Mergers as a Probe of Particle Dark Matter

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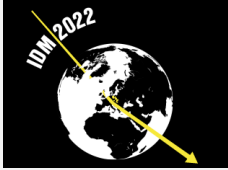
August 27, 2022

Abstract

Black holes below Chandrasekhar mass limit (1.4 $M_\odot$) can not be produced via any standard stellar evolution. Recently, gravitational wave experiments have also discovered unusually low mass black holes whose origin is yet to be known. We propose a simple yet novel formation mechanism of such low mass black holes. Non-annihilating particle dark matter, owing to their interaction with stellar nuclei, can gradually accumulate inside compact stars, and eventually swallows them to low mass black holes, ordinarily impermissible by the Chandrasekhar limit. We point out several avenues to test this proposal, concentrating on the cosmic evolution of the binary merger rates.

1 Introduction

The recent observations of unusually low mass compact objects by the LIGO-VIRGO collaboration [1–3] have ignited interest in the study of low mass black holes (BHs). More interestingly, standard stellar evolution cannot lead to a sub-Chandrasekhar mass BH, and the observation of such a BH would herald new physics. With immense improvement in gravitational wave (GW) astronomy in recent times, the detection of a sub-Chandrasekhar mass BH is possibly forthcoming. Therefore, the key question, assuming a future GW observation involving a sub-Chandrasekhar mass BH, is how to identify its origin?

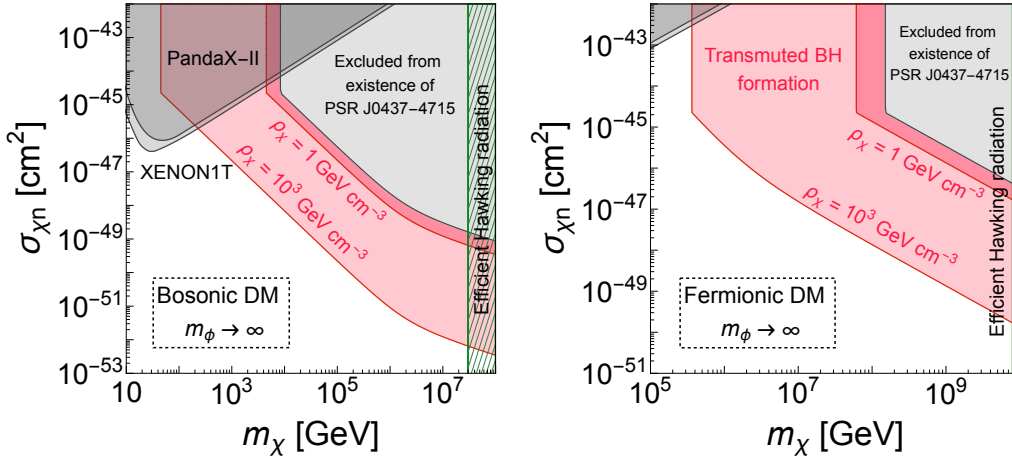



Figure 1: DM mass and scattering cross-section required for a dark core collapse and subsequent transmutation of a $1.3\,M_\odot$ neutron star (NS) to a comparable mass BH are shown in the red shaded regions. The left (right) panel is for bosonic (fermionic) DM, and a contact interaction between DM and the stellar nuclei is assumed. Two representative values of ambient DM density, $\rho_\chi = 1$ and $10^3\,\mathrm{GeV\,cm^{-3}}$ are considered. Exclusion limits from the underground direct detection experiments PandaX-II [13] and XENON1T [14] as well as from existence of an ~ 7 Gyr old [15] nearby pulsar PSR J0437-4715 [16–18] are also shown by the gray shaded regions. Green hatched regions denote the parameter space where efficient Hawking evaporation ceases the implosion of the NS. The figure is taken from [19].

