# Dark matter, fine-tuning and $(g-2)_{\mu}$ in the pMSSM

M. van Beekveld<sup>1\*</sup>, W. Beenakker<sup>2</sup>, M. Schutten<sup>2,4</sup>, J. de Wit<sup>2</sup>

1 Rudolf Peierls Centre for Theoretical Physics, 20 Parks Road, Oxford OX1 3PU, United Kingdom

2 THEP, Radboud University, Heyendaalseweg 135, 6525 AJ Nijmegen, the Netherlands 3 Institute of Physics, University of Amsterdam, Science Park 904, 1018 XE Amsterdam,

the Netherlands

4 Van Swinderen Institute for Particle Physics and Gravity, University of Groningen, 9747 AG Groningen, The Netherlands

\* melissa.vanbeekveld@physics.ox.ac.uk

June 18, 2021

# <sup>1</sup> Abstract

In this paper we perform for the first time an in-depth analysis of the spectra in the phe-2 nomenological supersymmetric Standard Model that simultaneously offer an explanation 3 for the  $(g-2)_{\mu}$  discrepancy  $\Delta a_{\mu}$ , result in the right dark-matter relic density  $\Omega_{\rm DM}h^2$  and 4 are minimally fine-tuned. The resulting spectra may be obtained from [1]. To discuss 5 the experimental exclusion potential for our models, we analyse the resulting LHC phe-6 nomenology as well as the sensitivity of dark-matter direct detection experiments to these 7 spectra. We find that the latter type of experiments with sensitivity to the spin-dependent 8 dark-matter – nucleon scattering cross section  $\sigma_{\rm SD,p}$  will probe all of our found solutions. 9

10

# 11 Contents

12	1	Introduction	<b>2</b>
13	<b>2</b>	The muon anomalous magnetic moment and fine-tuning in the pMSSM	3
14		2.1 Electroweak fine-tuning in the pMSSM	4
15		2.2 The muon anomalous magnetic moment	5
16	3	Analysis setup	6
17	<b>4</b>	Phenomenology	6
18		4.1 LHC phenomenology for the funnel regimes	9
19		4.2 LHC phenomenology for the coannihilation regimes	11
20		4.3 LHC phenomenology for the bino-higgsino LSP	12
21		4.4 Dark-matter direct detection experiments	13
22	5	Conclusion	13
23	Re	eferences	14

25

## <sup>26</sup> 1 Introduction

The Large Hadron Collider (LHC) has been searching for over a decade for signs of physics 27 that originate from beyond-the-Standard-Model (BSM) scenarios, including searches for 28 signals that originate from supersymmetric (SUSY) particle production. These high-energy 29 searches are complemented by low-energy experiments such as dark-matter (DM) exper-30 iments, or experiments that search for small deviations in known Standard-Model (SM) 31 processes from their SM prediction. In the former category, the XENON1T [2,3], PandaX-32 II [4,5] and PICO [6–8] experiments provide limits on the DM-nucleus scattering cross 33 section, whereas the Planck collaboration provides a precise measurement of the DM relic 34 abundance [9]. In the latter category, the anomalous magnetic moment of the muon  $(q-2)_{\mu}$ 35 plays an important role. There is a long-standing discrepancy between the experimental 36 result [10–12] and the SM prediction for the muon anomalous magnetic moment. The 37 latter is composed of quantum-electrodynamic, weak, hadronic vacuum-polarization, and 38 hadronic light-by-light contributions, and reads [13–34] 39

$$a_{\mu}^{\rm SM} = \frac{(g-2)_{\mu}}{2} = 116\,591\,810(43) \times 10^{-11},$$
 (1)

 $_{40}$  where the value between parentheses represents the theoretical uncertainty. The improved

41 experimental results obtained at Fermilab [35–38], combined with the Brookhaven re-42 sult [10–12] read

$$a_{\mu}^{\exp} = 116\,592\,061(41) \times 10^{-11},\tag{2}$$

43 showing that the deviation is now

$$\Delta a_{\mu} = a_{\mu}^{\exp} - a_{\mu}^{SM} = 251(59) \times 10^{-11}.$$
(3)

An independent experiment with different techniques than those employed by the Fermilab
 experiment is being constructed at J-PARC [39,40].

The Minimal Supersymmetric Standard Model (MSSM) with *R*-parity conservation pre-46 dicts a DM candidate and can simultaneously provide an explanation for the  $(g-2)_{\mu}$ 47 discrepancy<sup>1</sup>. Furthermore, the MSSM provides a solution to the fine-tuning (FT) prob-48 lem in the Higgs sector that any BSM model introduces, even after taking into account 49 the constraints on colored sparticles originating from the LHC. It is clear that for a rich 50 model such as the MSSM, the interplay between the various experimental results is of 51 crucial importance. In this context, several studies have been performed to study a subset 52 of these constraints. For instance, the interplay between the LHC limits and the  $(g-2)_{\mu}$ 53 discrepancy has been studied in e.g. Ref. [42–49]. DM direct detection (DMDD) searches 54 are complementary in regions of the MSSM parameter space where the LHC has little 55 sensitivity, for example in compressed regions. Papers that explore the DM implications of 56 spectra that explain the  $(g-2)_{\mu}$  discrepancy include Refs. [48–53], where the relic density 57 requirement is not always taken into account. Likelihood analyses or global fits, where all 58 experimental data that constrain the MSSM parameter space are taken into account, have 59 been performed in e.g. Ref. [53–59]. The degree of FT in constrained models that explain 60 the  $(g-2)_{\mu}$  discrepancy is studied in [60, 61], whereas the role of FT in spectra with the 61 right DM properties is studied in Ref. [62–66]. 62

<sup>63</sup> In this work we perform for the first time a study of the phenomenology of the MSSM<sup>64</sup> that simultaneously accounts for the DM relic abundance and the observed discrepancy

<sup>&</sup>lt;sup>1</sup>A simultaneous explanation of the muon and electron anomalous magnetic moments in the MSSM context is provided in Ref. [41].

<sup>65</sup> of  $(g-2)_{\mu}$ , that includes all DMDD and LHC limits, and that constrains the model-<sup>66</sup> parameter space to models that are minimally fine-tuned. The resulting spectra may be <sup>67</sup> obtained from [1]. The paper is structured as follows. In Section 2 we introduce our nota-<sup>68</sup> tion, the muon anomalous magnetic moment and the electroweak fine-tuning measure. In <sup>69</sup> Section 3 we explain the set-up of our analysis. In Section 4 we explore the phenomenology <sup>70</sup> of the viable spectra, and in Section 5 we present our conclusions.

# <sup>71</sup> 2 The muon anomalous magnetic moment and fine-tuning in <sup>72</sup> the pMSSM

Instead of exploring the full MSSM with 105 free parameters, we focus on the phenomeno-73 logical MSSM (pMSSM) [67], which has 19 free parameters whose boundary conditions are 74 given at the SUSY scale of  $\mathcal{O}(1 \text{ TeV})$ . In this phenomenologically motivated pMSSM one 75 requires that the first and second generation squark and slepton masses are degenerate, 76 that the trilinear couplings of the first and second generation sfermions are set to zero 77 (leaving only those of the third generation,  $A_t$ ,  $A_b$  and  $A_{\tau}$ ), and that no new sources of 78 CP violation are introduced. In addition one assumes that all sfermion mass matrices are 79 diagonal. The sfermion soft-masses are then described by the first and second generation 80 squark masses  $m_{\widetilde{Q}_1}, m_{\widetilde{u}_R}$  and  $m_{\widetilde{d}_R}$ , the third generation squark masses  $m_{\widetilde{Q}_3}, m_{\widetilde{t}_R}$  and  $m_{\widetilde{b}_R}$ , the first and second generation of slepton masses  $m_{\widetilde{L}_1}$  and  $m_{\widetilde{e}_R}$ , and the third generation 81 82 of slepton masses  $m_{\tilde{L}_3}$  and  $m_{\tilde{\tau}_R}$ . The Higgs sector is described by the ratio of the Higgs 83 vacuum expectation values tan  $\beta$  and the soft Higgs masses  $m_{H_u}$  and  $m_{H_d}$ . Instead of 84 these parameters, it is customary to use the higgsino mass parameter  $\mu$  and the mass  $m_A$ 85 of the pseudoscalar Higgs boson as free parameters. The gaugino sector consists of the 86 bino (B), wino (W) and gluino with their mass parameters  $M_1(=|M_1|), M_2(=|M_2|)$  and 87  $M_3(=|M_3|).$ 88

As a result of electroweak symmetry breaking (EWSB), the gaugino and the higgsino in-89 teraction eigenstates mix into mass eigenstates, called neutralinos and charginos. The 90 neutralinos, denoted by  $\tilde{\chi}_i^0$  with  $i = 1, \ldots, 4$ , are the neutral mass eigenstates of the bino, 91 wino and higgsino interaction eigenstates. The neutralinos are ordered by increasing mass, 92 with  $\tilde{\chi}_1^0$  the lightest neutralino. Given the constraints from DMDD experiments on sneu-93 trino DM, we take the lightest neutralino as lightest-supersymmetric particle (LSP), which 94 makes it our DM candidate. Depending on the exact values of  $M_1$ ,  $M_2$  and  $|\mu|$ , this lightest 95 mass eigenstate can be mostly bino-like (if  $M_1$  is smallest), wino-like (if  $M_2$  is smallest) 96 or higgsino-like (if  $|\mu|$  is smallest). The amount of bino, wino and higgsino mixing of the 97 lightest neutralino is given by  $N_{11}$ ,  $N_{12}$  and  $\sqrt{N_{13}^2 + N_{14}^2}$ , where  $N_{ij}$  are the entries of the 98 matrix that diagonalizes the neutralino mass matrix. In the basis of  $(\widetilde{B}, \widetilde{W}^0, \widetilde{H}^0_d, \widetilde{H}^0_u)$ , this 99 mass matrix is given by 100

$$M_{\tilde{\chi}^{0}} = \begin{pmatrix} M_{1} & 0 & -c_{\beta}s_{\theta_{W}}M_{Z} & s_{\beta}s_{\theta_{W}}M_{Z} \\ 0 & M_{2} & c_{\beta}c_{\theta_{W}}M_{Z} & -s_{\beta}c_{\theta_{W}}M_{Z} \\ -c_{\beta}s_{\theta_{W}}M_{Z} & c_{\beta}c_{\theta_{W}}M_{Z} & 0 & -\mu \\ s_{\beta}s_{\theta_{W}}M_{Z} & -s_{\beta}c_{\theta_{W}}M_{Z} & -\mu & 0 \end{pmatrix},$$
(4)

with  $s_x \equiv \sin x$ ,  $c_x \equiv \cos x$ , and the ratio of the SM W- and Z-boson masses being denoted by  $\cos \theta_W = M_W/M_Z$ .

<sup>103</sup> The charginos, denoted by  $\tilde{\chi}_i^{\pm}$  with i = 1, 2, are the charged mass eigenstates of the <sup>104</sup> wino and higgsino interaction eigenstates, with  $\tilde{\chi}_1^{\pm}$  the lightest chargino. In the basis of 105  $(\widetilde{W}^{\pm}, \widetilde{H}^{\pm}_{u/d})$ , their mass matrix at tree level reads

$$M_{\tilde{\chi}^{\pm}} = \begin{pmatrix} M_2 & \sqrt{2}c_{\beta}c_{\theta_W}M_Z \\ \sqrt{2}s_{\beta}c_{\theta_W}M_Z & \mu \end{pmatrix} .$$
(5)

The composition of the lightest chargino is predominantly higgsino when  $|\mu| < M_2$ , predominantly wino when  $M_2 < |\mu|$ , or a mixture when the two gaugino parameters are close in value.

