for the coannihilation regimes

The second regime is the coannihilation regime. It starts to open up at DM masses of roughly 75 GeV, as no charged sparticles (and therefore no coannihilation partners other than the sneutrino) can exist with masses below 85 GeV due to the LEP/LHC bounds. Three different types of coannihilation partners are identified: first-/second-generation sleptons, third-generation sleptons, and charginos or heavier neutralinos. Interestingly, only with the help of slepton coannihilations the DM particle can have a mass between $\mathcal{O}(70 - 150)$ GeV and still give the right $\Omega_{\text{DM}} h^2$. To obtain the right relic density in this regime without a slepton-coannihilation partner, one generally needs high higgsino fractions, which increases the value of $\sigma_{\text{SI}, p}$ beyond the exclusion limit of the DMDD experiments. The lowest values of Δ_{EW} are found in the stau-coannihilation regime ($\Delta_{\text{EW}} = 12.3$), while the first-/second-generation slepton and chargino/neutralino regimes result in lowest values $\Delta_{\text{EW}} = 14.4$ and $\Delta_{\text{EW}} = 16.4$ respectively. The coannihilation regimes are all characterized by small mass differences between the LSP and its coannihilation partner(s).

The first type of coannihilation is that of first-/second-generation sleptons (\tilde{l}_1^\pm). The compression between $m_{\tilde{l}_1^\pm}$ and $m_{\tilde{\chi}_1^0}$ is increased for higher LSP masses such that the right $\Omega_{\text{DM}} h^2$ can still be obtained. Spectra with $\Delta(m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_1^0}) > M_Z$ are under strong constraints from searches for $\tilde{\chi}_2^0 \tilde{\chi}_1^\pm \rightarrow \tilde{l} l \nu_l$ (see e.g. [132]). We explicitly remove those points from our spectra, leaving only models with $\Delta(m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_1^0}) < M_Z$. The $\tilde{\chi}_1^\pm$ and $\tilde{\chi}_2^0$ sparticles are typically higgsino-like with a small wino component, and have masses between 180 and 500 GeV.

The second coannihilation regime is characterized by low $\tilde{\tau}_1^\pm$ masses. The masses of $\tilde{\chi}_1^\pm/\tilde{\chi}_2^0$ can still be as light as 105 GeV in this regime, where they are predominantly wino-like. The higgsino component of these particles increases when their masses increase, up to $m_{\tilde{\chi}_1^\pm/\tilde{\chi}_2^0} \simeq 500$ GeV. Although we have a large production cross section for the wino-like $\tilde{\chi}_1^\pm/\tilde{\chi}_2^0$ pair, these models are not constrained by the LHC experiments due to the presence of the light staus. The staus are often lighter than $\tilde{\chi}_1^\pm$ and $\tilde{\chi}_2^0$, and the searches for $\tilde{\tau}_1^\pm$ -mediated decays of $\tilde{\chi}_1^+ \tilde{\chi}_1^- / \tilde{\chi}_1^\pm \tilde{\chi}_2^0$ production have no sensitivity when $\Delta(m_{\tilde{\chi}_1^0}, m_{\tilde{\tau}_1^\pm}) < 100$ GeV [134,135]. The latter holds for our spectra in the second coannihilation regime, since the mass differences between the LSP and $\tilde{\tau}_1^\pm$ are between 5 – 50 GeV in that case. Additionally, relatively few LHC searches for low-mass $\tilde{\tau}^\pm$ particles exist. Small $\tilde{\tau}^+ \tilde{\tau}^-$ production cross sections and low signal acceptances make these searches difficult, so the experiments have no constraining power in the compressed regime [136,137].

A dedicated low mass $\tilde{\tau}^\pm$ search without an assumed mass degeneracy between $\tilde{\tau}_1^\pm$ and $\tilde{\tau}_2^\pm$ would be interesting to probe the sensitivity of the LHC to these scenarios.

The last coannihilation regime has a $\tilde{\chi}_1^\pm$ or $\tilde{\chi}_2^0$ that is close in mass to the LSP. Note that although the slepton masses in these regions can be $\mathcal{O}(200)$ GeV, the results from the $\tilde{l}_{R,L}^\pm \tilde{l}_{R,L}^\pm$ searches with $\tilde{l}^\pm = \tilde{e}^\pm, \tilde{\mu}^\pm$ or $\tilde{\tau}^\pm$ (e.g. [137–139]) are not directly applicable here, as often one or more of the chargino/heavier neutralino states is lighter than the sleptons. Therefore, the slepton will not decay with a 100% branching ratio to $\tilde{\chi}_1^0 l^\pm$, although this is assumed in the above-mentioned searches. Instead, in this regime, only the $\tilde{\chi}_1^\pm \tilde{\chi}_2^0$ searches are of relevance, similar to the case in the funnel region discussed above. Interestingly, although the mass compression for the slepton coannihilation regimes needs to increase to obtain the right relic density for higher DM masses, for the gaugino-coannihilation regime it instead needs to decrease. The mass compression between the LSP and wino-higgsino like $\tilde{\chi}_1^\pm/\tilde{\chi}_2^0$ sparticles is generally around 15-20 GeV, and Ref. [133] excludes our solutions with $m_{\tilde{\chi}_1^\pm}$ up to 140 – 180 GeV.

4.3 LHC phenomenology for the bino-higgsino LSP

The last regime we identify consists of bino-higgsino LSPs and is labeled with $b\bar{b}$ and $t\bar{t}$. These early-universe annihilation channels are mediated by either s-channel Z or h/H exchanges. The $t\bar{t}$ annihilation channel opens up when $m_{\tilde{\chi}_1^0}$ becomes larger than the mass of the top quark m_t , as then the invariant mass of the two LSPs is enough to create a $t\bar{t}$ pair⁶. For the Z -exchange channel this annihilation becomes favored over the annihilation into a lighter fermion pair, since any Z -mediated annihilation of two Majorana fermions is helicity suppressed at tree level [140]. This is explained as follows. The two identical LSPs form a Majorana pair. Such a pair is even under the operation of charge-conjugation $C = (-1)^{L+S}$ with S the total spin and L the total orbital angular momentum, so L and S must either both be even, or both be odd. Taking the limit of zero velocity, as the present-day velocity of DM particles is non-relativistic, we may assume $L = 0$ and even S .

⁶The annihilation to a $W^+ W^-$ pair is possible when $m_{\tilde{\chi}_1^0} > M_W$. However, this is constrained by DMDD due to the high wino/higgsino fraction that is necessary for this channel.

