

Transport and Magnetic Properties in the Nd Diluted System $Y_{1-x}Nd_xCo_2Zn_{20}$

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Abstract

We report the electrical resistivity, specific heat, and magnetization measurements of $Y_{1-x}Nd_xCo_2Zn_{20}$ for $0.017 \leq x \leq 0.95$. The Schottky-type specific heat peak at around 13 K for all the samples is reproduced by the crystalline electric field model with the Γ_6 doublet ground state of a Nd^{3+} ion. The magnetization and magnetic susceptibility data of the samples for $x \leq 0.06$ are well reproduced by the calculation without intersite magnetic interactions among Nd moments. Therefore, the dilute Nd system $Y_{1-x}Nd_xCo_2Zn_{20}$ for $x \leq 0.06$ is a good candidate to study on-site interaction of the Γ_6 doublet ground state of $4f$ electrons with conduction electrons.

1 Introduction

The caged compounds RTr_2X_{20} (R : rare-earth, Tr : transition metal, $X = Al, Zn,$ and Cd) crystallize in the cubic $CeCr_2Al_{20}$ -type structure with the space group of $Fd\bar{3}m$ (No. 227, O_h^7) [1]. The R^{3+} ions at the $8a$ site with the cubic point group T_d are encapsulated in the Frank-Kasper cages formed by sixteen X atoms. This feature weakens the crystalline electric field (CEF) effect and enhances hybridization of $4f$ electrons with conduction electrons ($c-f$ hybridization).

In a Pr-based compound $PrIr_2Zn_{20}$, this characteristic gives rise to non-Fermi liquid (NFL) behavior related to the quadrupolar degrees of freedom in the Γ_3 ground state of Pr^{3+} ion under the cubic CEF [2]. In fact, the temperature dependences of the electrical resistivity ρ and the magnetic specific heat C_m agree with those calculated based on the two-channel Anderson lattice model. Therefore, formation of a quadrupolar Kondo lattice was proposed [3]. In recent years, a Pr-diluted system $Y_{1-x}Pr_xIr_2Zn_{20}$ has been systematically studied to investigate the single-site quadrupole Kondo effect [4–6]. In addition to the NFL behaviors of $\rho(T)$ and $C_m(T)$, the elastic constant $(C_{11} - C_{12})/2$ shows a logarithmic temperature dependence below 0.3 K, providing another support for the single-site quadrupolar Kondo effect. On the other hand, the quadrupolar Kondo effect predicted the residual entropy of $0.5R\ln 2$ at $T = 0$, which has not been observed yet.

The Nd-based family $NdTr_2Zn_{20}$ ($Tr = Co, Ru, Rh, Os,$ and Ir) and $NdTr_2Al_{20}$ ($Tr = Ti, V,$ and Cr) with mostly the Γ_6 doublet ground state of the $4f^3$ configuration provide a new platform

19 to investigate the magnetic two-channel Kondo effect. A theoretical calculation using a numerical
 20 renormalization group method with a seven-orbital impurity Anderson model showed that the
 21 residual entropy of $0.5R\ln 2$, which is the characteristic of the two-channel Kondo effect, manifests
 22 itself in a wide range of parameters for the local Γ_6 doublet ground state [7]. Here, it is noted
 23 that relatively large $c-f$ hybridization is needed to exhibit the two-channel Kondo effect in the
 24 $4f^3$ systems. Among $\text{NdTr}_2\text{X}_{20}$, the $c-f$ hybridization in $\text{NdCo}_2\text{Zn}_{20}$ is expected to be larger than
 25 the other $\text{NdTr}_2\text{X}_{20}$ compounds, because the lattice parameter is the smallest and the magnetic
 26 transition temperature $T_N = 0.53$ K is the lowest [8–13]. In fact, the $\rho(T)$ data of $\text{NdCo}_2\text{Zn}_{20}$
 27 decrease with a downward convex curvature on cooling from 4 K to T_N , which is expressed by the
 28 theoretical form derived from the two-channel Anderson lattice model [8]. However, it is not clear
 29 whether this temperature variation of $\rho(T)$ is ascribed to the two-channel Kondo effect or intersite
 30 magnetic interaction between Nd moments.