#### <sup>109</sup> 2.1 Electroweak fine-tuning in the pMSSM

The EWSB conditions link  $M_Z$  to the input parameters via the minimization of the scalar potential of the Higgs fields. The resulting equation at one loop is [68, 69]

$$\frac{M_Z^2}{2} = \frac{m_{H_d}^2 + \Sigma_d^d - (m_{H_u}^2 + \Sigma_u^u) \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2, \qquad (6)$$

where the two effective potential terms  $\Sigma_u^u$  and  $\Sigma_d^d$  denote the one-loop corrections to 112 the soft SUSY breaking Higgs masses (explicit expressions are shown in the appendix of 113 Ref. [69]). In order to obtain the observed value of  $M_Z = 91.2$  GeV, one needs some degree 114 of cancellation between the SUSY parameters appearing in Eq. (6). If small relative changes 115 in the SUSY parameters will result in a distinctly different value of  $M_Z$ , the considered 116 spectrum is said to be fine-tuned, as then a large degree of cancellation is needed to obtain 117 the right value of  $M_Z$ . FT measures aim to quantify this sensitivity of  $M_Z$  to the SUSY 118 input parameters. 119

The electroweak (EW) FT measure [70,71] is an agnostic approach to the computation of 120 fine-tuning. We take this approach because a generic broken minimal SUSY theory has 121 two relevant energy scales: a high-scale one at which SUSY breaking takes place, and a 122 low-scale one  $(M_{SUSY})$  where the resulting SUSY particle spectrum is situated and the 123 EWSB conditions must be satisfied. We do not know which and how many fundamental 124 parameters exist for a possible high-scale theory. The EW FT measure does not take such 125 underlying high-scale model assumptions into account for its computation. The EW FT 126 measure  $(\Delta_{\rm EW})$  parameterizes how sensitive  $M_Z$  is to variations in each of the coefficients 127  $C_i$ , which are evaluated at  $M_Z$ . It is defined as 128

$$\Delta_{\rm EW} \equiv \max_{i} \left| \frac{C_i}{M_Z^2/2} \right|,\tag{7}$$

129 where the  $C_i$  are

$$C_{m_{H_d}} = \frac{m_{H_d}^2}{\tan^2 \beta - 1}, \quad C_{m_{H_u}} = \frac{-m_{H_u}^2 \tan^2 \beta}{\tan^2 \beta - 1}, \quad C_{\mu} = -\mu^2,$$
$$C_{\Sigma_d^d} = \frac{\max(\Sigma_d^d)}{\tan^2 \beta - 1}, \quad C_{\Sigma_u^u} = \frac{-\max(\Sigma_u^u) \tan^2 \beta}{\tan^2 \beta - 1}.$$

The tadpole contributions  $\Sigma_u^u$  and  $\Sigma_d^d$  contain a sum of different contributions. These contributions are computed individually and the maximum contribution is used to compute the  $C_{\Sigma_u^u}$  and  $C_{\Sigma_d^d}$  coefficients. We will use an upper bound of  $\Delta_{\rm EW} < 100$  (implying no worse than  $\mathcal{O}(1\%)$  fine-tuning on the mass of the Z-boson) to determine whether a given set of MSSM parameters is fine-tuned, and use the code from Ref. [64] to compute the measure.

136 Using this measure, one generically finds that minimally fine-tuned scenarios have low

values for  $|\mu|$ , where  $\Delta_{\rm EW} = 100$  is reached at  $|\mu| \simeq 800$  GeV [64, 66, 70, 72–76]. The masses of the gluino, sbottom, stop and squarks are allowed to get large for models with low  $\Delta_{\rm EW}$  [65, 77, 78]. Therefore, we assume that the masses of these sparticles are above 2.5 TeV (for the gluino), above 1.2 TeV (for the stops and bottoms) and above 2 TeV (for the squarks), such that they evade the ATLAS and CMS limits <sup>2</sup>.

#### <sup>142</sup> 2.2 The muon anomalous magnetic moment

In the pMSSM, one-loop contributions to  $a_{\mu}$  arise from diagrams with a chargino-sneutrino or neutralino-smuon loop [79]. The expressions for these one-loop corrections read [80]

$$\delta a_{\mu}^{\tilde{\chi}^{0}} = \frac{m_{\mu}}{16\pi^{2}} \sum_{i=1}^{4} \sum_{m=1}^{2} \left[ -\frac{m_{\mu}}{12m_{\tilde{\mu}_{m}}^{2}} \left( |n_{im}^{L}|^{2} + |n_{im}^{R}|^{2} \right) F_{1}^{N} \left( \frac{m_{\tilde{\chi}_{i}^{0}}^{2}}{m_{\tilde{\mu}_{m}}^{2}} \right) + \frac{m_{\tilde{\chi}_{i}^{0}}}{3m_{\tilde{\mu}_{m}}^{2}} \operatorname{Re}\left[ n_{im}^{L} n_{im}^{R} \right] F_{2}^{N} \left( \frac{m_{\tilde{\chi}_{i}^{0}}^{2}}{m_{\tilde{\mu}_{m}}^{2}} \right) \right],$$

$$\delta a_{\mu}^{\tilde{\chi}^{\pm}} = \frac{m_{\mu}}{16\pi^{2}} \sum_{k=1}^{2} \left[ \frac{m_{\mu}}{12m_{\tilde{\nu}_{\mu}}^{2}} \left( |c_{k}^{L}|^{2} + |c_{k}^{R}|^{2} \right) F_{1}^{C} \left( \frac{m_{\tilde{\chi}_{k}^{\pm}}^{2}}{m_{\tilde{\nu}_{\mu}}^{2}} \right) + \frac{2m_{\tilde{\chi}_{k}^{\pm}}}{3m_{\tilde{\nu}_{\mu}}^{2}} \operatorname{Re}\left[ c_{k}^{L} c_{k}^{R} \right] F_{2}^{C} \left( \frac{m_{\tilde{\chi}_{k}^{\pm}}^{2}}{m_{\tilde{\nu}_{\mu}}^{2}} \right) \right]$$

$$(8)$$

with  $m_{\mu}$  the muon mass,  $m_{\tilde{\mu}_m}$  the first or second smuon mass,  $m_{\tilde{\nu}_{\mu}}$  the muon sneutrino mass, *i*, *m* and *k* the indices for the neutralinos, smuons and charginos and the couplings

$$n_{im}^{R} = \sqrt{2}g_{1}N_{i1}X_{m2} + y_{\mu}N_{i3}X_{m1}, \qquad n_{im}^{L} = \frac{1}{\sqrt{2}}\left(g_{2}N_{i2} + g_{1}N_{i1}\right)X_{m1}^{*} - y_{\mu}N_{i3}X_{m2}^{*}(10)$$

$$c_{k}^{R} = y_{\mu}U_{k2}, \qquad c_{k}^{L} = -g_{2}V_{k1}. \qquad (11)$$

The down-type muon Yukawa coupling is denoted by  $y_{\mu} = g_2 m_{\mu}/(\sqrt{2}M_W \cos\beta)$ , and the SU(2) and U(1) gauge couplings are  $g_2$  and  $g_1$ . The matrices N and U, V diagonalize the neutralino and chargino mass matrices (Eq. (4), (5)), while the unitary matrix Xdiagonalizes the smuon mass matrix  $M_{\tilde{\mu}}^2$ , which reads for the pMSSM in the  $(\tilde{\mu}_L, \tilde{\mu}_R)$  basis

$$M_{\tilde{\mu}}^2 = \begin{pmatrix} m_{\tilde{L}_1}^2 + \left(s_{\theta_W}^2 - \frac{1}{2}\right) M_Z^2 \cos(2\beta) & -m_{\mu}\mu \tan\beta \\ -m_{\mu}\mu \tan\beta & m_{\tilde{e}_R}^2 - s_{\theta_W}^2 M_Z^2 \cos(2\beta) \end{pmatrix}.$$
 (12)

The loop functions  $F_{1,2}^N$  and  $F_{1,2}^C$  can be found in Ref. [80]. They are normalized such that  $F_{1,2}^{N,C}(x=1) = 1$ , and go to zero for  $x \to \infty$ .

At two-loop, the numerical values of the various contributions differ considerably. The photonic Barr-Zee diagrams are the source of the largest possible two-loop contribution. Here a Higgs boson and a photon connect to either a chargino or sfermion loop [81]<sup>3</sup>.

As one can see in the expressions above, the chargino-sneutrino and neutralino-smuon contributions are controlled by  $M_1$ ,  $M_2$ ,  $\tan \beta$  and  $\mu$  (through  $m_{\tilde{\chi}_i^0}$  and  $m_{\tilde{\chi}_k^\pm}$ ), as well as  $m_{\tilde{L}_1}$  and  $m_{\tilde{e}_R}$  (through  $m_{\tilde{\mu}_m}$  and  $m_{\tilde{\nu}_{\mu}}$ ). They are enhanced when  $\tan \beta$  grows large and when simultaneously light ( $\mathcal{O}(100)$  GeV) neutralinos/charginos and smuons/sneutrinos exist in the sparticle spectrum. The Barr-Zee diagrams are enhanced by large values of  $\tan \beta$ , small values of  $m_A$  and large Higgs-sfermion couplings. In general, the one-loop chargino-sneutrino contribution dominates over the neutralino-slepton contribution [80],

 $<sup>^{2}</sup>$ Note that those limits are shown to be significantly less stringent for MSSM spectra with rich sparticle decays, see e.g. Ref. [59].

 $<sup>^{3}</sup>$ Two-loop corrections from sfermion loops contribute with a few percent here as well, since we assume heavy squark masses [82,83].

unless there is a large smuon left-right mixing induced by a sizable value for  $\mu$  [84]. These latter spectra will however result in slightly higher FT values, which is a direct consequence of a higher value of  $|\mu|$ .

## <sup>167</sup> 3 Analysis setup

To create the SUSY spectra we use SOFTSUSY 4.0 [85], the Higgs mass is calculated using 168 FeynHiggs 2.14.2 [86–90], and SUSYHIT [91] is used to calculate the decay of the SUSY 169 and Higgs particles. Vevacious [92–94] is used to check that the models have at least a 170 meta-stable minimum state that has a lifetime that exceeds that of our universe and that 171 this state is not color/charge breaking<sup>4</sup>. We use SUSY-AI [95] and SMODELS [96–100] 172 to determine the LHC exclusion of a model point. LHC cross sections for sparticle pro-173 duction at NLO accuracy are calculated using Prospino [101]. HIGGSBOUNDS 5.1.1 is 174 used to determine whether the SUSY models satisfy the LEP, Tevatron and LHC Higgs 175 constraints [102–109]. MICROMEGAS 5.2.1 [110–115] is used to compute the DM relic 176 density  $(\Omega_{\rm DM}h^2)$ , the present-day velocity-weighted annihilation cross section  $(\langle \sigma v \rangle)$  and 177 the spin-dependent and spin-independent dark-matter-nucleon scattering cross sections 178  $(\sigma_{\rm SD,p} \text{ and } \sigma_{\rm SL,p})$ . For DM indirect detection we only consider the limit on  $\langle \sigma v \rangle$  stemming 179 from the observation of gamma rays originating from dwarf galaxies, which we implement 180 as a hard cut on each of the channels reported on the last page of Ref. [116]. The current 181 constraints on the dark-matter – nucleon scattering cross sections originating from various 182 dark matter direct detection (DMDD) experiments are determined via MICROMEGAS, 183 while future projections of constraints are determined via DDCALC 2.0.0 [117]. Flavor 184 observables are computed with SuperIso 4.1 [118, 119]. The muon anomalous magnetic 185 moment and its theoretical uncertainty is determined including two-loop corrections and 186  $\tan \beta$  resummation with GM2Calc [82, 120–122]. 187

We use the Gaussian particle filter [123] to search the pMSSM parameter space for in-188 teresting areas. The lightest SM-like Higgs boson is required to be in the mass range of 189 122 GeV  $\leq m_h \leq 128$  GeV. Spectra that do not satisfy the LHC bounds on sparticle 190 masses, branching fractions of B/D-meson decays, the DMDD, or DM indirect detection 191 bounds are removed. Our spectra are furthermore required to satisfy the LEP limits on 192 the masses of the charginos, light sleptons and staus  $(m_{\tilde{\chi}_1^{\pm}} > 103.5 \text{ GeV}, m_{\tilde{l}^{\pm}} > 90 \text{ GeV})$ 193 and  $m_{\tilde{\tau}^{\pm}} > 85$  GeV) [124,125], and the constraints on the invisible and total width of the 194 Z-boson ( $\Gamma_{Z,inv} = 499.0 \pm 1.5$  MeV and  $\Gamma_Z = 2.4952 \pm 0.0023$  GeV) [126]. The spectra 195 surviving all constraints are available via [1]. 196

# <sup>197</sup> 4 Phenomenology

The main experimental constraints on our models that explain the  $(g-2)_{\mu}$  discrepancy 198  $\Delta a_{\mu}$  come from DMDD experiments and the LHC. To understand which spectra are still 199 viable it is crucial to understand the phenomenology of them, since the experimental ex-200 clusion power varies depending on the composition of the neutralinos and charginos. In 201 this section, we therefore take a look at the different scenarios and contributing compo-202 sitions, and describe in detail the properties of these spectra. Knowing these properties 203 is also relevant for considering future experimental setups, e.g. for LHC studies where the 204 exclusion power heavily depends on the assumed model. 205

<sup>&</sup>lt;sup>4</sup>These scenarios appear in the  $(g-2)_{\mu}$  context for large  $\mu \tan \beta$ , see e.g. Ref. [84].