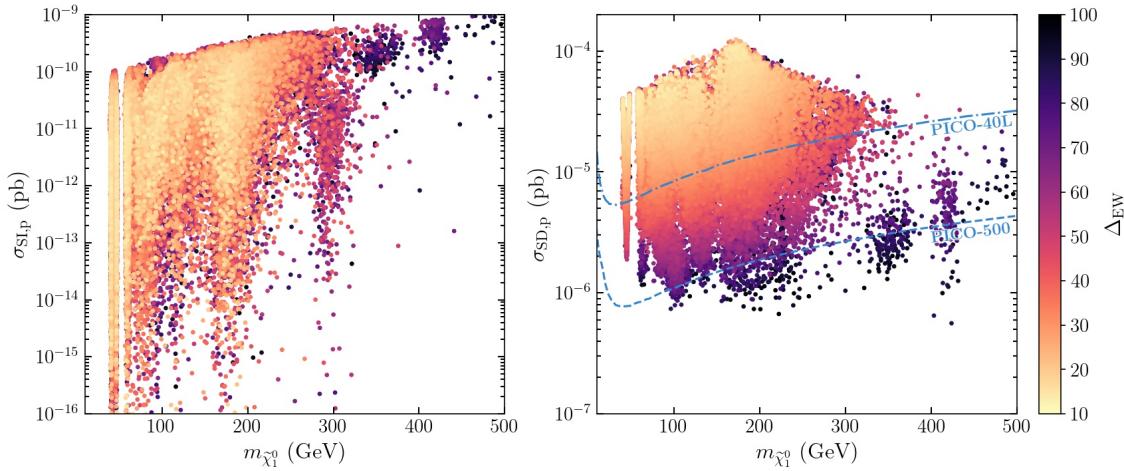


Figure 4: Right (left): The mass of the DM particle versus the spin-(in)dependent cross section $\sigma_{SD,p}$ ($\sigma_{SI,p}$). The value of Δ_{EW} is shown in color code. We also show the projected PICO-40L and PICO-500 central limits on $\sigma_{SD,p}$ [141]. The points are ordered such that those with lower values of Δ_{EW} lie on top of those with higher values.

The final-state fermion pair can have a total spin of $S = 1$ or $S = 0$, but only the latter is allowed for the Majorana-pair annihilation in the non-relativistic limit. For a Dirac-field pair, an $S = 0$ configuration is obtained if the fermion and anti-fermion are from different Weyl spinors: a left- and right-handed one. In the SM, a coupling with this combination only arises (at tree level) by a mass insertion. Therefore, the transition amplitude is proportional to the mass of the final-state fermions, and a decay to a heavier pair of fermions is generally preferred. In spectra where $\tan \beta$ is large we also see the heavy-Higgs-mediated decays to $b\bar{b}$, as the bottom-Yukawa coupling is enhanced. As can be seen in Fig. 2, in the regime of $m_{\tilde{\chi}_1^0} \gtrsim m_t$, the masses of $\tilde{\chi}_1^\pm$ and $\tilde{\chi}_2^0$ are relatively close to that of the LSP, so due to the coannihilation mechanism these spectra tend to show slightly lower values of $\langle \sigma v \rangle$ than naively would be expected. The minimal value of Δ_{EW} is around 14.2 for these models. The $\tilde{\chi}_2^0$ and $\tilde{\chi}_1^\pm$ are predominantly higgsino-like with masses from 180 to 500 GeV. Due to their small production cross section, the LHC searches do not have exclusion power in this regime.

4.4 Dark-matter direct detection experiments

In the previous subsections we discussed the phenomenology of the viable spectra at the LHC. We now comment on the sensitivity of DMDD experiments. The resulting values for $\sigma_{SI,p}$ and $\sigma_{SD,p}$ may be seen in Fig. 4. While the value of $\sigma_{SI,p}$ varies by over 7 orders of magnitude, $\sigma_{SD,p}$ is relatively constrained. Moreover, we observe that $\sigma_{SD,p}$ is directly correlated with Δ_{EW} : lower values of $\sigma_{SD,p}$ result in higher values of Δ_{EW} . This is due to the fact that the LSP in our spectra is always bino-like with a small higgsino component. The value of $\sigma_{SD,p}$ decreases with smaller higgsino fractions in the LSP, while Δ_{EW} increases since $|\mu|$ needs to increase (for a given fixed LSP mass). *For this reason, future DMDD experiments that probe $\sigma_{SD,p}$ will be sensitive to all our solutions, irrespective of the masses and compositions of the rest of the sparticle spectrum.* In Fig. 4, we indicate the projected limit of the PICO-40L and the PICO-500 experiments [141]. We observe that the latter one is sensitive to all of our solutions with $\Delta_{EW} < 62$. The LUX-ZEPLIN experiment [142] (whose projected limit is not shown in Fig. 4) will exclude all of our solutions with $\Delta_{EW} < 100$.

368 5 Conclusion

369 In this paper we have analyzed the spectra in the pMSSM that are minimally fine-tuned,
 370 result in the right $\Omega_{\text{DM}} h^2$ and simultaneously offer an explanation for Δa_μ . In terms of DM
 371 phenomenology, we have distinguished three interesting branches of solutions: the funnel
 372 regimes, three types of coannihilation regimes, and the generic bino-higgsino solution.
 373 All these solutions have in common that the LSP is predominantly bino-like with a small
 374 higgsino component. Masses of the DM particle range between 39 – 495 GeV. We discussed
 375 the phenomenology at the LHC for each of the regimes. The first and second regime
 376 are relatively more constrained by $\tilde{\chi}_2^0 \tilde{\chi}_1^\pm$ searches at the LHC (in particular by the one
 377 presented in Ref. [133]) than the last regime, which is due to the lower wino-components
 378 and higher masses of the $\tilde{\chi}_2^0 / \tilde{\chi}_1^\pm$ sparticles that is typical in the last regime. On the other
 379 hand, in particular when the coannihilation partner of the LSP is a light stau, the LHC
 380 searches show little to no sensitivity to our found solutions. A dedicated low-mass $\tilde{\tau}^\pm$
 381 search without an assumed mass degeneracy between $\tilde{\tau}_1^\pm$ and $\tilde{\tau}_2^\pm$ would be interesting to
 382 probe the sensitivity of the LHC to these scenarios. The requirement of satisfying Δa_μ
 383 excludes models with a higher-mass higgsino of around 600 GeV as the LSP, which means
 384 that the value of $\sigma_{\text{SD},p}$ is directly linked to Δ_{EW} . Therefore, DMDD experiments that
 385 probe $\sigma_{\text{SD},p}$ will ultimately be sensitive to all of our found solutions.

386 Acknowledgments

387 MvB acknowledges support from the Science and Technology Facilities Council (grant
 388 number ST/T000864/1).

389 References

- 390 [1] E. Aprile *et al.*, *Dark matter search results from a one ton-year*
 391 *exposure of XENON1T*, Phys. Rev. Lett. **121**(11), 111302 (2018),
 392 doi:10.1103/PhysRevLett.121.111302, 1805.12562.
- 393 [2] E. Aprile *et al.*, *Constraining the spin-dependent WIMP-nucleon cross*
 394 *sections with XENON1T*, Phys. Rev. Lett. **122**(14), 141301 (2019),
 395 doi:10.1103/PhysRevLett.122.141301, 1902.03234.
- 396 [3] J. Xia *et al.*, *PandaX-II constraints on spin-dependent WIMP-nucleon effective*
 397 *interactions*, Phys. Lett. **B792**, 193 (2019), doi:10.1016/j.physletb.2019.02.043,
 398 1807.01936.
- 399 [4] A. Tan *et al.*, *Dark matter results from first 98.7 days of data from*
 400 *the PandaX-II experiment*, Phys. Rev. Lett. **117**(12), 121303 (2016),
 401 doi:10.1103/PhysRevLett.117.121303, 1607.07400.
- 402 [5] C. Amole *et al.*, *Dark Matter Search Results from the Complete Exposure of the*
 403 *PICO-60 C₃F₈ Bubble Chamber* (2019), 1902.04031.
- 404 [6] C. Amole *et al.*, *Dark Matter Search Results from the PICO-60 C₃F₈ Bubble Cham-*
 405 *ber*, Phys. Rev. Lett. **118**(25), 251301 (2017), doi:10.1103/PhysRevLett.118.251301,
 406 1702.07666.