Primordial black holes (PBHs), with no compelling formation mechanisms, are the most accepted explanation of these objects [4–6]. The existing alternative proposals, such as, accretion of fermionic asymmetric DM with non-negligible self-interaction into compact stars [7] or dark atomic cooling [8] are not generic, and appeal to fairly convoluted DM models. Transit of tiny PBHs (PBHs in the mass range of $10^{-15} - 10^{-9} M_\odot$) through a compact star, and subsequent conversion of the compact star to a BH is also thought to be a novel mechanism to produce such low mass BHs [9,10]. However, several recent works [11,12] have falsified this proposal. We point out a simple yet novel mechanism that transmutes a sub-Chandrasekhar or $\mathcal{O}(1)M_\odot$ compact star to a comparable "low mass BH". Non-annihilating particle DM with non-zero interaction strength with the stellar nuclei, a universal feature of the DM models, is sufficient to produce such low mass non-primordial BHs. In the following, we briefly describe the formation mechanism of such low mass BHs, and answer a few basic questions, such as, what particle physics parameter space can they probe, how to test their origin?

2   Formation of Low Mass Transmuted Black Holes

Non-annihilating particle dark matter (DM) [20,21], owing to their interactions with the stellar nuclei, can accumulate inside stellar objects via single [22–25] or multiple [26–28] scatterings with the stellar targets. Inside the stellar core, the captured number of DM particles grow linearly with time. Once the total number of captured DM particles $\left(N_\chi|_{t_{\mathrm{age}}}\right)$ throughout the age of the stellar object $\left(t_{\mathrm{age}}\right)$ satisfies the BH formation criterion, i.e., $N_\chi|_{t_{\mathrm{age}}} \geq \max\left[N_\chi^{\mathrm{self}}, N_\chi^{\mathrm{cha}}\right]$, it ensues a dark core collapse, eventually transmuting the hosts to comparable mass BHs. N_χ^{self} denotes the required number of DM particles for self-gravitation, and is set by the condition

that the captured DM density within the stellar core has to exceed the corresponding baryonic density [17]. Whereas, Chandrasekhar limit, N_χ^{cha}, depends on the spin-statistics of the DM particles, and it is much easier to achieve for bosonic DM as compared to fermionic DM, explaining an easier transmutation for bosonic DM.

Once the number of captured DM particles satisfies the BH formation criterion, dark core collapse initiates, and a tiny BH forms inside the stellar object. This tiny BH accumulates matter from the host, and eventually swallows the host to a comparable mass BH in a very short timescale [29–32]. Such BHs are known as transmuted black holes (TBHs), and depending on the mass of the progenitors, TBHs can naturally be sub-Chandrasekhar, or even sub-solar. However, note that, if the nascent BH that forms via dark core collapse is sufficiently light, it quickly evaporates due to its efficient Hawking emission, ceasing the transmutation. For typical neutron star (NS) parameters, if the initial BH mass is lighter than $\sim 10^{-20} M_\odot$, Hawking evaporation dominates over the swallowing process, and the transmutation ceases [16, 33]. For non-annihilating bosonic and fermionic DM, it corresponds to DM masses $\gtrsim \mathcal{O}(10^7)$ and $\gtrsim \mathcal{O}(10^{10})$ GeV, respectively, providing an upper limit on the DM mass for transmutation. In Fig. 1 we demonstrate the DM parameter space where a NS with mass $1.3 M_\odot$ can transmute to a low mass BH for either bosonic or fermionic DM, for two choices of ambient DM density.

3 Identifying the Origin of Low Mass Black Holes

Formation of sub-Chandrasekhar mass non-primordial BHs via gradual accumulation of non-annihilating DM in compact stars demand a critical investigation to pinpoint the origin of the low mass BHs. In this following, we briefly describe how cosmic evolution of the binary merger rates can be used to determine the origin of low mass BHs.