Figure 1: The mass of the DM particle  $(m_{\tilde{\chi}_1^0})$  vs the velocity-weighted annihilation cross section  $(\langle \sigma v \rangle)$ . The value of  $\Delta_{\rm EW}$  is shown as a color code on the left, where the points are ordered such that spectra with lower values of  $\Delta_{\rm EW}$  lie on top of those with higher values of  $\Delta_{\rm EW}$ . On the right we show the dominant early-universe annihilation process that contributes to the value of  $\Omega_{\rm DM}h^2$ . In both plots, we only show points that satisfy all experimental constraints, and have  $133 \times 10^{-11} < \Delta a_{\mu} < 369 \times 10^{-11}$ , allowing for a  $2\sigma$  uncertainty.

We first discuss the DM phenomenology of the LSP. We assume that the DM abundance 206 is determined by thermal freeze-out and require that the lightest neutralino saturates 207  $\Omega_{\rm DM}h^2$  with the observed value of 0.12 [9] within 0.03 to allow for a theoretical uncer-208 tainty on the relic-density calculation. As explained above, the mass eigenstate of the 209 DM particle is a mixture of bino, wino and higgsino interaction eigenstates. To obtain 210 the correct relic density in the pMSSM with a pure state, one can either have a higgsino 211 with a mass of  $m_{\tilde{\chi}_1^0} \simeq 800$  GeV or a wino with  $m_{\tilde{\chi}_1^0} \simeq 2.5$  TeV. Spectra that saturate the 212 relic density with lower DM masses necessarily are predominantly bino-like, mixed with 213 higgsino/wino components. Negligible higgsino/wino components are found in so-called 214 funnel regions [127, 128], i.e. regions where the mass of the DM particle is roughly half of 215 the mass of the Z boson, SM-like Higgs boson or heavy Higgs boson. In such a scenario, 216 the mass of the neutralino can even get below 100 GeV with  $M_1 < 100$  GeV, and in par-217 ticular the early-universe DM annihilation cross section is enhanced for  $m_{\tilde{\chi}_1^0} \simeq m_h/2$  and 218  $M_Z/2$ . Moreover, spectra with another particle close in mass to the LSP can satisfy the 219 relic density constraint without having a large wino/higgsino component too, due to the 220 co-annihilation mechanism [129]. 221

Requiring minimally fine-tuned spectra removes two types of solutions where the DM 222 relic density constraint is satisfied. Firstly, the case where the lightest neutralino is pre-223 dominantly wino-like results in a fine-tuned spectrum: to obtain the right relic density 224  $M_2 \simeq 2.5$  TeV for a pure wino, so  $|\mu| > 2.5$  TeV in that scenario. Note that such high LSP 225 neutralino masses also do not give a large enough contribution to  $\Delta a_{\mu}$ , since the other 226 sparticle masses have to exceed this LSP mass. Secondly, the pure-higgsino solutions that 227 satisfy the relic density constraint need a high value of  $|\mu|$  and therefore also result in a 228 fine-tuned spectrum. In addition, they do not allow for an explanation of  $\Delta a_{\mu}$  [52] either. 229 Therefore we will see that our solutions feature predominantly bino-like LSPs. Due to the 230 combined  $\Delta a_{\mu}$  constraint (requiring high tan  $\beta$ ), DMDD limits and the FT requirement, 231 the composition has a small higgsino component (< 20%) and a negligible wino compo-232 nent. 233

234

On the left-hand side of Fig. 1 we show the spectra that survive all constraints and have  $\Delta_{\rm EW} < 100$ . Lower values for  $\Delta_{\rm EW}$  are generally found for lower DM masses. The mass



**Figure 2:** The mass of the DM particle  $(m_{\tilde{\chi}_1^0})$  vs the velocity-weighted annihilation cross section  $(\langle \sigma v \rangle)$ . The same points as in Fig. 1 are shown, but split out individually for each early-universe annihilation process.

of the DM particle does not exceed 500 GeV, which is a direct result of the combined requirements of having  $\Delta_{\rm EW} < 100$  and a sufficiently high contribution to  $\Delta a_{\mu}$ . The lowest-obtained value is  $\Delta_{\rm EW} = 12.3$ . From the right-hand side of Fig. 1, we can distinguish three different type of DM early-universe annihilation mechanisms: the funnel regions, the coannihilation regions and the bino-higgsino solution (indicated with  $b\bar{b}$  and  $t\bar{t}$ ). For clarity we show in Fig. 2 the same plot split out per annihilation channel, where it clearly can be seen that for example the  $t\bar{t}$  and  $b\bar{b}$  annihilation regimes overlap.

Before discussing the phenomenology of each of these regions in more detail, we first discuss 244 the compositions of the LSP, the second-to-lightest neutralino and the lightest chargino. 245 As anticipated in the previous section, and as shown in Fig. 3, we find that the LSP is 246 predominantly bino-like and has a small higgsino component. Larger higgsino components 247 are generally found for spectra that show larger values of  $\langle \sigma v \rangle$ . The second-to-lightest 248 neutralino and the lightest chargino are either wino-like, higgsino-like, or mixed wino-249 higgsino states. It might be surprising to read that spectra with bino-higgsino LSPs are 250 allowed to have wino-like  $\tilde{\chi}_2^0/\tilde{\chi}_1^{\pm}$ , as one would expect that in general these sparticles would 251 be predominantly higgsino-like. Such configurations can however be found in spectra for 252 which  $M_1$ ,  $M_2$  and  $|\mu|$  are all of  $\mathcal{O}(100)$  GeV with  $M_2$  being smaller than  $|\mu|$ , and that 253 have moderate to large values of  $\tan \beta$  (10  $\lesssim \tan \beta \lesssim$  20). From Eq. (4) one may infer that 254 for such spectra, little mixing can take place between the bino and wino. This results in 255 negligible wino components of the LSP, whereas  $\tilde{\chi}_1^{\pm}$  and  $\tilde{\chi}_2^0$  can be predominantly wino-256 like. Moreover, decreasing  $|\mu|$  for such models will not only result in a higher higgsino-257 component of the LSP, but counter-intuitively also in a higher wino component, while the 258 wino component of  $\tilde{\chi}_1^{\pm}$  and  $\tilde{\chi}_2^0$  then *decreases*. The composition of the  $\tilde{\chi}_1^{\pm}$  and  $\tilde{\chi}_2^0$  sparticles 259 is relevant for the LHC phenomenology, as those spectra where these are predominantly 260 higgsino-like are typically difficult to probe at the LHC due to low production cross sections 261 compared to the pure wino  $\tilde{\chi}_1^{\pm}/\tilde{\chi}_2^0$  case. 262

In what follows, we will explore the DM phenomenology of each of these regimes in some more detail (Section 4.1-4.3). We also discuss their LHC phenomenology, and explain why our solutions elude the LHC constraints. This allows us to identify gaps in the LHC search



Figure 3: The mass of the DM particle  $(m_{\tilde{\chi}_1^0})$  vs the velocity-weighted annihilation cross section  $(\langle \sigma v \rangle)$ . The composition of the LSP is shown as a color code, with the bino component  $|N_{11}|$  indicated on the left, the wino component  $|N_{12}|$  in the middle, and the higgsino component  $\sqrt{N_{13}^2 + N_{14}^2}$  on the right.



**Figure 4:** The mass difference between the DM particle and the lightest chargino (left), lightest smuon (middle) and lightest stau (right) versus the mass of the heavier particle. The color code represents the dominant early-universe annihilation channel.

program for supersymmetric particles. We end our discussion on the phenomenology of the found solutions by discussing the sensitivity of DMDD experiments in Section 4.4.

### <sup>263</sup> 4.1 LHC phenomenology for the funnel regimes

We start with discussing the DM phenomenology of the funnel regions, of which there 269 are two in our spectra <sup>5</sup>. The first one centers around  $m_{\tilde{\chi}_{1}^{0}} \simeq 40$  GeV, which is slightly 270 less than  $M_Z/2$ . This can be explained as follows. The velocities of the DM particles 271 were much higher in the early universe than what they are in the present-day universe. 272 This means that DM annihilations via s-channel Z exchanges could happen on-resonance 273 in the early universe, whereas in the present-day universe these exchanges only happen 274 off-resonance. This also explains the fact that the value for  $\langle \sigma v \rangle$  is allowed to get orders 275 of magnitude smaller than the value that one usually expects for a thermal relic (around 276  $\langle \sigma v \rangle = 3 \cdot 10^{-26} \,\mathrm{cm^3 s^{-1}}$  for a DM mass of 100 GeV). These models are characterized by small 277 wino/higgsino components of the LSP - otherwise the early-universe annihilation would be 278 too efficient, resulting in a too-low value of  $\Omega_{\rm DM}h^2$ . The second funnel region is centered 279 around  $m_{\tilde{v}_{1}^{0}} \simeq 60$  GeV, slightly less than  $m_{h}/2$ . These DM particles annihilated in the early 280 universe predominantly via s-channel SM-like Higgs exchanges. No solutions are found 281 for spectra with DM masses in-between the two funnel regions. Here, the wino/higgsino 282

 $<sup>^{5}</sup>$ The heavy Higgs funnel is not identified here, and will be left for future study.

component necessarily needs to increase to satisfy the  $\Omega_{\rm DM}h^2$  requirement, and these spectra are excluded by DMDD experiments. The minimal value of  $\Delta_{\rm EW}$  for these spectra is 13.2.

We now consider the compositions of  $\tilde{\chi}_1^0$ ,  $\tilde{\chi}_2^0$  and  $\tilde{\chi}_1^{\pm}$ , and identify the mass difference 286 between the LSP and the next-to-lightest SUSY particles in the funnel regimes, as this is 287 important to understand the LHC phenomenology of these regions. The two funnel regimes 288 are characterized by light ( $m_{\tilde{\chi}_1^0} < 100 \text{ GeV}$ ) bino-like LSPs. The  $\tilde{\chi}_1^{\pm}$  and  $\tilde{\chi}_2^0$  are degenerate in mass. They are wino mixtures for masses around 100 - 200 GeV, while they become 289 290 higgsino-like for heavier  $\tilde{\chi}_1^{\pm}/\tilde{\chi}_2^0$  (up to  $m_{\tilde{\chi}_1^{\pm}/\tilde{\chi}_2^0} \simeq 500$  GeV). The mass gap between  $\tilde{\chi}_1^0$  and 291  $\widetilde{\chi}_2^0$  or  $\widetilde{\chi}_1^{\pm}$   $(\Delta(m_{\widetilde{\chi}_2^0}, m_{\widetilde{\chi}_1^0})$  or  $\Delta(m_{\widetilde{\chi}_1^{\pm}}, m_{\widetilde{\chi}_1^0}))$  is at least around 50 GeV, and exceeds 100 GeV 292 for  $m_{\tilde{\chi}^{\pm}_{1}} \gtrsim 150$  GeV (see Fig. 4, left panel). The masses of the sleptons are heavier than 293 (at least) the masses of  $\tilde{\chi}_2^0$  and  $\tilde{\chi}_1^{\pm}$ . 294

- Three different sorts of decays for  $\tilde{\chi}_2^0$  can be identified that are relevant final-state topologies for LHC searches:
- 297 1.  $\widetilde{\chi}_2^0 \to h \widetilde{\chi}_1^0$  when  $\Delta(m_{\widetilde{\chi}_2^0}, m_{\widetilde{\chi}_1^0}) > m_h$ ,

298 2. 
$$\widetilde{\chi}_2^0 \to Z \widetilde{\chi}_1^0$$
 when  $\Delta(m_{\widetilde{\chi}_2^0}, m_{\widetilde{\chi}_1^0}) > M_Z$ ,

299 3. off-shell decays when  $\Delta(m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_1^0}) < M_Z$ .