31 In this paper, we focus on $\text{Y}_{1-x}\text{Nd}_x\text{Co}_2\text{Zn}_{20}$ for $0.017 \leq x \leq 0.95$ to study how the inter-
 32 site magnetic interaction is modified by the Nd substitutions. In intermetallic compounds, the
 33 Ruderman-Kittel-Kasuya-Yosida (RKKY) interaction is mediated by the spin polarization of con-
 34 duction electrons, which sign oscillates with respect to the distance. The oscillating and long-
 35 ranged nature is well manifested in $\text{La}_{1-x}\text{Nd}_x$ [14]. An antiferromagnetic order in $x = 1$ changes
 36 to a ferromagnetic one for $x = 0.6$ and it persists down to $x = 0.2$. These results indicate that
 37 the intersite magnetic interaction in the Nd rich region depends on band structure. In analogy, to
 38 examine the on-site interaction of the $4f^3$ state with conduction electrons in $\text{Y}_{1-x}\text{Nd}_x\text{Co}_2\text{Zn}_{20}$, the
 39 dilute range $x < 0.2$ should be studied carefully. We synthesized the single-crystalline samples of
 40 $\text{Y}_{1-x}\text{Nd}_x\text{Co}_2\text{Zn}_{20}$ and measured the electrical resistivity, specific heat, isothermal magnetization,
 41 and magnetic susceptibility for $T \geq 1.8$ K.

42 2 Experimental Procedure

43 Single-crystalline samples of $\text{Y}_{1-x}\text{Nd}_x\text{Co}_2\text{Zn}_{20}$ for $0.017 \leq x \leq 0.95$ were synthesized by the
 44 Zn self-flux method as described in the previous report [15]. We used high purity elements of
 45 Y (99.9%), Nd (99.99%), Co (99.9%), and Zn (99.9999%). The samples were characterized
 46 by powder x-ray diffraction (XRD) measurements. The Rietveld analysis of the XRD patterns
 47 using RIETAN-FP [16] confirmed the $\text{CeCr}_2\text{Al}_{20}$ -type structure for all the samples. **The lattice**
 48 **parameter determined by the Rietveld analysis increases linearly with respect to x .** The atomic
 49 compositions were obtained by the wavelength-dispersive electron-probe microanalysis (EPMA).
 50 For the Nd diluted samples of $x < 0.05$, it was difficult to determine the compositions of the
 51 bulk samples since the EPMA probes only the surface and the resolution is not high for detecting
 52 the small ratio below 0.05. To estimate the Nd compositions more accurately, we measured the
 53 magnetization curves at $T = 1.8$ K to compare with that calculated by using the CEF level schemes
 54 determined by inelastic neutron scattering (INS) measurements of $\text{NdCo}_2\text{Zn}_{20}$ [17].

55 The electrical resistance was measured by a standard four-probe AC method with a laboratory-
 56 built system using a Gifford-McMahon-type refrigerator in the temperature range of 3–300 K.
 57 Heat capacity measurements were performed by the thermal relaxation method between 4 and
 58 300 K using a physical property measurement system (PPMS, Quantum Design). Magnetization
 59 measurements were carried out with a commercial superconducting quantum interference device
 60 magnetometer (MPMS, Quantum Design) from 1.8 to 300 K in magnetic fields up to 5 T.

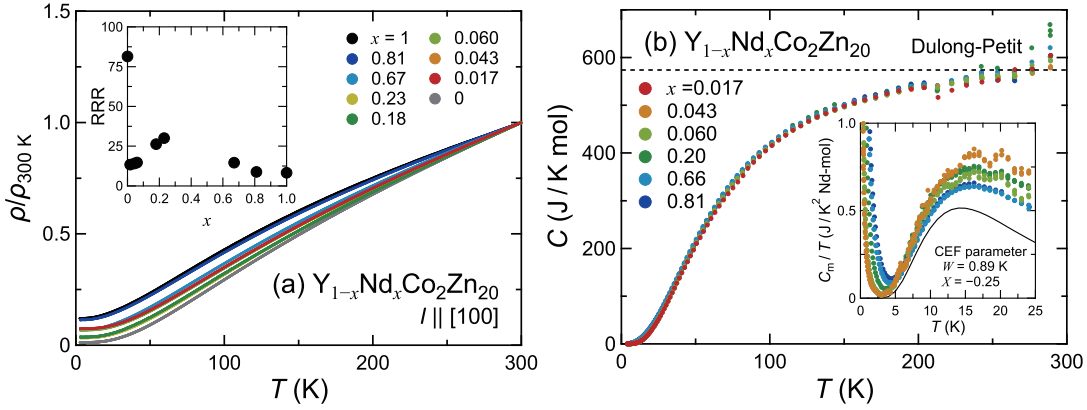


Figure 1: (a) Normalized electrical resistivity $\rho(T)/\rho(300\text{ K})$ versus temperature T of $\text{Y}_{1-x}\text{Nd}_x\text{Co}_2\text{Zn}_{20}$ for $0 \leq x \leq 1$. The $\rho(T)$ data for $x = 1$ are from [8]. The inset shows the residual resistivity ratio as $\text{RRR} = \rho(300\text{ K})/\rho(3\text{ K})$. (b) Specific heat C versus T of $\text{Y}_{1-x}\text{Nd}_x\text{Co}_2\text{Zn}_{20}$ for $0.017 \leq x \leq 0.81$. The dashed line is the Dulong-Petit value of $573.7\text{ J/K mol}^{-1}$. The inset shows the magnetic specific heat divided by temperature C_m/T for $x = 0.043, 0.060, 0.66,$ and 0.81 . The solid line represents the CEF calculation.