The merger rate of PBH binaries keeps rising with higher redshift, and it has a universal time dependence of $R_{\mathrm{PBH}} \propto t^{-34/37}$, where t is the coalescence time at formation [36–40]. On the other hand, the merger rate of binary NSs, $R_{\mathrm{NS}}(t)$ [41], as shown in Fig. 2, follows the cosmic star formation rate [34, 42]

$$R_{\mathrm{NS}}(t) = \int_{t_f = t_*}^{t} dt_f \frac{dP_m}{dt}(t - t_f) \lambda \frac{d\rho_*}{dt}(t_f). \tag{1}$$

It peaks at an $\mathcal{O}(1)$ redshift when the star formation rate is maximal. In Eq. (1), $\lambda = 10^{-5} M_\odot^{-1}$ is the number of merging NS binaries per unit star forming mass, $\frac{d\rho_*}{dt}(t_f)$ denotes the cosmic star formation rate at the binary formation time t_f [34], and $\frac{dP_m}{dt}(t - t_f) \propto (t - t_f)^{-1}$ denotes the probability density distribution of coalescing BNSs within the time interval $(t - t_f)$ after formation. The earliest star formation time t_* is taken as 4.9×10^8 year which corresponds to $z_* = 10$ [41].

The merger rate of TBH binaries, $R_{\mathrm{TBH}}(t)$, depends on the particle DM parameters such as DM mass (m_χ), and DM-nucleon interaction strength $(\sigma_{\chi n})$ via the transmutation time (τ_{trans}), as well as on the astrophysical parameters such as the merger rate of binary NSs. $R_{\mathrm{TBH}}(t)$ is systematically lower than $R_{\mathrm{NS}}(t)$, as only a fraction of the binary NS implode depending on the time required for transmutation. This fraction depends on the binary NS population in the galaxies, as well as evolution of the DM density in the galaxies, and it gradually decreases with higher redshifts as NS binaries at higher redshift do not have the sufficient time to accumulate enough DM required for implosion. Hence, $R_{\mathrm{TBH}}(t)$ takes the form

$$R_{\mathrm{TBH}}(t) = \sum_i f_i \int_{t_f = t_*}^{t} dt_f \frac{dP_m}{dt}(t - t_f) \lambda \frac{d\rho_*}{dt}(t_f) \times \Theta\left\{t - t_f - \tau_{\mathrm{trans}}\left[m_\chi, \sigma_{\chi n}, \rho_{\mathrm{ext},i}(t)\right]\right\},$$

$$\tag{2}$$

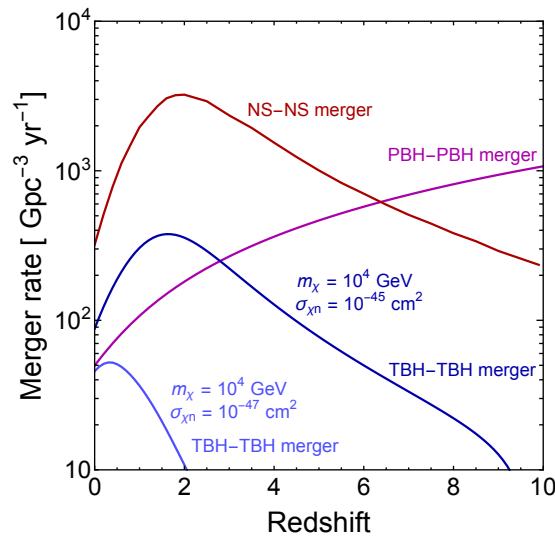



Figure 2: Cosmic evolution of the binary merger rates provides a novel technique to determine the stellar or primordial origin of low mass BHs. Cosmic evolution of the binary PBH, NS, and TBH merger rates are shown in the redshift range of 0 to 10. For the binary NS and TBH merger rate, cosmic star formation rate is adopted from [34] and they are normalized to the recent LIGO-VIRGO measurement [35]. Non-annihilating bosonic DM with mass of 10 TeV and DM-nucleon scattering cross-section of 10^{-45} and 10^{-47} cm^2 in the contact approximation are assumed for the estimation of binary TBH merger rate. The PBH merger rate is estimated by considering 1.3 $M_\odot$− 1.3 $M_\odot$ PBH binary and a DM fraction $f_{PBH} = 10^{-3}$. The figure is taken from [19].