For  $\tilde{\chi}_1^{\pm}$ , there are only two sorts of decays

301 1. 
$$\widetilde{\chi}_1^{\pm} \to W^{\pm} \widetilde{\chi}_1^0$$
 when  $\Delta(m_{\widetilde{\chi}_1^{\pm}}, m_{\widetilde{\chi}_1^0}) > M_W$ ,

302 2. off-shell decays when 
$$\Delta(m_{\tilde{\chi}_1^{\pm}}, m_{\tilde{\chi}_1^0}) < M_W$$
.

We now determine why our points in the funnel region survive the LHC constraints. Given 303 that the sleptons in these spectra are heavier than  $\tilde{\chi}_2^0$  and  $\tilde{\chi}_1^{\pm}$ , searches for  $\tilde{\chi}_2^0 \tilde{\chi}_1^{\pm}$  production 304 with on-shell decays of  $\tilde{\chi}_2^0 \to Z \tilde{\chi}_1^0$ , such as those in Ref. [130–133], are most sensitive to 305 our spectra. However, whenever  $\Delta(m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_1^0}) > m_h$ , we find that in our models there 306 exists a mixture between  $\tilde{\chi}_2^0 \to h \tilde{\chi}_1^0$  and  $\tilde{\chi}_2^0 \to Z \tilde{\chi}_1^0$  decays. This is part of the reason 307 why our models evade the LHC limits: the sensitivity of the experiments drops when  $\tilde{\chi}_2^0$ 308 can decay into the SM-like Higgs boson [131, 134]. A second reason why these spectra 309 evade the LHC limits is that the simplified limits of the searches mentioned above assume 310 a wino-like  $\tilde{\chi}_2^0 \tilde{\chi}_1^{\pm}$  pair, whereas we deal with mixed wino-higgsino pairs. To interpret the 311 above-mentioned analyses, we show in the left panel of Fig. 5 the average cross section per 312 10 by 10 GeV bin for  $\tilde{\chi}_2^0 \tilde{\chi}_1^{\pm}$  production. We determined whether a given model point is 313 excluded by parameterizing the upper bounds on the cross sections as shown in Ref. [132], 314 Fig. 7 and 8, Ref. [131], Fig. 11 and Ref. [133], Fig. 5 and 6. We find that our cross sections 315 in the regime where  $M_Z < \Delta(m_{\tilde{\chi}_0^0}, m_{\tilde{\chi}_1^0}) < m_h$  do no not exceed the 95% confidence level 316 (CL) limits. We expect this situation to change if more LHC data is collected, making the 317 LHC sensitive to this part of the funnel parameter space. The models with off-shell decays 318 are slightly more constrained by the current results of the LHC experiments. Particularly 319 Ref. [133] excludes some of our spectra in this regime that have  $m_{\tilde{\chi}_1^{\pm}}$  up to 210 GeV and 320  $\Delta(m_{\tilde{\chi}^0_1}, m_{\tilde{\chi}^0_1}) < 55$  GeV. These spectra are explicitly removed from the plots. The LHC 321 shows limited sensitivity to the models in the mass range of 55 GeV  $< \Delta(m_{\tilde{\chi}_1^{\pm}}, m_{\tilde{\chi}_1^0}) < M_Z$ . 322 To gain full sensitivity to the funnel regions, this mass range is an important domain to 323 cover in the LHC searches. 324



**Figure 5:** The mass of the DM particle versus the mass of the lightest chargino (left) and smuon (right), combined in 10 by 10 GeV bins. The average production cross section of  $\sigma_{pp\to\tilde{\chi}_{2}^{0}\tilde{\chi}_{1}^{\pm}}$  (left) and  $\sigma_{pp\to\tilde{l}_{1}^{\pm}\tilde{l}_{1}^{\mp}}$  (right) is shown in color code for each bin. The dashed black line in the plot on the left-hand side shows the limit where  $m_{\tilde{\chi}_{1}^{0}} = m_{\tilde{\chi}_{1}^{\pm}}$ , whereas the gray dashed (dotted) lines show  $m_{\tilde{\chi}_{1}^{\pm}} = m_{\tilde{\chi}_{1}^{0}} + M_{Z}$   $(m_{\tilde{\chi}_{1}^{\pm}} = m_{\tilde{\chi}_{1}^{0}} + m_{h})$ . The dashed black line in the plot on the right-hand side shows  $m_{\tilde{\chi}_{1}^{0}} = m_{\tilde{\chi}_{1}^{0}} + m_{h}$ ).

#### 325 4.2 LHC phenomenology for the coannihilation regimes

The second regime is the coannihilation regime, whose DM phenomenology we now discuss. 326 It starts to open up at DM masses of roughly 75 GeV, as no charged sparticles (and 327 therefore no coannihilation partners other than the sneutrino) can exist with masses below 328 85 GeV due to the LEP/LHC bounds. Three different types of coannihilation partners 329 are identified: first-/second-generation sleptons, third-generation sleptons, and charginos 330 or heavier neutralinos. Interestingly, only with the help of slepton coannihilations the 331 DM particle can have a mass between  $\mathcal{O}(70 - 150)$  GeV and still give the right  $\Omega_{\rm DM}h^2$ . 332 To obtain the right relic density in this regime without a slepton-coannihilation partner, 333 one generally needs high higgsino fractions, which increases the value of  $\sigma_{SLp}$  beyond 334 the exclusion limit of the DMDD experiments. The lowest values of  $\Delta_{\rm EW}$  are found in 335 the stau-coannihilation regime ( $\Delta_{\rm EW} = 12.3$ ), while the first-/second-generation slepton 336 and chargino/neutralino regimes result in lowest values  $\Delta_{\rm EW} = 14.4$  and  $\Delta_{\rm EW} = 16.4$ 337 respectively. The coannihilation regimes are all characterized by small mass differences 338 between the LSP and its coannihilation partner(s). 339

The first type of coannihilation is that of first-/second-generation sleptons  $(l_1^{\pm})$ . The 340 compression between  $m_{\tilde{\chi}^{\pm}}$  and  $m_{\tilde{\chi}^{0}}$  is increased for higher LSP masses such that the right 341  $\Omega_{\rm DM}h^2$  can still be obtained. By computing the production cross section (see Fig. 5), 342 and comparing these to the results of Fig. 20 of Ref. [134], we see that spectra with 343  $\Delta(m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_1^0}) > M_Z$  are under strong constraints from searches for  $\tilde{\chi}_2^0 \tilde{\chi}_1^{\pm} \to l l \nu_l$ . We 344 explicitly remove those points from our data, leaving only models with  $\Delta(m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_1^0}) < M_Z$ . 345 The  $\tilde{\chi}_1^{\pm}$  and  $\tilde{\chi}_2^0$  sparticles of the surviving models are typically higgsino-like with a small 346 wino component, and have masses between 180 and 500 GeV. 347

The second coannihilation regime is characterized by low  $\tilde{\tau}_1^{\pm}$  masses. The masses of  $\tilde{\chi}_1^{\pm}/\tilde{\chi}_2^0$ can still be as light as 105 GeV in this regime, where they are predominantly wino-like. The higgsino component of these particles increases when their masses increase, up to  $m_{\tilde{\chi}_1^{\pm}/\tilde{\chi}_2^0} \simeq 500$  GeV. Although we have a large production cross section for the wino-like  $\tilde{\chi}_1^{\pm}/\tilde{\chi}_2^0$  pair, these models are not constrained by the LHC experiments due to the presence of the light staus. The staus are often lighter than  $\tilde{\chi}_1^{\pm}$  and  $\tilde{\chi}_2^0$ , and the searches for <sup>354</sup>  $\tilde{\tau}_1^{\pm}$ -mediated decays of  $\tilde{\chi}_1^+ \tilde{\chi}_1^- / \tilde{\chi}_1^{\pm} \tilde{\chi}_2^0$  production have no sensitivity when  $\Delta(m_{\tilde{\chi}_1^0}, m_{\tilde{\tau}_1^{\pm}}) <$ <sup>355</sup> 100 GeV [135, 136]. The latter holds for our spectra in the second coannihilation regime, <sup>356</sup> since the mass differences between the LSP and  $\tilde{\tau}_1^{\pm}$  are between 5 – 50 GeV in that case. <sup>357</sup> Additionally, relatively few LHC searches for low-mass  $\tilde{\tau}^{\pm}$  particles exist. Small  $\tilde{\tau}^+ \tilde{\tau}^-$ <sup>358</sup> production cross sections and low signal acceptances make these searches difficult, so the <sup>359</sup> experiments have no constraining power in the compressed regime [137, 138]. We suggest <sup>360</sup> a dedicated low mass  $\tilde{\tau}^{\pm}$  search without an assumed mass degeneracy between  $\tilde{\tau}_1^{\pm}$  and  $\tilde{\tau}_2^{\pm}$ <sup>361</sup> to probe the sensitivity of the LHC to these scenarios.

The last coannihilation regime has a  $\tilde{\chi}_1^{\pm}$  or  $\tilde{\chi}_2^0$  that is close in mass to the LSP. Interestingly, 362 although the mass compression for the slepton coannihilation regimes needs to increase to 363 obtain the right relic density for higher DM masses, for the gaugino-coannihilation regime 364 it needs to decrease instead. Regarding the LHC phenomenology, note that although the 365 slepton masses in these regions can be  $\mathcal{O}(200)$  GeV, the results from the  $l_{R,L}^+ l_{R,L}^-$  searches 366 with  $\tilde{l}^{\pm} = \tilde{e}^{\pm}, \tilde{\mu}^{\pm}$  or  $\tilde{\tau}^{\pm}$  (e.g. [138–140]) are not directly applicable here, as often one or 367 more of the chargino/heavier neutralino states is lighter than the sleptons. Therefore, the 368 slepton will not decay with a 100% branching ratio to  $\tilde{\chi}_1^0 l^{\pm}$ , although this is assumed 369 in the above-mentioned searches. Instead, in this regime, only the  $\tilde{\chi}_1^{\pm}\tilde{\chi}_2^0$  searches are of 370 relevance, similar to the case in the funnel region discussed above. The mass compression 371 between the LSP and wino-higgsino like  $\tilde{\chi}_1^{\pm}/\tilde{\chi}_2^0$  sparticles is generally around 15-20 GeV, 372 and Ref. [133] excludes our solutions with  $m_{\tilde{\chi}_1^{\pm}}$  up to 140 – 180 GeV. 373