61 3 Results and Discussion

62 Figure 1(a) shows the temperature dependences of the normalized electrical resistivity
 63 $\rho(T)/\rho(300\text{ K})$ of $\text{Y}_{1-x}\text{Nd}_x\text{Co}_2\text{Zn}_{20}$ including end compositions $x = 0$ and 1 [8]. The electric
 64 current was applied along the $[100]$ direction for the single-crystalline samples. The data decrease
 65 with downward curvature, and asymptotically approach constant values below 10 K . As shown
 66 in the inset of Fig. 1, the residual resistivity ratio defined as $\text{RRR} = \rho(300\text{ K})/\rho(3\text{ K})$ largely
 67 decreases from 81.4 for $x = 0$ to 13.4 for $x = 0.017$.

68 The specific heat C versus temperature is displayed in Fig. 1(b). The $C(T)$ data certainly reach
 69 the Dulong-Petit value of 573.7 J/K mol at 300 K as expected for a compound with 23 atoms in
 70 the formula unit. **The magnetic specific heat divided by temperature as a function of temperature,**
 71 **$C_m(T)/T$ vs T , is shown in the inset of Fig. 1(b).** We obtained the magnetic contribution $C_m(T)$
 72 by subtracting the $C(T)$ data of a nonmagnetic counterpart $\text{YCo}_2\text{Zn}_{20}$ as the lattice contribution
 73 from the measured specific heat. The $C_m(T)/T$ data show maxima at around 13 K , representing
 74 the Schottky specific heat due to the thermal excitations from the CEF ground state to the excited
 75 CEF levels. The CEF Hamiltonian \mathcal{H}_{CEF} for the Nd^{3+} ion under the cubic CEF is described as [18]

$$\mathcal{H}_{\text{CEF}} = W \left[\frac{X}{60} (O_4^0 + 5O_4^4) + \frac{1 - |X|}{2520} (O_6^0 - 21O_6^4) \right]. \quad (1)$$

76 The solid line is the CEF calculation by using the CEF level scheme of $\Gamma_6(0\text{ K}) - \Gamma_8^{(1)}(44\text{ K}) -$
 77 $\Gamma_8^{(2)}(84\text{ K})$ for $\text{NdCo}_2\text{Zn}_{20}$ determined by the INS measurements [17]. Here, we adopted the CEF
 78 parameters of $W = 0.89\text{ K}$ and $X = -0.25$. The maxima in $C_m(T)/T$ stays at around 13 K
 79 as calculated by the CEF model. This fact indicates that the CEF level scheme hardly changes
 80 among $\text{Y}_{1-x}\text{Nd}_x\text{Co}_2\text{Zn}_{20}$.

81 Figure 2(a) shows the $4f$ contribution of the magnetic susceptibility χ_{Nd} measured in $B = 0.1$
 82 T applied along the $[100]$ direction. The data for $x \leq 0.06$ was measured in $B = 0.5\text{ T}$. The χ_{Nd}
 83 data are deduced by subtracting the $\chi(T)$ data of $\text{YCo}_2\text{Zn}_{20}$ from the measured magnetic suscep-
 84 tibility. **It is noted that the band structure calculation of $\text{YCo}_2\text{Zn}_{20}$ suggests an intermetallic state**
 85 **with negligible electron-electron correlation, leading to a non-magnetic ground state [19, 20]** The
 86 χ_{Nd} data follow the Curie-Weiss law above 50 K . The effective magnetic moments are estimated
 87 to be $3.7\text{--}4.2\ \mu_{\text{B}}/\text{Nd}$, which are slightly higher than $3.62\ \mu_{\text{B}}$ of a free Nd^{3+} ion. The paramagnetic