In Eq. (2), we assume that the binary NSs reside in Milky-Way-like galaxies, and are uniformly distributed in $r = (0.01, 0.1)$ kpc, where r is the Galactocentric distance. We also assume that the DM density in each halo (at all redshifts) follows the Navarro-Frenk-White profile [43,44], and the parameters of the Navarro-Frenk-White profile is essentially determined by the time evolution of the Hubble parameter. From the expression for the merger rate, it is evident that $R_{TBH}(t)$ decreases with increase in transmutation time. Therefore, for a given a DM mass, decrease in DM-nucleon scattering cross-section leads to higher τ_{trans}, and, hence, lower R_{TBH}, as shown in Fig. 2. This distinct redshift dependence of the binary merger rates, particularly at higher redshifts, can be measured with the imminent ground as well as space-based GW detectors like Cosmic Explorer [45], Einstein Telescope (ET) [46], and Pre-DECIGO [47], enabling them to distinguish the transmutation scenario from PBHs.

4 Conclusion

Sub-Chandrasekhar mass BHs cannot be described via any standard stellar evolution and will augur new physics. The existing alternative proposals are either not effective or appeal to fairly convoluted DM models. Here, we study a simple yet novel production mechanism for sub-Chandrasekhar mass non-primordial BHs. Gradual accumulation of non-annihilating particle DM inside compact stars can lead to transmutation of compact stars via dark core collapse, and that can give rise to low mass BHs. Cosmic evolution of the binary merger rates can be used as a novel probe to determine the origin of such low mass BHs. We demonstrate that meeasurement of the high-redshift binary merger rates by the imminent GW detectors can conclusively shed light on this topic.

Acknowledgments

A.R. wishes to thank his collaborators Basudeb Dasgupta, Aritra Gupta, and Ranjan Laha for valuable contributions in the original works [16, 19, 28].

References

[1] B. P. Abbott *et al.*, *GW190425: Observation of a Compact Binary Coalescence with Total Mass* $\sim 3.4 M_\odot$, Astrophys. J. Lett. **892**(1), L3 (2020), doi:10.3847/2041-8213/ab75f5, 2001.01761.

[2] R. Abbott *et al.*, *GW190814: Gravitational Waves from the Coalescence of a 23 Solar Mass Black Hole with a 2.6 Solar Mass Compact Object*, Astrophys. J. Lett. **896**(2), L44 (2020), doi:10.3847/2041-8213/ab960f, 2006.12611.

[3] R. Abbott *et al.*, *Observation of Gravitational Waves from Two Neutron Star–Black Hole Coalescences*, Astrophys. J. Lett. **915**(1), L5 (2021), doi:10.3847/2041-8213/ac082e, 2106.15163.

[4] Y. B. Zel'dovich and I. D. Novikov, *The Hypothesis of Cores Retarded during Expansion and the Hot Cosmological Model*, Soviet Astronomy **10**, 602 (1967).

[5] S. Hawking, *Gravitationally collapsed objects of very low mass*, Mon. Not. Roy. Astron. Soc. **152**, 75 (1971).

[6] G. F. Chapline, *Cosmological effects of primordial black holes*, Nature **253**(5489), 251 (1975), doi:10.1038/253251a0.

[7] C. Kouvaris, P. Tinyakov and M. H. Tytgat, *NonPrimordial Solar Mass Black Holes*, Phys. Rev. Lett. **121**(22), 221102 (2018), doi:10.1103/PhysRevLett.121.221102, 1804.06740.

[8] S. Shandera, D. Jeong and H. S. G. Gebhardt, *Gravitational Waves from Binary Mergers of Subsolar Mass Dark Black Holes*, Phys. Rev. Lett. **120**(24), 241102 (2018), doi:10.1103/PhysRevLett.120.241102, 1802.08206.