### <sup>374</sup> 4.3 LHC phenomenology for the bino-higgsino LSP

The last regime we identify consists of bino-higgsino LSPs and is labeled with bb and  $t\bar{t}$ . 375 These early-universe annihilation channels are mediated by either s-channel Z or h/H ex-376 changes. The  $t\bar{t}$  annihilation channel opens up when  $m_{\tilde{\chi}_1^0}$  becomes larger than the mass 377 of the top quark  $m_t$ , as then the invariant mass of the two LSPs is enough to create a  $t\bar{t}$ 378 pair  $^{6}$ . For the Z-exchange channel this annihilation becomes favored over the annihilation 379 into a lighter fermion pair, since any Z-mediated annihilation of two Majorana fermions 380 is helicity suppressed at tree level [141]. This is explained as follows. The two identical 381 LSPs form a Majorana pair. Such a pair is even under the operation of charge-conjugation 382  $C = (-1)^{L+S}$  with S the total spin and L the total orbital angular momentum, so L and 383 S must either both be even, or both be odd. Taking the limit of zero velocity, as the 384 present-day velocity of DM particles is non-relativistic, we may assume L = 0 and even S. 385 The final-state fermion pair can have a total spin of S = 1 or S = 0, but only the latter is 386 allowed for the Majorana-pair annihilation in the non-relativistic limit. For a Dirac-field 387 pair, an S = 0 configuration is obtained if the fermion and anti-fermion are from different 388 Weyl spinors: a left- and right-handed one. In the SM, a coupling with this combination 389 only arises (at tree level) by a mass insertion. Therefore, the transition amplitude is pro-390 portional to the mass of the final-state fermions, and a decay to a heavier pair of fermions 391 is generally preferred. In spectra where  $\tan \beta$  is large we also see the heavy-Higgs-mediated 392 decays to bb, as the bottom-Yukawa coupling is enhanced. As can be seen in Fig. 4, in the 393 regime of  $m_{\tilde{\chi}_1^0} \gtrsim m_t$ , the masses of  $\tilde{\chi}_1^{\pm}$  and  $\tilde{\chi}_2^0$  are relatively close to that of the LSP, so 394 due to the coannihilation mechanism these spectra tend to show slightly lower values of 395  $\langle \sigma v \rangle$  than naively would be expected. 396

The minimal value of  $\Delta_{\rm EW}$  is around 14.2 for these models. The  $\tilde{\chi}_2^0$  and  $\tilde{\chi}_1^{\pm}$  are predominantly higgsino-like with masses from 180 to 500 GeV. Due to their small production cross section, the LHC searches do not have exclusion power in this regime.

<sup>&</sup>lt;sup>6</sup>The annihilation to a  $W^+W^-$  pair is possible when  $m_{\tilde{\chi}_1^0} > M_W$ . However, this is constrained by DMDD due to the high wino/higgsino fraction that is necessary for this channel.



Figure 6: Right (left): The mass of the DM particle versus the spin-(in)dependent cross section  $\sigma_{\rm SD,p}$  ( $\sigma_{\rm SI,p}$ ). The value of  $\Delta_{\rm EW}$  is shown in color code. We also show the projected PICO-40L and PICO-500 central limits on  $\sigma_{\rm SD,p}$  [142]. The points are ordered such that those with lower values of  $\Delta_{\rm EW}$  lie on top of those with higher values.

#### 400 4.4 Dark-matter direct detection experiments

In the previous subsections we discussed the phenomenology of the viable spectra at the 401 LHC. We now comment on the sensitivity of DMDD experiments. We have seen that the 402 LSP in our spectra is always bino-like with a small higgsino component (Fig. 3). We find 403 that the relative size of the wino component of the LSP is constraint by DMDD exper-404 iments: higher wino components result in larger values of  $\sigma_{SI,p}$  and  $\sigma_{SD,p}$ . Surprisingly, 405 this indirectly also places a lower bound on  $|\mu|$ : decreasing  $|\mu|$  for our models will not only 406 result in a higher higgsino-component, but also in a higher wino component of the LSP, as 407 more mixing between the wino and bino components is then allowed. Therefore, decreasing 408  $|\mu|$  for these scenarios is limited by the constraints imposed by the DMDD experiments. 409

The resulting values for  $\sigma_{SI,p}$  and  $\sigma_{SD,p}$  of the surviving models may be seen in Fig. 6. 410 While the value of  $\sigma_{SI,p}$  varies by over 7 orders of magnitude,  $\sigma_{SD,p}$  is relatively con-411 strained. We moreover observe that  $\sigma_{SD,p}$  is directly correlated with  $\Delta_{EW}$ : lower values of 412  $\sigma_{\rm SD,p}$  result in higher values of  $\Delta_{\rm EW}$ . The value of  $\sigma_{\rm SD,p}$  decreases with smaller higgsino 413 fractions in the LSP, while for a given fixed LSP mass  $\Delta_{\rm EW}$  increases since  $|\mu|$  needs to 414 increase. For this reason, future DMDD experiments that probe  $\sigma_{SD,p}$  will be sensitive to 415 all our solutions, irrespective of the masses and compositions of the rest of the sparticle 416 spectrum. In Fig. 6, we indicate the projected limit of the PICO-40L and the PICO-500 417 experiments [142]. We observe that the latter one is sensitive to all of our solutions with 418  $\Delta_{\rm EW} < 62$ . The LUX-ZEPLIN experiment [143] (whose projected limit is not shown in 419 Fig. 6) will probe all of our solutions with  $\Delta_{\rm EW} < 100$ . 420

## 421 5 Conclusion

In this paper we have analyzed the spectra in the pMSSM that are minimally fine-tuned, result in the right  $\Omega_{\text{DM}}h^2$  and simultaneously offer an explanation for  $\Delta a_{\mu}$ . We make these spectra publicly available under [1].

In terms of DM phenomenology, we have distinguished three interesting branches of solutions: the funnel regimes, three types of coannihilation regimes, and the generic binohiggsino solution. All these solutions have in common that the LSP is predominantly

bino-like with a small higgsino component. Masses of the DM particle range between 428 39 - 495 GeV. We discussed the phenomenology at the LHC for each of the regimes. The 429 first and second regime are relatively more constrained by  $\tilde{\chi}_2^0 \tilde{\chi}_1^{\pm}$  searches at the LHC than 430 the last regime, which is due to the lower wino-components and higher masses of the  $\tilde{\chi}_2^0/\tilde{\chi}_1^{\pm}$ 431 sparticles that is typical in the last regime. On the other hand, in particular when the 432 coannihilation partner of the LSP is a light stau, the LHC searches show little to no sen-433 sitivity to our found solutions. Our solutions motivate further the ongoing efforts at the 434 LHC to probe pMSSM spectra that feature (compressed) higgsino-like production of  $\tilde{\chi}_2^0 \tilde{\chi}_1^{\pm}$ 435 pairs. In addition, to increase the sensitivity of the LHC to our found solutions, we find 436 that a dedicated low-mass  $\tilde{\tau}^{\pm}$  search without an assumed mass degeneracy between  $\tilde{\tau}_{1}^{\pm}$  and 437  $\tilde{\tau}_2^{\pm}$  would be needed, but also that the mass-gap region of 55 GeV  $< \Delta(m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_1^0}) < M_Z$ 438 is not probed at the LHC. Proposing a dedicated search for these regimes, however, lies 439 beyond the scope of this work. 440

The requirement of satisfying  $\Delta a_{\mu}$  excludes models with a higher-mass higgsino of around 600 GeV as the LSP. Simultaneously, low values of  $\Delta_{\rm EW}$  generally also go with low values of  $|\mu|$ . As the value of  $\Delta_{\rm EW}$  is directly linked to the value for  $\sigma_{\rm SD,p}$  for pMSSM spectra that satisfy the relic density requirement, we see that DMDD experiments that probe  $\sigma_{\rm SD,p}$ will ultimately be sensitive to all of the spectra that offer an explanation for  $\Delta a_{\mu}$  and that are in addition minimally fine-tuned.

## 447 Acknowledgments

448 MvB acknowledges support from the Science and Technology Facilities Council (grant 449 number ST/T000864/1).

## 450 References

- [1] M. van Beekveld, Supplementary Data: "Dark matter, fine-tuning and mu(g-2) in the pMSSM", doi:10.5281/zenodo.4934398 (2021).
- [2] E. Aprile et al., Dark matter search results from aoneton-year 453 of XENON1T, Rev. Lett. **121**(11), exposure Phys. 111302 (2018),454 doi:10.1103/PhysRevLett.121.111302, 1805.12562. 455
- 456 [3] E. Aprile et al., Constraining the spin-dependent WIMP-nucleon cross
   457 sections with XENON1T, Phys. Rev. Lett. **122**(14), 141301 (2019),
   458 doi:10.1103/PhysRevLett.122.141301, **1902.03234**.
- [4] J. Xia et al., PandaX-II constraints on spin-dependent WIMP-nucleon effective *interactions*, Phys. Lett. **B792**, 193 (2019), doi:10.1016/j.physletb.2019.02.043,
  1807.01936.
- 462 [5] A. Tan et al., Dark matter results from first 98.7 days of data from
   463 the PandaX-II experiment, Phys. Rev. Lett. 117(12), 121303 (2016),
   464 doi:10.1103/PhysRevLett.117.121303, 1607.07400.
- <sup>465</sup> [6] C. Amole *et al.*, Dark Matter Search Results from the Complete Exposure of the <sup>466</sup>  $PICO-60 C_3F_8$  Bubble Chamber (2019), 1902.04031.

- 467 [7] C. Amole *et al.*, *Dark Matter Search Results from the PICO-60*  $C_3F_8$  *Bubble Cham-*468 *ber*, Phys. Rev. Lett. **118**(25), 251301 (2017), doi:10.1103/PhysRevLett.118.251301, 469 1702.07666.
- [8] C. Amole et al., Improved dark matter search results from PICO-2L Run 2, Phys.
   Rev. D93(6), 061101 (2016), doi:10.1103/PhysRevD.93.061101, 1601.03729.
- [9] N. Aghanim et al., Planck 2018 results. VI. Cosmological parameters, Astron. Astrophys. 641, A6 (2020), doi:10.1051/0004-6361/201833910, 1807.06209.
- 474 [10] G. W. Bennett *et al.*, *Final Report of the Muon E821 Anomalous Mag-* 475 *netic Moment Measurement at BNL*, Phys. Rev. D **73**, 072003 (2006),
   476 doi:10.1103/PhysRevD.73.072003, hep-ex/0602035.
- 477 [11] G. W. Bennett *et al.*, Measurement of the negative muon anomalous
   478 magnetic moment to 0.7 ppm, Phys. Rev. Lett. 92, 161802 (2004),
   479 doi:10.1103/PhysRevLett.92.161802, hep-ex/0401008.
- [12] G. W. Bennett *et al.*, Measurement of the positive muon anomalous magnetic moment to 0.7 ppm, Phys. Rev. Lett. **89**, 101804 (2002), doi:10.1103/PhysRevLett.89.101804,
   [Erratum: Phys.Rev.Lett. 89, 129903 (2002)], hep-ex/0208001.
- [13] G. Colangelo, M. Hoferichter and P. Stoffer, *Two-pion contribution to hadronic vacuum polarization*, JHEP **02**, 006 (2019), doi:10.1007/JHEP02(2019)006, 1810.
   00007.
- [14] M. Davier, A. Hoecker, B. Malaescu and Z. Zhang, Reevaluation of the hadronic vacuum polarisation contributions to the Standard Model predictions of the muon g - 2 and  $\alpha(m_Z^2)$  using newest hadronic cross-section data, Eur. Phys. J. C 77(12), 827 (2017), doi:10.1140/epjc/s10052-017-5161-6, 1706.09436.
- [15] A. Keshavarzi, D. Nomura and T. Teubner, Muon g-2 and  $\alpha(M_Z^2)$ : a new data-based analysis, Phys. Rev. D 97(11), 114025 (2018), doi:10.1103/PhysRevD.97.114025, 1802.02995.
- [16] M. Hoferichter, B.-L. Hoid and B. Kubis, *Three-pion contribution to hadronic vacuum polarization*, JHEP 08, 137 (2019), doi:10.1007/JHEP08(2019)137, 1907.01556.
- [17] A. Kurz, T. Liu, P. Marquard and M. Steinhauser, *Hadronic contribution to the muon anomalous magnetic moment to next-to-next-to-leading order*, Phys. Lett. B **734**, 144 (2014), doi:10.1016/j.physletb.2014.05.043, 1403.6400.
- [18] K. Melnikov and A. Vainshtein, Hadronic light-by-light scattering contribution to
   the muon anomalous magnetic moment revisited, Phys. Rev. D 70, 113006 (2004),
   doi:10.1103/PhysRevD.70.113006, hep-ph/0312226.
- [19] G. Colangelo, M. Hoferichter, M. Procura and P. Stoffer, Dispersion relation for
   hadronic light-by-light scattering: two-pion contributions, JHEP 04, 161 (2017),
   doi:10.1007/JHEP04(2017)161, 1702.07347.
- [20] M. Hoferichter, B.-L. Hoid, B. Kubis, S. Leupold and S. P. Schneider, *Dispersion relation for hadronic light-by-light scattering: pion pole*, JHEP 10, 141 (2018), doi:10.1007/JHEP10(2018)141, 1808.04823.