- 407 [7] C. Amole *et al.*, *Improved dark matter search results from PICO-2L Run 2*, Phys.
408 Rev. **D93**(6), 061101 (2016), doi:10.1103/PhysRevD.93.061101, 1601.03729.
- 409 [8] N. Aghanim *et al.*, *Planck 2018 results. VI. Cosmological parameters*, Astron. As-
410 trophys. **641**, A6 (2020), doi:10.1051/0004-6361/201833910, 1807.06209.
- 411 [9] G. W. Bennett *et al.*, *Final Report of the Muon E821 Anomalous Mag-
412 netic Moment Measurement at BNL*, Phys. Rev. D **73**, 072003 (2006),
413 doi:10.1103/PhysRevD.73.072003, hep-ex/0602035.
- 414 [10] G. W. Bennett *et al.*, *Measurement of the negative muon anomalous
415 magnetic moment to 0.7 ppm*, Phys. Rev. Lett. **92**, 161802 (2004),
416 doi:10.1103/PhysRevLett.92.161802, hep-ex/0401008.
- 417 [11] G. W. Bennett *et al.*, *Measurement of the positive muon anomalous magnetic moment
418 to 0.7 ppm*, Phys. Rev. Lett. **89**, 101804 (2002), doi:10.1103/PhysRevLett.89.101804,
419 [Erratum: Phys.Rev.Lett. 89, 129903 (2002)], hep-ex/0208001.
- 420 [12] G. Colangelo, M. Hoferichter and P. Stoffer, *Two-pion contribution to hadronic
421 vacuum polarization*, JHEP **02**, 006 (2019), doi:10.1007/JHEP02(2019)006, 1810.
422 00007.
- 423 [13] M. Davier, A. Hoecker, B. Malaescu and Z. Zhang, *Reevaluation of the hadronic
424 vacuum polarisation contributions to the Standard Model predictions of the muon
425 g - 2 and $\alpha(m_Z^2)$ using newest hadronic cross-section data*, Eur. Phys. J. C **77**(12),
426 827 (2017), doi:10.1140/epjc/s10052-017-5161-6, 1706.09436.
- 427 [14] A. Keshavarzi, D. Nomura and T. Teubner, *Muon g-2 and $\alpha(M_Z^2)$: a new data-based
428 analysis*, Phys. Rev. D **97**(11), 114025 (2018), doi:10.1103/PhysRevD.97.114025,
429 1802.02995.
- 430 [15] M. Hoferichter, B.-L. Hoid and B. Kubis, *Three-pion contribution to hadronic vacuum
431 polarization*, JHEP **08**, 137 (2019), doi:10.1007/JHEP08(2019)137, 1907.01556.
- 432 [16] A. Kurz, T. Liu, P. Marquard and M. Steinhauser, *Hadronic contribution to the
433 muon anomalous magnetic moment to next-to-next-to-leading order*, Phys. Lett. B
434 **734**, 144 (2014), doi:10.1016/j.physletb.2014.05.043, 1403.6400.
- 435 [17] K. Melnikov and A. Vainshtein, *Hadronic light-by-light scattering contribution to
436 the muon anomalous magnetic moment revisited*, Phys. Rev. D **70**, 113006 (2004),
437 doi:10.1103/PhysRevD.70.113006, hep-ph/0312226.
- 438 [18] G. Colangelo, M. Hoferichter, M. Procura and P. Stoffer, *Dispersion relation for
439 hadronic light-by-light scattering: two-pion contributions*, JHEP **04**, 161 (2017),
440 doi:10.1007/JHEP04(2017)161, 1702.07347.
- 441 [19] M. Hoferichter, B.-L. Hoid, B. Kubis, S. Leupold and S. P. Schneider, *Disper-
442 sion relation for hadronic light-by-light scattering: pion pole*, JHEP **10**, 141 (2018),
443 doi:10.1007/JHEP10(2018)141, 1808.04823.
- 444 [20] A. Gérardin, H. B. Meyer and A. Nyffeler, *Lattice calculation of the pion transition
445 form factor with $N_f = 2 + 1$ Wilson quarks*, Phys. Rev. D **100**(3), 034520 (2019),
446 doi:10.1103/PhysRevD.100.034520, 1903.09471.

- 447 [21] G. Colangelo, F. Hagelstein, M. Hoferichter, L. Laub and P. Stoffer, *Longitudinal*
448 *short-distance constraints for the hadronic light-by-light contribution to $(g-2)_\mu$ with*
449 *large- N_c Regge models*, JHEP **03**, 101 (2020), doi:10.1007/JHEP03(2020)101, 1910.
450 13432.
- 451 [22] G. Colangelo, M. Hoferichter, A. Nyffeler, M. Passera and P. Stoffer, *Remarks on*
452 *higher-order hadronic corrections to the muon $g-2$* , Phys. Lett. B **735**, 90 (2014),
453 doi:10.1016/j.physletb.2014.06.012, 1403.7512.
- 454 [23] P. Masjuan and P. Sanchez-Puertas, *Pseudoscalar-pole contribution to the*
455 *$(g_\mu - 2)$: a rational approach*, Phys. Rev. D **95**(5), 054026 (2017),
456 doi:10.1103/PhysRevD.95.054026, 1701.05829.
- 457 [24] T. Blum, N. Christ, M. Hayakawa, T. Izubuchi, L. Jin, C. Jung and C. Lehner,
458 *Hadronic Light-by-Light Scattering Contribution to the Muon Anomalous Mag-*
459 *netic Moment from Lattice QCD*, Phys. Rev. Lett. **124**(13), 132002 (2020),
460 doi:10.1103/PhysRevLett.124.132002, 1911.08123.
- 461 [25] J. Prades, E. de Rafael and A. Vainshtein, *The Hadronic Light-by-Light Scattering*
462 *Contribution to the Muon and Electron Anomalous Magnetic Moments*, Adv. Ser.
463 Direct. High Energy Phys. **20**, 303 (2009), doi:10.1142/9789814271844_0009, 0901.
464 0306.
- 465 [26] M. Davier, A. Hoecker, B. Malaescu and Z. Zhang, *A new evaluation of the hadronic*
466 *vacuum polarisation contributions to the muon anomalous magnetic moment and to*
467 $\alpha(\mathbf{m}_Z^2)$, Eur. Phys. J. C **80**(3), 241 (2020), doi:10.1140/epjc/s10052-020-7792-2,
468 [Erratum: Eur.Phys.J.C 80, 410 (2020)], 1908.00921.
- 469 [27] A. Keshavarzi, D. Nomura and T. Teubner, *$g-2$ of charged leptons, $\alpha(M_Z^2)$*
470 *, and the hyperfine splitting of muonium*, Phys. Rev. D **101**(1), 014029 (2020),
471 doi:10.1103/PhysRevD.101.014029, 1911.00367.
- 472 [28] C. Gnendiger, D. Stöckinger and H. Stöckinger-Kim, *The electroweak contributions*
473 *to $(g-2)_\mu$ after the Higgs boson mass measurement*, Phys. Rev. D **88**, 053005 (2013),
474 doi:10.1103/PhysRevD.88.053005, 1306.5546.
- 475 [29] A. Czarnecki, W. J. Marciano and A. Vainshtein, *Refinements in electroweak con-*
476 *tributions to the muon anomalous magnetic moment*, Phys. Rev. D **67**, 073006
477 (2003), doi:10.1103/PhysRevD.67.073006, [Erratum: Phys.Rev.D 73, 119901 (2006)],
478 hep-ph/0212229.
- 479 [30] M. Knecht, S. Peris, M. Perrottet and E. De Rafael, *Electroweak hadronic contribu-*
480 *tions to the muon $(g-2)$* , JHEP **11**, 003 (2002), doi:10.1088/1126-6708/2002/11/003,
481 hep-ph/0205102.
- 482 [31] T. Aoyama, T. Kinoshita and M. Nio, *Revised and Improved Value of the QED*
483 *Tenth-Order Electron Anomalous Magnetic Moment*, Phys. Rev. D **97**(3), 036001
484 (2018), doi:10.1103/PhysRevD.97.036001, 1712.06060.
- 485 [32] T. Aoyama, M. Hayakawa, T. Kinoshita and M. Nio, *Complete Tenth-Order*
486 *QED Contribution to the Muon $g-2$* , Phys. Rev. Lett. **109**, 111808 (2012),
487 doi:10.1103/PhysRevLett.109.111808, 1205.5370.
- 488 [33] T. Aoyama *et al.*, *The anomalous magnetic moment of the muon in the Standard*
489 *Model*, Phys. Rept. **887**, 1 (2020), doi:10.1016/j.physrep.2020.07.006, 2006.04822.