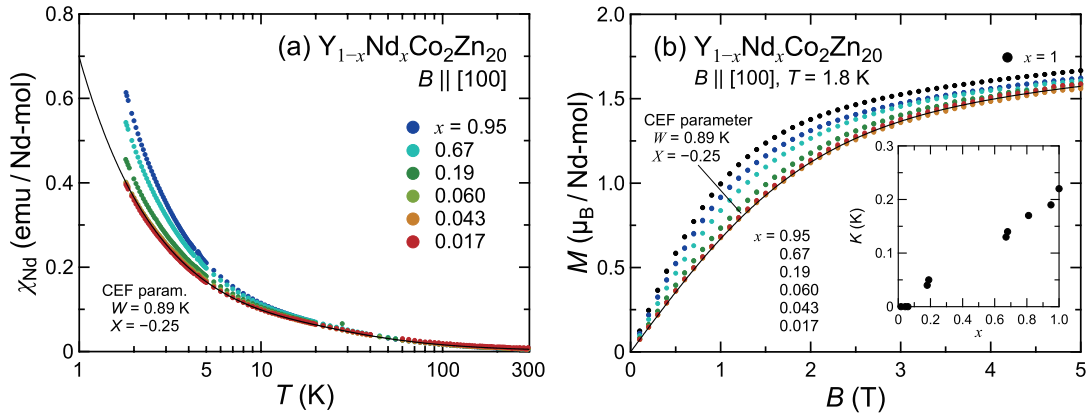


Figure 2: (a) $4f$ contribution of the magnetic susceptibility χ_{Nd} versus temperature T of $\text{Y}_{1-x}\text{Nd}_x\text{Co}_2\text{Zn}_{20}$ for $0.017 \leq x \leq 0.95$ on a logarithmic scale. The solid line shows the $M(B)$ data calculated with the CEF parameters $W = 0.89$ K and $X = -0.25$. (b) Isothermal magnetization $M(B)$ at $T = 1.8$ K, where the data for $x = 1$ are taken from [17]. The data are normalized by the Nd composition x . The solid line was calculated using the CEF parameters. The inset shows the intersite magnetic interaction parameter K estimated by the $M(B)$ data.

88 Curie temperatures θ_p are negative, indicating that the antiferro-type magnetic interaction is pre-
 89 dominant. Below 10 K, the χ_{Nd} data depends on x . The χ_{Nd} data for $x \geq 0.19$ are larger than the
 90 solid line that was calculated by the CEF model without a molecular-field parameter. On the other
 91 hand, as x is reduced from $x = 0.19$, the χ_{Nd} data for $T < 10$ K approach the solid line. Con-
 92 sidering that the Γ_6 doublet ground states is mostly populated below 10 K, the intersite magnetic
 93 interaction among the CEF ground states is ferro-type but negligible for $x \leq 0.06$.

94 The strength of intersite magnetic interaction was estimated from mean-field analysis of the
 95 isothermal magnetization data $M(B) \parallel [100]$ at 1.8 K as displayed in Fig. 2(b). The curvatures of
 96 $M(B)$ are gradually suppressed as decreasing x . To evaluate the intersite magnetic interaction, we
 97 use a mean-field Hamiltonian expressed as

$$\mathcal{H} = \mathcal{H}_{\text{CEF}} + g_J \mu_B \mathbf{J} B - K \langle \mathbf{J} \rangle \mathbf{J}, \quad (2)$$

98 where $g_J = 8/11$ is the Landé g -factor for a Nd^{3+} ion, \mathbf{J} the total angular momentum, and K the
 99 strength of the intersite magnetic interaction between the Nd moments. The solid line represents
 100 the CEF calculation with no magnetic interaction as described below.

$$M = \frac{g_J \mu_B}{Z} \sum_i \langle i | \mathbf{J} | j \rangle e^{-E_i / k_B T}. \quad (3)$$

101 Z is the partition function. The calculation with $K = 0$ reproduces the data for $x \leq 0.06$. The
 102 intersite magnetic interaction K versus x is plotted in the inset of Fig. 2(b). The values of K for
 103 $x \leq 0.06$ were estimated to be zero within the error of the present analysis. Ferro-type intersite
 104 magnetic interaction deduced from the $M(B)$ data is consistent with the value of θ_p evaluated from
 105 the $\chi(T)$ data below 10 K. These facts suggest that the single-site state of the Γ_6 doublet with
 106 no intersite magnetic interaction is realized in $\text{Y}_{1-x}\text{Nd}_x\text{Co}_2\text{Zn}_{20}$ for $x \leq 0.06$. Therefore, this
 107 dilute Nd system could provide a good platform to investigate the single-site hybridization effect
 108 of the $4f$ electrons with the conduction electrons. The low-temperature transport and magnetic
 109 properties below 1.8 K will be reported in a forthcoming paper.

4 Conclusion

We have measured $\rho(T)$, $C(T)$, $\chi(T)$, and $M(B)$ of $Y_{1-x}Nd_xCo_2Zn_{20}$ for $0.017 \leq x \leq 0.95$. The Schottky anomalies of $C(T)$ at around 13 K are moderately reproduced with the CEF level scheme determined for $NdCo_2Zn_{20}$. The intersite magnetic interaction parameter K is estimated from the $\chi(T)$ and $M(B)$ data. The positive values of K for $x \geq 0.18$ decrease to almost zero for $x \leq 0.06$. The diluted Nd system $Y_{1-x}Nd_xCo_2Zn_{20}$ for $x \leq 0.06$ becomes a good candidate to study the on-site interaction of Γ_6 doublet ground state of the $4f$ electrons with conduction electrons.

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