- [21] A. Gérardin, H. B. Meyer and A. Nyffeler, Lattice calculation of the pion transition form factor with  $N_f = 2 + 1$  Wilson quarks, Phys. Rev. D **100**(3), 034520 (2019), doi:10.1103/PhysRevD.100.034520, **1903.09471**.
- <sup>510</sup> [22] G. Colangelo, F. Hagelstein, M. Hoferichter, L. Laub and P. Stoffer, Longitudinal <sup>511</sup> short-distance constraints for the hadronic light-by-light contribution to  $(g-2)_{\mu}$  with <sup>512</sup> large-N<sub>c</sub> Regge models, JHEP **03**, 101 (2020), doi:10.1007/JHEP03(2020)101, **1910**. <sup>513</sup> **13432**.
- <sup>514</sup> [23] G. Colangelo, M. Hoferichter, A. Nyffeler, M. Passera and P. Stoffer, *Remarks on* <sup>515</sup> *higher-order hadronic corrections to the muon* g-2, Phys. Lett. B **735**, 90 (2014), <sup>516</sup> doi:10.1016/j.physletb.2014.06.012, 1403.7512.
- <sup>517</sup> [24] P. Masjuan and P. Sanchez-Puertas, *Pseudoscalar-pole contribution to the* <sup>518</sup>  $(g_{\mu} - 2)$ : *a rational approach*, Phys. Rev. D **95**(5), 054026 (2017), <sup>519</sup> doi:10.1103/PhysRevD.95.054026, 1701.05829.
- [25] T. Blum, N. Christ, M. Hayakawa, T. Izubuchi, L. Jin, C. Jung and C. Lehner, *Hadronic Light-by-Light Scattering Contribution to the Muon Anomalous Magnetic Moment from Lattice QCD*, Phys. Rev. Lett. **124**(13), 132002 (2020), doi:10.1103/PhysRevLett.124.132002, 1911.08123.
- [26] J. Prades, E. de Rafael and A. Vainshtein, *The Hadronic Light-by-Light Scattering Contribution to the Muon and Electron Anomalous Magnetic Moments*, Adv. Ser.
  Direct. High Energy Phys. 20, 303 (2009), doi:10.1142/9789814271844\_0009, 0901.
  0306.
- [27] M. Davier, A. Hoecker, B. Malaescu and Z. Zhang, A new evaluation of the hadronic vacuum polarisation contributions to the muon anomalous magnetic moment and to  $\alpha(\mathbf{m}_{\mathbf{Z}}^{2})$ , Eur. Phys. J. C 80(3), 241 (2020), doi:10.1140/epjc/s10052-020-7792-2, [Erratum: Eur.Phys.J.C 80, 410 (2020)], 1908.00921.
- <sup>532</sup> [28] A. Keshavarzi, D. Nomura and T. Teubner, g 2 of charged leptons,  $\alpha(M_Z^2)$ <sup>533</sup> , and the hyperfine splitting of muonium, Phys. Rev. D **101**(1), 014029 (2020), <sup>534</sup> doi:10.1103/PhysRevD.101.014029, **1911.00367**.
- [29] C. Gnendiger, D. Stöckinger and H. Stöckinger-Kim, The electroweak contributions to  $(g-2)_{\mu}$  after the Higgs boson mass measurement, Phys. Rev. D 88, 053005 (2013), doi:10.1103/PhysRevD.88.053005, 1306.5546.
- [30] A. Czarnecki, W. J. Marciano and A. Vainshtein, *Refinements in electroweak contributions to the muon anomalous magnetic moment*, Phys. Rev. D 67, 073006 (2003), doi:10.1103/PhysRevD.67.073006, [Erratum: Phys.Rev.D 73, 119901 (2006)], hep-ph/0212229.
- [31] M. Knecht, S. Peris, M. Perrottet and E. De Rafael, *Electroweak hadronic contribu- tions to the muon (g-2)*, JHEP **11**, 003 (2002), doi:10.1088/1126-6708/2002/11/003,
   hep-ph/0205102.
- [32] T. Aoyama, T. Kinoshita and M. Nio, Revised and Improved Value of the QED
   Tenth-Order Electron Anomalous Magnetic Moment, Phys. Rev. D 97(3), 036001
   (2018), doi:10.1103/PhysRevD.97.036001, 1712.06060.
- [33] T. Aoyama, M. Hayakawa, T. Kinoshita and M. Nio, Complete Tenth-Order
   *QED Contribution to the Muon g-2*, Phys. Rev. Lett. **109**, 111808 (2012),
   doi:10.1103/PhysRevLett.109.111808, **1205.5370**.

#### SciPost Physics

- [34] T. Aoyama et al., The anomalous magnetic moment of the muon in the Standard Model, Phys. Rept. 887, 1 (2020), doi:10.1016/j.physrep.2020.07.006, 2006.04822.
- [35] Muon g 2 Collaboration, Muon (g-2) Technical Design Report (2015), 1501.
   06858.
- [36] Muon g 2 Collaboration, Measurement of the positive muon anomalous magnetic moment to 0.46 ppm, Phys. Rev. Lett. 126, 141801 (2021), doi:10.1103/PhysRevLett.126.141801.
- <sup>558</sup> [37] Muon g 2 Collaboration, Magnetic-field measurement and analysis for the <sup>559</sup> muon g - 2 experiment at fermilab, Phys. Rev. A **103**, 042208 (2021), <sup>560</sup> doi:10.1103/PhysRevA.103.042208.
- <sup>561</sup> [38] **Muon g 2** Collaboration, Measurement of the anomalous precession frequency of <sup>562</sup> the muon in the fermilab muon g - 2 experiment, Phys. Rev. D **103**, 072002 (2021), <sup>563</sup> doi:10.1103/PhysRevA.103.042208.
- [39] T. Mibe, Measurement of muon g-2 and edm with an ultra-cold muon beam
  at j-parc, Nuclear Physics B Proceedings Supplements 218(1), 242 (2011),
  doi:https://doi.org/10.1016/j.nuclphysbps.2011.06.039, Proceedings of the Eleventh
  International Workshop on Tau Lepton Physics.
- [40] M. Abe et al., A New Approach for Measuring the Muon Anomalous Magnetic Moment and Electric Dipole Moment, PTEP 2019(5), 053C02 (2019), doi:10.1093/ptep/ptz030, 1901.03047.
- <sup>571</sup> [41] M. Badziak and K. Sakurai, Explanation of electron and muon g 2 anomalies in <sup>572</sup> the MSSM, JHEP **10**, 024 (2019), doi:10.1007/JHEP10(2019)024, **1908.03607**.
- [42] K. Kowalska, L. Roszkowski, E. M. Sessolo and A. J. Williams, *GUT-inspired SUSY* and the muon g 2 anomaly: prospects for LHC 14 TeV, JHEP 06, 020 (2015),
   doi:10.1007/JHEP06(2015)020, 1503.08219.
- <sup>576</sup> [43] M. A. Ajaib, B. Dutta, T. Ghosh, I. Gogoladze and Q. Shafi, Neutralinos and <sup>577</sup> sleptons at the LHC in light of muon  $(g - 2)_{\mu}$ , Phys. Rev. D **92**(7), 075033 (2015), <sup>578</sup> doi:10.1103/PhysRevD.92.075033, 1505.05896.
- [44] S. P. Das, M. Guchait and D. P. Roy, *Testing SUSY models for the muon g-2* anomaly via chargino-neutralino pair production at the LHC, Phys. Rev. D 90(5), 055011 (2014), doi:10.1103/PhysRevD.90.055011, 1406.6925.
- [45] M. Endo, K. Hamaguchi, S. Iwamoto and T. Kitahara, *Muon g 2 vs LHC Run 2 in supersymmetric models*, JHEP 04, 165 (2020), doi:10.1007/JHEP04(2020)165, 2001.11025.
- [46] K. Hagiwara, K. Ma and S. Mukhopadhyay, Closing in on the chargino contribution to the muon g-2 in the MSSM: current LHC constraints, Phys. Rev. D 97(5), 055035
  (2018), doi:10.1103/PhysRevD.97.055035, 1706.09313.
- <sup>588</sup> [47] H. M. Tran and H. T. Nguyen, *GUT-inspired MSSM in light of muon* g 2 and *LHC results at*  $\sqrt{s} = 13$  *TeV*, Phys. Rev. D **99**(3), 035040 (2019), doi:10.1103/PhysRevD.99.035040, 1812.11757.

17

- [48] M. Abdughani, K.-I. Hikasa, L. Wu, J. M. Yang and J. Zhao, *Testing electroweak SUSY for muon g 2 and dark matter at the LHC and beyond*, JHEP **11**, 095 (2019), doi:10.1007/JHEP11(2019)095, 1909.07792.
- [49] A. Kobakhidze, M. Talia and L. Wu, Probing the MSSM explanation of the muon *g-2 anomaly in dark matter experiments and at a 100 TeV pp collider*, Phys. Rev. D **95**(5), 055023 (2017), doi:10.1103/PhysRevD.95.055023, 1608.03641.
- <sup>597</sup> [50] M. Endo, K. Hamaguchi, S. Iwamoto and K. Yanagi, *Probing minimal SUSY* <sup>598</sup> scenarios in the light of muon g - 2 and dark matter, JHEP **06**, 031 (2017), <sup>599</sup> doi:10.1007/JHEP06(2017)031, 1704.05287.
- [51] M. Chakraborti, S. Heinemeyer and I. Saha, Improved  $(g-2)_{\mu}$  Measurements and Supersymmetry, Eur. Phys. J. C 80(10), 984 (2020), doi:10.1140/epjc/s10052-020-08504-8, 2006.15157.
- [52] P. Cox, C. Han and T. T. Yanagida, Muon g 2 and dark matter in the
   minimal supersymmetric standard model, Phys. Rev. D 98(5), 055015 (2018),
   doi:10.1103/PhysRevD.98.055015, 1805.02802.
- [53] M. Chakraborti, S. Heinemeyer and I. Saha, Improved  $(g-2)_{\mu}$  Measurements and Wino/Higgsino Dark Matter (2021), 2103.13403.
- [54] E. A. Bagnaschi et al., Supersymmetric Dark Matter after LHC Run 1, Eur. Phys.
   J. C 75, 500 (2015), doi:10.1140/epjc/s10052-015-3718-9, 1508.01173.
- [55] G. Bertone, F. Calore, S. Caron, R. Ruiz, J. S. Kim, R. Trotta and C. Weniger,
  Global analysis of the pMSSM in light of the Fermi GeV excess: prospects for the
  LHC Run-II and astroparticle experiments, JCAP 04, 037 (2016), doi:10.1088/14757516/2016/04/037, 1507.07008.
- [56] C. Strege, G. Bertone, G. J. Besjes, S. Caron, R. Ruiz de Austri, A. Strubig and
   R. Trotta, *Profile likelihood maps of a 15-dimensional MSSM*, JHEP 09, 081 (2014),
   doi:10.1007/JHEP09(2014)081, 1405.0622.
- [57] A. Fowlie, K. Kowalska, L. Roszkowski, E. M. Sessolo and Y.-L. S. Tsai, *Dark matter and collider signatures of the MSSM*, Phys. Rev. D 88, 055012 (2013), doi:10.1103/PhysRevD.88.055012, 1306.1567.
- [58] E. Bagnaschi et al., Likelihood Analysis of the pMSSM11 in Light of LHC 13-TeV
   Data, Eur. Phys. J. C 78(3), 256 (2018), doi:10.1140/epjc/s10052-018-5697-0, 1710.
   11091.
- [59] P. Athron *et al.*, A global fit of the MSSM with GAMBIT, Eur. Phys. J. C 77(12),
   879 (2017), doi:10.1140/epjc/s10052-017-5196-8, 1705.07917.
- [60] T. Li and S. Raza, *Electroweak supersymmetry from the generalized mini- mal supergravity model in the MSSM*, Phys. Rev. D **91**(5), 055016 (2015),
   doi:10.1103/PhysRevD.91.055016, 1409.3930.
- [61] T. Li, S. Raza and K. Wang, Constraining Natural SUSY via the Higgs Coupling and
   the Muon Anomalous Magnetic Moment Measurements, Phys. Rev. D 93(5), 055040
   (2016), doi:10.1103/PhysRevD.93.055040, 1601.00178.
- [62] M. Drees and G. Ghaffari, Impact of the Bounds on the Direct Search for Neutralino
   Dark Matter on Naturalness (2021), 2103.15617.