- 490 [34] Muon **g – 2** Collaboration, *Muon (g-2) Technical Design Report* (2015), 1501.
491 06858.
- 492 [35] Muon **g – 2** Collaboration, *Measurement of the positive muon anomalous magnetic moment to 0.46 ppm*, Phys. Rev. Lett. **126**, 141801 (2021),
493 doi:10.1103/PhysRevLett.126.141801.
- 494 [36] Muon **g – 2** Collaboration, *Magnetic-field measurement and analysis for the muon g – 2 experiment at fermilab*, Phys. Rev. A **103**, 042208 (2021),
495 doi:10.1103/PhysRevA.103.042208.
- 496 [37] Muon **g – 2** Collaboration, *Measurement of the anomalous precession frequency of the muon in the fermilab muon g – 2 experiment*, Phys. Rev. D **103**, 072002 (2021),
497 doi:10.1103/PhysRevA.103.042208.
- 498 [38] T. Mibe, *Measurement of muon g-2 and edm with an ultra-cold muon beam at j-parc*, Nuclear Physics B - Proceedings Supplements **218**(1), 242 (2011),
499 doi:<https://doi.org/10.1016/j.nuclphysbps.2011.06.039>, Proceedings of the Eleventh
500 International Workshop on Tau Lepton Physics.
- 501 [39] M. Abe *et al.*, *A New Approach for Measuring the Muon Anomalous Magnetic Moment and Electric Dipole Moment*, PTEP **2019**(5), 053C02 (2019),
502 doi:10.1093/ptep/ptz030, 1901.03047.
- 503 [40] M. Badziak and K. Sakurai, *Explanation of electron and muon g – 2 anomalies in the MSSM*, JHEP **10**, 024 (2019), doi:10.1007/JHEP10(2019)024, 1908.03607.
- 504 [41] K. Kowalska, L. Roszkowski, E. M. Sessolo and A. J. Williams, *GUT-inspired SUSY and the muon g – 2 anomaly: prospects for LHC 14 TeV*, JHEP **06**, 020 (2015),
505 doi:10.1007/JHEP06(2015)020, 1503.08219.
- 506 [42] M. A. Ajaib, B. Dutta, T. Ghosh, I. Gogoladze and Q. Shafi, *Neutralinos and sleptons at the LHC in light of muon (g – 2)_μ*, Phys. Rev. D **92**(7), 075033 (2015),
507 doi:10.1103/PhysRevD.92.075033, 1505.05896.
- 508 [43] S. P. Das, M. Guchait and D. P. Roy, *Testing SUSY models for the muon g-2 anomaly via chargino-neutralino pair production at the LHC*, Phys. Rev. D **90**(5),
509 055011 (2014), doi:10.1103/PhysRevD.90.055011, 1406.6925.
- 510 [44] M. Endo, K. Hamaguchi, S. Iwamoto and T. Kitahara, *Muon g – 2 vs LHC Run 2 in supersymmetric models*, JHEP **04**, 165 (2020), doi:10.1007/JHEP04(2020)165,
511 2001.11025.
- 512 [45] K. Hagiwara, K. Ma and S. Mukhopadhyay, *Closing in on the chargino contribution to the muon g-2 in the MSSM: current LHC constraints*, Phys. Rev. D **97**(5), 055035 (2018), doi:10.1103/PhysRevD.97.055035, 1706.09313.
- 513 [46] H. M. Tran and H. T. Nguyen, *GUT-inspired MSSM in light of muon g – 2 and LHC results at $\sqrt{s} = 13$ TeV*, Phys. Rev. D **99**(3), 035040 (2019),
514 doi:10.1103/PhysRevD.99.035040, 1812.11757.
- 515 [47] M. Abdughani, K.-I. Hikasa, L. Wu, J. M. Yang and J. Zhao, *Testing electroweak SUSY for muon g – 2 and dark matter at the LHC and beyond*, JHEP **11**, 095 (2019), doi:10.1007/JHEP11(2019)095, 1909.07792.