- [63] M. Abdughani, L. Wu and J. M. Yang, Status and prospects of light
   bino-higgsino dark matter in natural SUSY, Eur. Phys. J. C 78(1), 4 (2018),
   doi:10.1140/epjc/s10052-017-5485-2, 1705.09164.
- [64] M. van Beekveld, W. Beenakker, S. Caron, R. Peeters and R. Ruiz de Austri, Supersymmetry with dark matter is still natural, Phys. Rev. D96(3), 035015 (2017), doi:10.1103/PhysRevD.96.035015, 1612.06333.
- [65] M. van Beekveld, S. Caron and R. Ruiz de Austri, *The current status of fine-tuning in supersymmetry*, JHEP **01**, 147 (2020), doi:10.1007/JHEP01(2020)147, 1906.10706.
- [66] H. Baer, V. Barger, D. Sengupta and X. Tata, *Is natural higgsino-only dark matter excluded?*, Eur. Phys. J. C78(10), 838 (2018), doi:10.1140/epjc/s10052-018-6306-y, 1803.11210.
- [67] MSSM Working Group, The minimal supersymmetric standard model: group
   summary report, In GDR (Groupement De Recherche) Supersymetrie Montpellier,
   France, April 15-17, 1998 (1998), 9901246.
- [68] S. R. Coleman and E. J. Weinberg, Radiative corrections as the origin of spontaneous symmetry breaking, Phys. Rev. D7, 1888 (1973), doi:10.1103/PhysRevD.7.1888.
- [69] H. Baer, V. Barger, P. Huang, D. Mickelson, A. Mustafayev and X. Tata, Radiative natural supersymmetry: Reconciling electroweak fine-tuning and the Higgs boson mass, Phys. Rev. D87(11), 115028 (2013), doi:10.1103/PhysRevD.87.115028, 1212.2655.
- [70] H. Baer, V. Barger, P. Huang, A. Mustafayev and X. Tata, *Radiative natural supersymmetry with a 125 GeV Higgs boson*, Phys. Rev. Lett. **109**, 161802 (2012), doi:10.1103/PhysRevLett.109.161802, **1207.3343**.
- [71] H. Baer, V. Barger and D. Mickelson, How conventional measures overestimate
  electroweak fine-tuning in supersymmetric theory, Phys. Rev. D88(9), 095013 (2013),
  doi:10.1103/PhysRevD.88.095013, 1309.2984.
- [72] H. Baer, V. Barger and M. Padeffke-Kirkland, *Electroweak versus high scale finetuning in the 19-parameter SUGRA model*, Phys. Rev. D88, 055026 (2013),
   doi:10.1103/PhysRevD.88.055026, 1304.6732.
- [73] H. Baer, V. Barger, D. Mickelson and M. Padeffke-Kirkland, SUSY models under
  siege: LHC constraints and electroweak fine-tuning, Phys. Rev. D89(11), 115019
  (2014), doi:10.1103/PhysRevD.89.115019, 1404.2277.
- [74] M. Drees and J. S. Kim, *Minimal natural supersymmetry after the LHC8*, Phys.
   Rev. D93(9), 095005 (2016), doi:10.1103/PhysRevD.93.095005, 1511.04461.
- [75] H. Baer, V. Barger, J. S. Gainer, H. Serce and X. Tata, *Reach of the high-energy LHC for gluinos and top squarks in SUSY models with light Higgsinos*, Phys. Rev.
   **D96**(11), 115008 (2017), doi:10.1103/PhysRevD.96.115008, 1708.09054.
- [76] A. Mustafayev and X. Tata, Supersymmetry, Naturalness, and Light Higgsinos,
   Indian J. Phys. 88, 991 (2014), doi:10.1007/s12648-014-0504-8, 1404.1386.
- [77] H. Baer, V. Barger, P. Huang, D. Mickelson, A. Mustafayev and X. Tata, *Radiative natural supersymmetry: Reconciling electroweak fine-tuning and the higgs boson mass*, Phys. Rev. D 87, 115028 (2013), doi:10.1103/PhysRevD.87.115028.

- [78] H. Baer, V. Barger and M. Savoy, Upper bounds on sparticle masses from naturalness
  or how to disprove weak scale supersymmetry, Phys. Rev. D 93, 035016 (2016),
  doi:10.1103/PhysRevD.93.035016.
- [79] T. Moroi, The Muon anomalous magnetic dipole moment in the minimal supersymmetric standard model, Phys. Rev. D 53, 6565 (1996), doi:10.1103/PhysRevD.53.6565, [Erratum: Phys.Rev.D 56, 4424 (1997)], hep-ph/ 9512396.
- [80] S. P. Martin and J. D. Wells, *Muon Anomalous Magnetic Dipole Mo- ment in Supersymmetric Theories*, Phys. Rev. D 64, 035003 (2001),
   doi:10.1103/PhysRevD.64.035003, hep-ph/0103067.
- [81] D. Stockinger, The Muon Magnetic Moment and Supersymmetry, J. Phys. G 34, R45 (2007), doi:10.1088/0954-3899/34/2/R01, hep-ph/0609168.
- [82] H. Fargnoli, C. Gnendiger, S. Paßehr, D. Stöckinger and H. Stöckinger-Kim, Twoloop corrections to the muon magnetic moment from fermion/sfermion loops in the MSSM: detailed results, JHEP 02, 070 (2014), doi:10.1007/JHEP02(2014)070, 1311.
   1775.
- [83] H. G. Fargnoli, C. Gnendiger, S. Paßehr, D. Stöckinger and H. Stöckinger-Kim, Nondecoupling two-loop corrections to  $(g-2)_{\mu}$  from fermion/sfermion loops in the MSSM, Phys. Lett. B **726**, 717 (2013), doi:10.1016/j.physletb.2013.09.034, 1309.0980.
- [84] M. Endo, K. Hamaguchi, T. Kitahara and T. Yoshinaga, *Probing Bino contribution* to muon g - 2, JHEP **11**, 013 (2013), doi:10.1007/JHEP11(2013)013, 1309.3065.
- [85] B. C. Allanach, SOFTSUSY: a program for calculating supersymmetric spectra,
   Comput. Phys. Commun. 143, 305 (2002), doi:10.1016/S0010-4655(01)00460-X,
   hep-ph/0104145.
- [86] H. Bahl and W. Hollik, Precise prediction for the light MSSM Higgs boson mass
  combining effective field theory and fixed-order calculations, Eur. Phys. J. C76(9),
  499 (2016), doi:10.1140/epjc/s10052-016-4354-8, 1608.01880.
- [87] T. Hahn, S. Heinemeyer, W. Hollik, H. Rzehak and G. Weiglein, *Highprecision predictions for the Light CP-even Higgs boson mass of the Minimal Supersymmetric Standard Model*, Phys. Rev. Lett. **112**(14), 141801 (2014), doi:10.1103/PhysRevLett.112.141801, 1312.4937.
- [88] M. Frank, T. Hahn, S. Heinemeyer, W. Hollik, H. Rzehak and G. Weiglein, The Higgs boson masses and mixings of the complex MSSM in the Feynman-diagrammatic approach, JHEP 0702, 047 (2007), doi:10.1088/1126-6708/2007/02/047, 0611326.
- [89] G. Degrassi, S. Heinemeyer, W. Hollik, P. Slavich and G. Weiglein, Towards high precision predictions for the MSSM Higgs sector, Eur. Phys. J. C28, 133 (2003), doi:10.1140/epjc/s2003-01152-2, 0212020.
- [90] S. Heinemeyer, W. Hollik and G. Weiglein, *FeynHiggs: A program for the calculation*of the masses of the neutral CP even Higgs bosons in the MSSM, Comput. Phys.
  Commun. 124, 76 (2000), doi:10.1016/S0010-4655(99)00364-1, 9812320.
- [91] A. Djouadi, M. M. Muhlleitner and M. Spira, Decays of supersymmetric particles: the program SUSY-HIT (SUspect-SdecaY-Hdecay-InTerface), Acta Phys. Polon. B38, 635 (2007), hep-ph/0609292.

- [92] J. E. Camargo-Molina, B. O'Leary, W. Porod and F. Staub, Vevacious: A tool for finding the global minima of one-loop effective potentials with many scalars, Eur. Phys. J. C73(10), 2588 (2013), doi:10.1140/epjc/s10052-013-2588-2, 1307.1477.
- [93] T. L. Lee, T. Y. Li and C. H. Tsai, Hom4ps-2.0: a software package for solving polynomial systems by the polyhedral homotopy continuation method, Computing 83(2), 109 (2008), doi:10.1007/s00607-008-0015-6.
- [94] C. L. Wainwright, Cosmo Transitions: Computing cosmological phase transition temperatures and bubble profiles with multiple fields, Comput. Phys. Commun. 183, 2006 (2012), doi:10.1016/j.cpc.2012.04.004, 1109.4189.
- [95] S. Caron, J. S. Kim, K. Rolbiecki, R. Ruiz de Austri and B. Stienen, *The BSM-AI* project: SUSY-AI-generalizing LHC limits on supersymmetry with machine learning, Eur. Phys. J. C77(4), 257 (2017), doi:10.1140/epjc/s10052-017-4814-9, 1605.02797.
- [96] F. Ambrogi et al., SModelS v1.2: long-lived particles, combination of signal regions, and other novelties (2018), 1811.10624.
- [97] J. Heisig, S. Kraml and A. Lessa, Constraining new physics with searches for
  long-lived particles: implementation into SModelS, Phys. Lett. B788, 87 (2019),
  doi:10.1016/j.physletb.2018.10.049, 1808.05229.
- [98] J. Dutta, S. Kraml, A. Lessa and W. Waltenberger, *SModelS extension with the CMS supersymmetry search results from Run 2*, LHEP 1(1), 5 (2018),
   doi:10.31526/LHEP.1.2018.02, 1803.02204.
- [99] F. Ambrogi, S. Kraml, S. Kulkarni, U. Laa, A. Lessa, V. Magerl, J. Sonneveld,
  M. Traub and W. Waltenberger, *SModelS v1.1 user manual: Improving simplified model constraints with efficiency maps*, Comput. Phys. Commun. 227, 72 (2018),
  doi:10.1016/j.cpc.2018.02.007, 1701.06586.
- [100] S. Kraml, S. Kulkarni, U. Laa, A. Lessa, W. Magerl, D. Proschofsky-Spindler and
  W. Waltenberger, *SModelS: a tool for interpreting simplified-model results from the LHC and its application to supersymmetry*, Eur. Phys. J. C74, 2868 (2014),
  doi:10.1140/epjc/s10052-014-2868-5, 1312.4175.
- [101] W. Beenakker, R. Hopker and M. Spira, *PROSPINO: A Program for the production* of supersymmetric particles in next-to-leading order QCD (1996), hep-ph/9611232.
- [102] P. Bechtle, S. Heinemeyer, O. Stål, T. Stefaniak and G. Weiglein, Applying exclusion *likelihoods from LHC searches to extended Higgs sectors*, Eur. Phys. J. C75(9), 421
  (2015), doi:10.1140/epjc/s10052-015-3650-z, 1507.06706.
- [103] P. Bechtle, O. Brein, S. Heinemeyer, O. Stål, T. Stefaniak, G. Weiglein and K. E.
  Williams, HiggsBounds-4: Improved tests of extended Higgs sectors against exclusion bounds from LEP, the Tevatron and the LHC, Eur. Phys. J. C74(3), 2693 (2014), doi:10.1140/epjc/s10052-013-2693-2, 1311.0055.
- [104] P. Bechtle, O. Brein, S. Heinemeyer, O. Stål, T. Stefaniak, G. Weiglein and K. Williams, *Recent developments in HiggsBounds and a preview of HiggsSignals*, PoS 2012, 024 (2012), doi:10.22323/1.156.0024, 1301.2345.