- 531 [48] A. Kobakhidze, M. Talia and L. Wu, *Probing the MSSM explanation of the muon*
532 *g-2 anomaly in dark matter experiments and at a 100 TeV pp collider*, Phys. Rev. D
533 **95**(5), 055023 (2017), doi:10.1103/PhysRevD.95.055023, 1608.03641.
- 534 [49] M. Endo, K. Hamaguchi, S. Iwamoto and K. Yanagi, *Probing minimal SUSY*
535 *scenarios in the light of muon g - 2 and dark matter*, JHEP **06**, 031 (2017),
536 doi:10.1007/JHEP06(2017)031, 1704.05287.
- 537 [50] M. Chakraborti, S. Heinemeyer and I. Saha, *Improved $(g - 2)_\mu$ Measurements and*
538 *Supersymmetry*, Eur. Phys. J. C **80**(10), 984 (2020), doi:10.1140/epjc/s10052-020-
539 08504-8, 2006.15157.
- 540 [51] P. Cox, C. Han and T. T. Yanagida, *Muon g - 2 and dark matter in the*
541 *minimal supersymmetric standard model*, Phys. Rev. D **98**(5), 055015 (2018),
542 doi:10.1103/PhysRevD.98.055015, 1805.02802.
- 543 [52] M. Chakraborti, S. Heinemeyer and I. Saha, *Improved $(g - 2)_\mu$ Measurements and*
544 *Wino/Higgsino Dark Matter* (2021), 2103.13403.
- 545 [53] E. A. Bagnaschi *et al.*, *Supersymmetric Dark Matter after LHC Run 1*, Eur. Phys.
546 J. C **75**, 500 (2015), doi:10.1140/epjc/s10052-015-3718-9, 1508.01173.
- 547 [54] G. Bertone, F. Calore, S. Caron, R. Ruiz, J. S. Kim, R. Trotta and C. Weniger,
548 *Global analysis of the pMSSM in light of the Fermi GeV excess: prospects for the*
549 *LHC Run-II and astroparticle experiments*, JCAP **04**, 037 (2016), doi:10.1088/1475-
550 7516/2016/04/037, 1507.07008.
- 551 [55] C. Strege, G. Bertone, G. J. Besjes, S. Caron, R. Ruiz de Austri, A. Strubig and
552 R. Trotta, *Profile likelihood maps of a 15-dimensional MSSM*, JHEP **09**, 081 (2014),
553 doi:10.1007/JHEP09(2014)081, 1405.0622.
- 554 [56] A. Fowlie, K. Kowalska, L. Roszkowski, E. M. Sessolo and Y.-L. S. Tsai, *Dark*
555 *matter and collider signatures of the MSSM*, Phys. Rev. D **88**, 055012 (2013),
556 doi:10.1103/PhysRevD.88.055012, 1306.1567.
- 557 [57] E. Bagnaschi *et al.*, *Likelihood Analysis of the pMSSM11 in Light of LHC 13-TeV*
558 *Data*, Eur. Phys. J. C **78**(3), 256 (2018), doi:10.1140/epjc/s10052-018-5697-0, 1710.
559 11091.
- 560 [58] P. Athron *et al.*, *A global fit of the MSSM with GAMBIT*, Eur. Phys. J. C **77**(12),
561 879 (2017), doi:10.1140/epjc/s10052-017-5196-8, 1705.07917.
- 562 [59] T. Li and S. Raza, *Electroweak supersymmetry from the generalized mini-*
563 *mal supergravity model in the MSSM*, Phys. Rev. D **91**(5), 055016 (2015),
564 doi:10.1103/PhysRevD.91.055016, 1409.3930.
- 565 [60] T. Li, S. Raza and K. Wang, *Constraining Natural SUSY via the Higgs Coupling and*
566 *the Muon Anomalous Magnetic Moment Measurements*, Phys. Rev. D **93**(5), 055040
567 (2016), doi:10.1103/PhysRevD.93.055040, 1601.00178.
- 568 [61] M. Drees and G. Ghaffari, *Impact of the Bounds on the Direct Search for Neutralino*
569 *Dark Matter on Naturalness* (2021), 2103.15617.
- 570 [62] M. Abdughani, L. Wu and J. M. Yang, *Status and prospects of light*
571 *bino-higgsino dark matter in natural SUSY*, Eur. Phys. J. C **78**(1), 4 (2018),
572 doi:10.1140/epjc/s10052-017-5485-2, 1705.09164.

- 573 [63] M. van Beekveld, W. Beenakker, S. Caron, R. Peeters and R. Ruiz de Austri, *Supersymmetry with dark matter is still natural*, Phys. Rev. **D96**(3), 035015 (2017),
574 doi:10.1103/PhysRevD.96.035015, 1612.06333.
- 576 [64] M. van Beekveld, S. Caron and R. Ruiz de Austri, *The current status of fine-tuning in*
577 *supersymmetry*, JHEP **01**, 147 (2020), doi:10.1007/JHEP01(2020)147, 1906.10706.
- 578 [65] H. Baer, V. Barger, D. Sengupta and X. Tata, *Is natural higgsino-only dark matter*
579 *excluded?*, Eur. Phys. J. **C78**(10), 838 (2018), doi:10.1140/epjc/s10052-018-6306-y,
580 1803.11210.
- 581 [66] **MSSM Working Group**, *The minimal supersymmetric standard model: group*
582 *summary report*, In *GDR (Groupement De Recherche) - Supersymetrie Montpellier,*
583 *France, April 15-17, 1998* (1998), 9901246.
- 584 [67] S. R. Coleman and E. J. Weinberg, *Radiative corrections as the origin of spontaneous*
585 *symmetry breaking*, Phys. Rev. **D7**, 1888 (1973), doi:10.1103/PhysRevD.7.1888.
- 586 [68] H. Baer, V. Barger, P. Huang, D. Mickelson, A. Mustafayev and X. Tata, *Radiative*
587 *natural supersymmetry: Reconciling electroweak fine-tuning and the Higgs*
588 *boson mass*, Phys. Rev. **D87**(11), 115028 (2013), doi:10.1103/PhysRevD.87.115028,
589 1212.2655.
- 590 [69] H. Baer, V. Barger, P. Huang, A. Mustafayev and X. Tata, *Radiative natural su-*
591 *persymmetry with a 125 GeV Higgs boson*, Phys. Rev. Lett. **109**, 161802 (2012),
592 doi:10.1103/PhysRevLett.109.161802, 1207.3343.
- 593 [70] H. Baer, V. Barger and D. Mickelson, *How conventional measures overestimate*
594 *electroweak fine-tuning in supersymmetric theory*, Phys. Rev. **D88**(9), 095013 (2013),
595 doi:10.1103/PhysRevD.88.095013, 1309.2984.
- 596 [71] H. Baer, V. Barger and M. Padelfke-Kirkland, *Electroweak versus high scale*
597 *finetuning in the 19-parameter SUGRA model*, Phys. Rev. **D88**, 055026 (2013),
598 doi:10.1103/PhysRevD.88.055026, 1304.6732.
- 599 [72] H. Baer, V. Barger, D. Mickelson and M. Padelfke-Kirkland, *SUSY models under*
600 *siege: LHC constraints and electroweak fine-tuning*, Phys. Rev. **D89**(11), 115019
601 (2014), doi:10.1103/PhysRevD.89.115019, 1404.2277.
- 602 [73] M. Drees and J. S. Kim, *Minimal natural supersymmetry after the LHC8*, Phys.
603 Rev. **D93**(9), 095005 (2016), doi:10.1103/PhysRevD.93.095005, 1511.04461.
- 604 [74] H. Baer, V. Barger, J. S. Gainer, H. Serce and X. Tata, *Reach of the high-energy*
605 *LHC for gluinos and top squarks in SUSY models with light Higgsinos*, Phys. Rev.
606 **D96**(11), 115008 (2017), doi:10.1103/PhysRevD.96.115008, 1708.09054.
- 607 [75] A. Mustafayev and X. Tata, *Supersymmetry, Naturalness, and Light Higgsinos*,
608 Indian J. Phys. **88**, 991 (2014), doi:10.1007/s12648-014-0504-8, 1404.1386.
- 609 [76] H. Baer, V. Barger, P. Huang, D. Mickelson, A. Mustafayev and X. Tata, *Radiative*
610 *natural supersymmetry: Reconciling electroweak fine-tuning and the higgs boson mass*,
611 Phys. Rev. D **87**, 115028 (2013), doi:10.1103/PhysRevD.87.115028.
- 612 [77] H. Baer, V. Barger and M. Savoy, *Upper bounds on sparticle masses from naturalness*
613 *or how to disprove weak scale supersymmetry*, Phys. Rev. D **93**, 035016 (2016),
614 doi:10.1103/PhysRevD.93.035016.

- 615 [78] T. Moroi, *The Muon anomalous magnetic dipole moment in the min-*
616 *imal supersymmetric standard model*, Phys. Rev. D **53**, 6565 (1996),
617 doi:10.1103/PhysRevD.53.6565, [Erratum: Phys.Rev.D 56, 4424 (1997)], hep-ph/
618 9512396.
- 619 [79] S. P. Martin and J. D. Wells, *Muon Anomalous Magnetic Dipole Mo-*
620 *ment in Supersymmetric Theories*, Phys. Rev. D **64**, 035003 (2001),
621 doi:10.1103/PhysRevD.64.035003, hep-ph/0103067.
- 622 [80] D. Stockinger, *The Muon Magnetic Moment and Supersymmetry*, J. Phys. G **34**,
623 R45 (2007), doi:10.1088/0954-3899/34/2/R01, hep-ph/0609168.
- 624 [81] H. Fargnoli, C. Gnendiger, S. Paßehr, D. Stöckinger and H. Stöckinger-Kim, *Two-*
625 *loop corrections to the muon magnetic moment from fermion/sfermion loops in the*
626 *MSSM: detailed results*, JHEP **02**, 070 (2014), doi:10.1007/JHEP02(2014)070, 1311.
627 1775.
- 628 [82] H. G. Fargnoli, C. Gnendiger, S. Paßehr, D. Stöckinger and H. Stöckinger-Kim, *Non-*
629 *decoupling two-loop corrections to $(g-2)_\mu$ from fermion/sfermion loops in the MSSM*,
630 Phys. Lett. B **726**, 717 (2013), doi:10.1016/j.physletb.2013.09.034, 1309.0980.
- 631 [83] M. Endo, K. Hamaguchi, T. Kitahara and T. Yoshinaga, *Probing Bino contribution*
632 *to muon $g - 2$* , JHEP **11**, 013 (2013), doi:10.1007/JHEP11(2013)013, 1309.3065.
- 633 [84] B. C. Allanach, *SOFTSUSY: a program for calculating supersymmetric spectra*,
634 Comput. Phys. Commun. **143**, 305 (2002), doi:10.1016/S0010-4655(01)00460-X,
635 hep-ph/0104145.
- 636 [85] H. Bahl and W. Hollik, *Precise prediction for the light MSSM Higgs boson mass*
637 *combining effective field theory and fixed-order calculations*, Eur. Phys. J. **C76**(9),
638 499 (2016), doi:10.1140/epjc/s10052-016-4354-8, 1608.01880.
- 639 [86] T. Hahn, S. Heinemeyer, W. Hollik, H. Rzehak and G. Weiglein, *High-*
640 *precision predictions for the Light CP-even Higgs boson mass of the Minimal*
641 *Supersymmetric Standard Model*, Phys. Rev. Lett. **112**(14), 141801 (2014),
642 doi:10.1103/PhysRevLett.112.141801, 1312.4937.
- 643 [87] M. Frank, T. Hahn, S. Heinemeyer, W. Hollik, H. Rzehak and G. Weiglein, *The*
644 *Higgs boson masses and mixings of the complex MSSM in the Feynman-diagrammatic*
645 *approach*, JHEP **0702**, 047 (2007), doi:10.1088/1126-6708/2007/02/047, 0611326.
- 646 [88] G. Degrassi, S. Heinemeyer, W. Hollik, P. Slavich and G. Weiglein, *Towards high*
647 *precision predictions for the MSSM Higgs sector*, Eur. Phys. J. **C28**, 133 (2003),
648 doi:10.1140/epjc/s2003-01152-2, 0212020.
- 649 [89] S. Heinemeyer, W. Hollik and G. Weiglein, *FeynHiggs: A program for the calculation*
650 *of the masses of the neutral CP even Higgs bosons in the MSSM*, Comput. Phys.
651 Commun. **124**, 76 (2000), doi:10.1016/S0010-4655(99)00364-1, 9812320.
- 652 [90] A. Djouadi, M. M. Muhlleitner and M. Spira, *Decays of supersymmetric particles: the*
653 *program SUSY-HIT (SUspect-Sdeca Y-Hdecay-InTerface)*, Acta Phys. Polon. **B38**,
654 635 (2007), hep-ph/0609292.
- 655 [91] J. E. Camargo-Molina, B. O'Leary, W. Porod and F. Staub, **Vevacious**: *A tool*
656 *for finding the global minima of one-loop effective potentials with many scalars*, Eur.
657 Phys. J. **C73**(10), 2588 (2013), doi:10.1140/epjc/s10052-013-2588-2, 1307.1477.