#### SciPost Physics

- [105] P. Bechtle, O. Brein, S. Heinemeyer, G. Weiglein and K. E. Williams, *Higgs-Bounds 2.0.0: Confronting neutral and charged Higgs sector predictions with exclusion bounds from LEP and the Tevatron*, Comput. Phys. Commun. 182, 2605 (2011), doi:10.1016/j.cpc.2011.07.015, 1102.1898.
- [106] P. Bechtle, O. Brein, S. Heinemeyer, G. Weiglein and K. E. Williams, *HiggsBounds: confronting arbitrary Higgs sectors with exclusion bounds from LEP and the Tevatron*, Comput. Phys. Commun. **181**, 138 (2010), doi:10.1016/j.cpc.2009.09.003, **0811**. **4169**.
- [107] O. Stål and T. Stefaniak, Constraining extended Higgs sectors with HiggsSignals,
   PoS 2013, 314 (2013), doi:10.22323/1.180.0314, 1310.4039.
- [108] P. Bechtle, S. Heinemeyer, O. Stål, T. Stefaniak and G. Weiglein, Probing the Standard Model with Higgs signal rates from the Tevatron, the LHC and a future ILC, JHEP 1411, 039 (2014), doi:10.1007/JHEP11(2014)039, 1403.1582.
- [109] P. Bechtle, S. Heinemeyer, O. Stål, T. Stefaniak and G. Weiglein, *HiggsSignals: Confronting arbitrary Higgs sectors with measurements at the Tevatron and the LHC*,
   Eur. Phys. J. C74(2), 2711 (2014), doi:10.1140/epjc/s10052-013-2711-4, 1305.1933.
- [110] G. Belanger, F. Boudjema, A. Pukhov and A. Semenov, *micrOMEGAs: Version 1.3*,
   Comput. Phys. Commun. **174**, 577 (2006), doi:10.1016/j.cpc.2005.12.005, hep-ph/
   0405253.
- [111] G. Belanger, F. Boudjema, A. Pukhov and A. Semenov, *MicrOMEGAs 2.0: A Program to calculate the relic density of dark matter in a generic model*, Comput.
   Phys. Commun. **176**, 367 (2007), doi:10.1016/j.cpc.2006.11.008, hep-ph/0607059.
- [112] G. Belanger, F. Boudjema, A. Pukhov and A. Semenov, *Dark matter direct detection* rate in a generic model with micrOMEGAs 2.2, Comput. Phys. Commun. 180, 747 (2009), doi:10.1016/j.cpc.2008.11.019, 0803.2360.
- [113] G. Belanger, F. Boudjema, P. Brun, A. Pukhov, S. Rosier-Lees, P. Salati and A. Semenov, *Indirect search for dark matter with micrOMEGAs2.4*, Comput. Phys. Commun. 182, 842 (2011), doi:10.1016/j.cpc.2010.11.033, 1004.1092.
- [114] G. Belanger, F. Boudjema, A. Pukhov and A. Semenov, micrOMEGAs\_3: A program for calculating dark matter observables, Comput. Phys. Commun. 185, 960 (2014), doi:10.1016/j.cpc.2013.10.016, 1305.0237.
- [115] G. Belanger, A. Mjallal and A. Pukhov, Recasting direct detection limits within
   micrOMEGAs and implication for non-standard Dark Matter scenarios (2020),
   2003.08621.
- [116] M. Ackermann et al., Searching for Dark Matter Annihilation from Milky Way Dwarf
   Spheroidal Galaxies with Six Years of Fermi Large Area Telescope Data, Phys. Rev.
   Lett. 115(23), 231301 (2015), doi:10.1103/PhysRevLett.115.231301, 1503.02641.
- [117] The GAMBIT Dark Matter Workgroup, DarkBit: A GAMBIT module for
   computing dark matter observables and likelihoods, Eur. Phys. J. C77(12), 831
   (2017), doi:10.1140/epjc/s10052-017-5155-4, 1705.07920.
- [118] F. Mahmoudi, SuperIso: A Program for calculating the isospin asymmetry of
   B —> K\* gamma in the MSSM, Comput. Phys. Commun. 178, 745 (2008),
   doi:10.1016/j.cpc.2007.12.006, 0710.2067.

- [119] F. Mahmoudi, SuperIso v2.3: A Program for calculating flavor physics observables in Supersymmetry, Comput. Phys. Commun. 180, 1579 (2009), doi:10.1016/j.cpc.2009.02.017, 0808.3144.
- [120] P. Athron, M. Bach, H. G. Fargnoli, C. Gnendiger, R. Greifenhagen, J.-h. Park, S. Paßehr, D. Stöckinger, H. Stöckinger-Kim and A. Voigt, *GM2Calc: Precise MSSM prediction for* (g - 2) *of the muon*, Eur. Phys. J. C **76**(2), 62 (2016), doi:10.1140/epjc/s10052-015-3870-2, 1510.08071.
- [121] P. von Weitershausen, M. Schafer, H. Stockinger-Kim and D. Stockinger, *Photonic SUSY Two-Loop Corrections to the Muon Magnetic Moment*, Phys. Rev. D 81, 093004 (2010), doi:10.1103/PhysRevD.81.093004, 1003.5820.
- <sup>811</sup> [122] M. Bach, J.-h. Park, D. Stöckinger and H. Stöckinger-Kim, Large muon (g 2) with TeV-scale SUSY masses for  $\tan \beta \rightarrow \infty$ , JHEP **10**, 026 (2015), <sup>813</sup> doi:10.1007/JHEP10(2015)026, **1504.05500**.
- [123] J. H. Kotecha and P. M. Djuric, *Gaussian particle filtering*, IEEE Transactions on
  Signal Processing 51(10), 2592 (2003), doi:10.1109/TSP.2003.816758.
- 816 [124] LEP2 SUSY Working Group, ALEPH, DELPHI, L3 and OPAL experiments.
- [125] A. Heister et al., Absolute lower limits on the masses of selectrons and sneutrinos
   in the MSSM, Phys. Lett. B 544, 73 (2002), doi:10.1016/S0370-2693(02)02471-1,
   hep-ex/0207056.
- <sup>820</sup> [126] M. Carena, A. de Gouvea, A. Freitas and M. Schmitt, *Invisible Z boson decays at* <sup>821</sup>  $e^+e^-$  colliders, Phys. Rev. **D68**, 113007 (2003), doi:10.1103/PhysRevD.68.113007, <sup>822</sup> 0308053.
- [127] T. Han, Z. Liu and A. Natarajan, Dark matter and Higgs bosons in the MSSM,
   JHEP 11, 008 (2013), doi:10.1007/JHEP11(2013)008, 1303.3040.
- [128] G. Belanger, F. Boudjema, A. Cottrant, R. M. Godbole and A. Semenov, *The MSSM invisible Higgs in the light of dark matter and g-2*, Phys. Lett. B **519**, 93 (2001),
   doi:10.1016/S0370-2693(01)00976-5, hep-ph/0106275.
- [129] T. Nihei, L. Roszkowski and R. Ruiz de Austri, *Exact cross-sections for the neutralino* slepton coannihilation, JHEP 07, 024 (2002), doi:10.1088/1126-6708/2002/07/024, hep-ph/0206266.
- [130] M. Aaboud et al., Search for chargino-neutralino production using recursive jigsaw reconstruction in final states with two or three charged leptons in proton-proton collisions at  $\sqrt{s} = 13$  TeV with the ATLAS detector, Phys. Rev. D **98**(9), 092012 (2018), doi:10.1103/PhysRevD.98.092012, 1806.02293.
- [131] A. M. Sirunyan *et al.*, Combined search for electroweak production of charginos and neutralinos in proton-proton collisions at  $\sqrt{s} = 13$  TeV, JHEP **03**, 160 (2018), doi:10.1007/JHEP03(2018)160, 1801.03957.
- [132] A. M. Sirunyan et al., Search for supersymmetry in final states with two oppositely charged same-flavor leptons and missing transverse momentum in proton-proton collisions at  $\sqrt{s} = 13$  TeV (2020), 2012.08600.

- [133] A. M. Sirunyan et al., Search for supersymmetry with a compressed mass spectrum in the vector boson fusion topology with 1-lepton and 0-lepton final states in proton-proton collisions at  $\sqrt{s} = 13$  TeV, JHEP **08**, 150 (2019), doi:10.1007/JHEP08(2019)150, 1905.13059.
- [134] Search for electroweak production of charginos and neutralinos in proton-proton collisions at sqrt(s)=13 TeV, Tech. Rep. CMS-PAS-SUS-19-012, CERN, Geneva (2021).
- [135] M. Aaboud et al., Search for the direct production of charginos and neutralinos in final states with tau leptons in  $\sqrt{s} = 13$  TeV pp collisions with the ATLAS detector, Eur. Phys. J. C **78**(2), 154 (2018), doi:10.1140/epjc/s10052-018-5583-9, 1708.07875.
- [136] A. M. Sirunyan et al., Search for direct pair production of supersymmetric partners to the  $\tau$  lepton in proton-proton collisions at  $\sqrt{s} = 13$  TeV, Eur. Phys. J. C 80(3), 189 (2020), doi:10.1140/epjc/s10052-020-7739-7, 1907.13179.
- [137] A. M. Sirunyan et al., Search for Supersymmetry with a Compressed Mass Spectrum in Events with a Soft  $\tau$  Lepton, a Highly Energetic Jet, and Large Missing Transverse Momentum in Proton-Proton Collisions at  $\sqrt{s} = TeV$ , Phys. Rev. Lett. **124**(4), 041803 (2020), doi:10.1103/PhysRevLett.124.041803, **1910.01185**.
- [138] G. Aad et al., Search for direct stau production in events with two hadronic  $\tau$ -leptons in  $\sqrt{s} = 13$  TeV pp collisions with the ATLAS detector, Phys. Rev. D **101**(3), 032009 (2020), doi:10.1103/PhysRevD.101.032009, **1911.06660**.
- [139] G. Aad et al., Searches for electroweak production of supersymmetric particles with compressed mass spectra in  $\sqrt{s} = 13$  TeV pp collisions with the ATLAS detector, Phys. Rev. D **101**(5), 052005 (2020), doi:10.1103/PhysRevD.101.052005, **1911**. **12606**.
- [140] G. Aad et al., Search for electroweak production of charginos and sleptons decaying into final states with two leptons and missing transverse momentum in  $\sqrt{s} = 13$ TeV pp collisions using the ATLAS detector, Eur. Phys. J. C 80(2), 123 (2020), doi:10.1140/epjc/s10052-019-7594-6, 1908.08215.
- [141] J. Kumar and D. Marfatia, Matrix element analyses of dark matter scattering and
   annihilation, Phys. Rev. D88(1), 014035 (2013), doi:10.1103/PhysRevD.88.014035,
   1305.1611.
- [142] Toward a next-generation dark matter search with the PICO-40L bubble chamber, https://indico.cern.ch/event/606690/contributions/2623446/attachments/
  1497228/2330240/Fallows\_2017\_07\_24\_\_TAUP\_\_PICO-40L\_v1.2.pdf, Accessed:
  2021-03-24.
- [143] D. S. Akerib *et al.*, LUX-ZEPLIN (LZ) Conceptual Design Report (2015), 1509.
   02910.