- 658 [92] T. L. Lee, T. Y. Li and C. H. Tsai, *Hom4ps-2.0: a software package for solving*
659 *polynomial systems by the polyhedral homotopy continuation method*, Computing
660 **83**(2), 109 (2008), doi:10.1007/s00607-008-0015-6.
- 661 [93] C. L. Wainwright, *CosmoTransitions: Computing cosmological phase transition tem-*
662 *peratures and bubble profiles with multiple fields*, Comput. Phys. Commun. **183**, 2006
663 (2012), doi:10.1016/j.cpc.2012.04.004, 1109.4189.
- 664 [94] S. Caron, J. S. Kim, K. Rolbiecki, R. Ruiz de Austri and B. Stienen, *The BSM-AI*
665 *project: SUSY-AI-generalizing LHC limits on supersymmetry with machine learning*,
666 Eur. Phys. J. **C77**(4), 257 (2017), doi:10.1140/epjc/s10052-017-4814-9, 1605.02797.
- 667 [95] F. Ambrogi *et al.*, *SModelS v1.2: long-lived particles, combination of signal regions,*
668 *and other novelties* (2018), 1811.10624.
- 669 [96] J. Heisig, S. Kraml and A. Lessa, *Constraining new physics with searches for*
670 *long-lived particles: implementation into SModelS*, Phys. Lett. **B788**, 87 (2019),
671 doi:10.1016/j.physletb.2018.10.049, 1808.05229.
- 672 [97] J. Dutta, S. Kraml, A. Lessa and W. Waltenberger, *SModelS extension with*
673 *the CMS supersymmetry search results from Run 2*, LHEP **1**(1), 5 (2018),
674 doi:10.31526/LHEP.1.2018.02, 1803.02204.
- 675 [98] F. Ambrogi, S. Kraml, S. Kulkarni, U. Laa, A. Lessa, V. Magerl, J. Sonneveld,
676 M. Traub and W. Waltenberger, *SModelS v1.1 user manual: Improving simplified*
677 *model constraints with efficiency maps*, Comput. Phys. Commun. **227**, 72 (2018),
678 doi:10.1016/j.cpc.2018.02.007, 1701.06586.
- 679 [99] S. Kraml, S. Kulkarni, U. Laa, A. Lessa, W. Magerl, D. Proschofsky-Spindler and
680 W. Waltenberger, *SModelS: a tool for interpreting simplified-model results from*
681 *the LHC and its application to supersymmetry*, Eur. Phys. J. **C74**, 2868 (2014),
682 doi:10.1140/epjc/s10052-014-2868-5, 1312.4175.
- 683 [100] W. Beenakker, R. Hopker and M. Spira, *PROSPINO: A Program for the production*
684 *of supersymmetric particles in next-to-leading order QCD* (1996), hep-ph/9611232.
- 685 [101] P. Bechtle, S. Heinemeyer, O. Stål, T. Stefaniak and G. Weiglein, *Applying exclusion*
686 *likelihoods from LHC searches to extended Higgs sectors*, Eur. Phys. J. **C75**(9), 421
687 (2015), doi:10.1140/epjc/s10052-015-3650-z, 1507.06706.
- 688 [102] P. Bechtle, O. Brein, S. Heinemeyer, O. Stål, T. Stefaniak, G. Weiglein and K. E.
689 Williams, *HiggsBounds-4: Improved tests of extended Higgs sectors against exclusion*
690 *bounds from LEP, the Tevatron and the LHC*, Eur. Phys. J. **C74**(3), 2693 (2014),
691 doi:10.1140/epjc/s10052-013-2693-2, 1311.0055.
- 692 [103] P. Bechtle, O. Brein, S. Heinemeyer, O. Stål, T. Stefaniak, G. Weiglein and
693 K. Williams, *Recent developments in HiggsBounds and a preview of HiggsSignals*,
694 PoS **2012**, 024 (2012), doi:10.22323/1.156.0024, 1301.2345.
- 695 [104] P. Bechtle, O. Brein, S. Heinemeyer, G. Weiglein and K. E. Williams, *Higgs-*
696 *Bounds 2.0.0: Confronting neutral and charged Higgs sector predictions with ex-*
697 *clusion bounds from LEP and the Tevatron*, Comput. Phys. Commun. **182**, 2605
698 (2011), doi:10.1016/j.cpc.2011.07.015, 1102.1898.

- 699 [105] P. Bechtle, O. Brein, S. Heinemeyer, G. Weiglein and K. E. Williams, *HiggsBounds:*
700 *confronting arbitrary Higgs sectors with exclusion bounds from LEP and the Tevatron*,
701 Comput. Phys. Commun. **181**, 138 (2010), doi:10.1016/j.cpc.2009.09.003, 0811.
702 4169.
- 703 [106] O. Stål and T. Stefaniak, *Constraining extended Higgs sectors with HiggsSignals*,
704 PoS **2013**, 314 (2013), doi:10.22323/1.180.0314, 1310.4039.
- 705 [107] P. Bechtle, S. Heinemeyer, O. Stål, T. Stefaniak and G. Weiglein, *Probing the Stan-*
706 *dard Model with Higgs signal rates from the Tevatron, the LHC and a future ILC*,
707 JHEP **1411**, 039 (2014), doi:10.1007/JHEP11(2014)039, 1403.1582.
- 708 [108] P. Bechtle, S. Heinemeyer, O. Stål, T. Stefaniak and G. Weiglein, *HiggsSignals:*
709 *Confronting arbitrary Higgs sectors with measurements at the Tevatron and the LHC*,
710 Eur. Phys. J. **C74**(2), 2711 (2014), doi:10.1140/epjc/s10052-013-2711-4, 1305.1933.
- 711 [109] G. Belanger, F. Boudjema, A. Pukhov and A. Semenov, *micrOMEGAs: Version 1.3*,
712 Comput. Phys. Commun. **174**, 577 (2006), doi:10.1016/j.cpc.2005.12.005, hep-ph/
713 0405253.
- 714 [110] G. Belanger, F. Boudjema, A. Pukhov and A. Semenov, *MicrOMEGAs 2.0: A*
715 *Program to calculate the relic density of dark matter in a generic model*, Comput.
716 Phys. Commun. **176**, 367 (2007), doi:10.1016/j.cpc.2006.11.008, hep-ph/0607059.
- 717 [111] G. Belanger, F. Boudjema, A. Pukhov and A. Semenov, *Dark matter direct detection*
718 *rate in a generic model with micrOMEGAs 2.2*, Comput. Phys. Commun. **180**, 747
719 (2009), doi:10.1016/j.cpc.2008.11.019, 0803.2360.
- 720 [112] G. Belanger, F. Boudjema, P. Brun, A. Pukhov, S. Rosier-Lees, P. Salati and A. Se-
721 *menov, Indirect search for dark matter with micrOMEGAs2.4*, Comput. Phys. Com-
722 mun. **182**, 842 (2011), doi:10.1016/j.cpc.2010.11.033, 1004.1092.
- 723 [113] G. Belanger, F. Boudjema, A. Pukhov and A. Semenov, *micrOMEGAs_3: A pro-*
724 *gram for calculating dark matter observables*, Comput. Phys. Commun. **185**, 960
725 (2014), doi:10.1016/j.cpc.2013.10.016, 1305.0237.
- 726 [114] G. Belanger, A. Mjallal and A. Pukhov, *Recasting direct detection limits within*
727 *micrOMEGAs and implication for non-standard Dark Matter scenarios* (2020),
728 2003.08621.
- 729 [115] M. Ackermann *et al.*, *Searching for Dark Matter Annihilation from Milky Way Dwarf*
730 *Spheroidal Galaxies with Six Years of Fermi Large Area Telescope Data*, Phys. Rev.
731 Lett. **115**(23), 231301 (2015), doi:10.1103/PhysRevLett.115.231301, 1503.02641.
- 732 [116] **The GAMBIT Dark Matter Workgroup**, *DarkBit: A GAMBIT module for*
733 *computing dark matter observables and likelihoods*, Eur. Phys. J. **C77**(12), 831
734 (2017), doi:10.1140/epjc/s10052-017-5155-4, 1705.07920.
- 735 [117] F. Mahmoudi, *SuperIso: A Program for calculating the isospin asymmetry of*
736 *$B \rightarrow K^* \gamma$ in the MSSM*, Comput. Phys. Commun. **178**, 745 (2008),
737 doi:10.1016/j.cpc.2007.12.006, 0710.2067.
- 738 [118] F. Mahmoudi, *SuperIso v2.3: A Program for calculating flavor physics ob-*
739 *servables in Supersymmetry*, Comput. Phys. Commun. **180**, 1579 (2009),
740 doi:10.1016/j.cpc.2009.02.017, 0808.3144.

- 741 [119] P. Athron, M. Bach, H. G. Farnoli, C. Gnendiger, R. Greifenhagen, J.-h. Park,
742 S. Paßehr, D. Stöckinger, H. Stöckinger-Kim and A. Voigt, *GM2Calc: Precise*
743 *MSSM prediction for ($g - 2$) of the muon*, Eur. Phys. J. C **76**(2), 62 (2016),
744 doi:10.1140/epjc/s10052-015-3870-2, 1510.08071.
- 745 [120] P. von Weitershausen, M. Schafer, H. Stockinger-Kim and D. Stockinger, *Photonic*
746 *SUSY Two-Loop Corrections to the Muon Magnetic Moment*, Phys. Rev. D **81**,
747 093004 (2010), doi:10.1103/PhysRevD.81.093004, 1003.5820.
- 748 [121] M. Bach, J.-h. Park, D. Stöckinger and H. Stöckinger-Kim, *Large muon ($g -$*
749 *2* *with TeV-scale SUSY masses for $\tan\beta \rightarrow \infty$* , JHEP **10**, 026 (2015),
750 doi:10.1007/JHEP10(2015)026, 1504.05500.
- 751 [122] J. H. Kotecha and P. M. Djuric, *Gaussian particle filtering*, IEEE Transactions on
752 Signal Processing **51**(10), 2592 (2003), doi:10.1109/TSP.2003.816758.
- 753 [123] *LEP2 SUSY Working Group, ALEPH, DELPHI, L3 and OPAL experiments*.
- 754 [124] A. Heister *et al.*, *Absolute lower limits on the masses of selectrons and sneutrinos*
755 *in the MSSM*, Phys. Lett. B **544**, 73 (2002), doi:10.1016/S0370-2693(02)02471-1,
756 hep-ex/0207056.
- 757 [125] M. Carena, A. de Gouvea, A. Freitas and M. Schmitt, *Invisible Z boson decays at*
758 *e^+e^- colliders*, Phys. Rev. **D68**, 113007 (2003), doi:10.1103/PhysRevD.68.113007,
759 0308053.
- 760 [126] T. Han, Z. Liu and A. Natarajan, *Dark matter and Higgs bosons in the MSSM*,
761 JHEP **11**, 008 (2013), doi:10.1007/JHEP11(2013)008, 1303.3040.
- 762 [127] G. Belanger, F. Boudjema, A. Cottrant, R. M. Godbole and A. Semenov, *The MSSM*
763 *invisible Higgs in the light of dark matter and g-2*, Phys. Lett. B **519**, 93 (2001),
764 doi:10.1016/S0370-2693(01)00976-5, hep-ph/0106275.
- 765 [128] T. Nihei, L. Roszkowski and R. Ruiz de Austri, *Exact cross-sections for the neutralino*
766 *slepton coannihilation*, JHEP **07**, 024 (2002), doi:10.1088/1126-6708/2002/07/024,
767 hep-ph/0206266.
- 768 [129] M. Aaboud *et al.*, *Search for chargino-neutralino production using recursive jigsaw*
769 *reconstruction in final states with two or three charged leptons in proton-proton col-*
770 *isions at $\sqrt{s} = 13$ TeV with the ATLAS detector*, Phys. Rev. D **98**(9), 092012 (2018),
771 doi:10.1103/PhysRevD.98.092012, 1806.02293.
- 772 [130] A. M. Sirunyan *et al.*, *Combined search for electroweak production of charginos and*
773 *neutralinos in proton-proton collisions at $\sqrt{s} = 13$ TeV*, JHEP **03**, 160 (2018),
774 doi:10.1007/JHEP03(2018)160, 1801.03957.
- 775 [131] A. M. Sirunyan *et al.*, *Search for supersymmetry in final states with two oppositely*
776 *charged same-flavor leptons and missing transverse momentum in proton-proton col-*
777 *isions at $\sqrt{s} = 13$ TeV* (2020), 2012.08600.
- 778 [132] *Search for electroweak production of charginos and neutralinos in proton-proton col-*
779 *isions at $\sqrt{s}=13$ TeV*, Tech. Rep. CMS-PAS-SUS-19-012, CERN, Geneva (2021).
- 780 [133] A. M. Sirunyan *et al.*, *Search for supersymmetry with a compressed mass*
781 *spectrum in the vector boson fusion topology with 1-lepton and 0-lepton final*
782 *states in proton-proton collisions at $\sqrt{s} = 13$ TeV*, JHEP **08**, 150 (2019),
783 doi:10.1007/JHEP08(2019)150, 1905.13059.

- 784 [134] M. Aaboud *et al.*, *Search for the direct production of charginos and neutralinos in*
785 *final states with tau leptons in $\sqrt{s} = 13$ TeV pp collisions with the ATLAS detector*,
786 *Eur. Phys. J. C* **78**(2), 154 (2018), doi:10.1140/epjc/s10052-018-5583-9, 1708.07875.
- 787 [135] A. M. Sirunyan *et al.*, *Search for direct pair production of supersymmetric partners*
788 *to the τ lepton in proton-proton collisions at $\sqrt{s} = 13$ TeV*, *Eur. Phys. J. C* **80**(3),
789 189 (2020), doi:10.1140/epjc/s10052-020-7739-7, 1907.13179.
- 790 [136] A. M. Sirunyan *et al.*, *Search for Supersymmetry with a Compressed Mass Spectrum*
791 *in Events with a Soft τ Lepton, a Highly Energetic Jet, and Large Missing Transverse*
792 *Momentum in Proton-Proton Collisions at $\sqrt{s} = 13$ TeV*, *Phys. Rev. Lett.* **124**(4),
793 041803 (2020), doi:10.1103/PhysRevLett.124.041803, 1910.01185.
- 794 [137] G. Aad *et al.*, *Search for direct stau production in events with two hadronic τ -leptons*
795 *in $\sqrt{s} = 13$ TeV pp collisions with the ATLAS detector*, *Phys. Rev. D* **101**(3), 032009
796 (2020), doi:10.1103/PhysRevD.101.032009, 1911.06660.
- 797 [138] G. Aad *et al.*, *Searches for electroweak production of supersymmetric particles with*
798 *compressed mass spectra in $\sqrt{s} = 13$ TeV pp collisions with the ATLAS detector*,
799 *Phys. Rev. D* **101**(5), 052005 (2020), doi:10.1103/PhysRevD.101.052005, 1911.
800 12606.
- 801 [139] G. Aad *et al.*, *Search for electroweak production of charginos and sleptons decaying*
802 *into final states with two leptons and missing transverse momentum in $\sqrt{s} = 13$*
803 *TeV pp collisions using the ATLAS detector*, *Eur. Phys. J. C* **80**(2), 123 (2020),
804 doi:10.1140/epjc/s10052-019-7594-6, 1908.08215.
- 805 [140] J. Kumar and D. Marfatia, *Matrix element analyses of dark matter scattering and*
806 *annihilation*, *Phys. Rev. D* **88**(1), 014035 (2013), doi:10.1103/PhysRevD.88.014035,
807 1305.1611.
- 808 [141] *Toward a next-generation dark matter search with the PICO-40L bubble chamber*,
809 https://indico.cern.ch/event/606690/contributions/2623446/attachments/1497228/2330240/Fallows_2017_07_24__TAUP__PICO-40L_v1.2.pdf, Accessed:
810 2021-03-24.
- 812 [142] D. S. Akerib *et al.*, *LUX-ZEPLIN (LZ) Conceptual Design Report* (2015), 1509.
813 02910.