[9] F. Capela, M. Pshirkov and P. Tinyakov, *Constraints on primordial black holes as dark matter candidates from capture by neutron stars*, Phys. Rev. D **87**(12), 123524 (2013), doi:10.1103/PhysRevD.87.123524, 1301.4984.

[10] V. Takhistov, *Transmuted Gravity Wave Signals from Primordial Black Holes*, Phys. Lett. B **782**, 77 (2018), doi:10.1016/j.physletb.2018.05.026, 1707.05849.

[11] P. Montero-Camacho, X. Fang, G. Vasquez, M. Silva and C. M. Hirata, *Revisiting constraints on asteroid-mass primordial black holes as dark matter candidates*, JCAP **08**, 031 (2019), doi:10.1088/1475-7516/2019/08/031, 1906.05950.

[12] Y. Génolini, P. Serpico and P. Tinyakov, *Revisiting primordial black hole capture into neutron stars*, Phys. Rev. D **102**(8), 083004 (2020), doi:10.1103/PhysRevD.102.083004, 2006.16975.

[13] X. Ren *et al.*, *Constraining Dark Matter Models with a Light Mediator at the PandaX-II Experiment*, Phys. Rev. Lett. **121**(2), 021304 (2018), doi:10.1103/PhysRevLett.121.021304, 1802.06912.

[14] E. Aprile *et al.*, *Dark Matter Search Results from a One Ton-Year Exposure of XENON1T*, Phys. Rev. Lett. **121**(11), 111302 (2018), doi:10.1103/PhysRevLett.121.111302, 1805.12562.

[15] R. N. Manchester, G. B. Hobbs, A. Teoh and M. Hobbs, *The Australia Telescope National Facility pulsar catalogue*, Astron. J. **129**, 1993 (2005), doi:10.1086/428488, astro-ph/0412641.

[16] B. Dasgupta, A. Gupta and A. Ray, *Dark matter capture in celestial objects: light mediators, self-interactions, and complementarity with direct detection*, JCAP **10**, 023 (2020), doi:10.1088/1475-7516/2020/10/023, 2006.10773.

[17] S. D. McDermott, H.-B. Yu and K. M. Zurek, *Constraints on Scalar Asymmetric Dark Matter from Black Hole Formation in Neutron Stars*, Phys. Rev. **D85**, 023519 (2012), doi:10.1103/PhysRevD.85.023519, 1103.5472.

[18] R. Garani, Y. Genolini and T. Hambye, *New Analysis of Neutron Star Constraints on Asymmetric Dark Matter*, JCAP **1905**(05), 035 (2019), doi:10.1088/1475-7516/2019/05/035, 1812.08773.

[19] B. Dasgupta, R. Laha and A. Ray, *Low Mass Black Holes from Dark Core Collapse*, Phys. Rev. Lett. **126**(14), 141105 (2021), doi:10.1103/PhysRevLett.126.141105, 2009.01825.

[20] K. Petraki and R. R. Volkas, *Review of asymmetric dark matter*, Int. J. Mod. Phys. A **28**, 1330028 (2013), doi:10.1142/S0217751X13300287, 1305.4939.

[21] K. M. Zurek, *Asymmetric Dark Matter: Theories, Signatures, and Constraints*, Phys. Rept. **537**, 91 (2014), doi:10.1016/j.physrep.2013.12.001, 1308.0338.

[22] W. H. Press and D. N. Spergel, *Capture by the sun of a galactic population of weakly interacting massive particles*, Astrophys. J. **296**, 679 (1985), doi:10.1086/163485, [,277(1985)].

[23] A. Gould, *Resonant enhancements in weakly interacting massive particle capture by the earth*, Astrophys. J. **321**, 571 (1987), doi:10.1086/165653.

[24] N. F. Bell, G. Busoni, S. Robles and M. Virgato, *Improved Treatment of Dark Matter Capture in Neutron Stars II: Leptonic Targets*, JCAP **03**, 086 (2021), doi:10.1088/1475-7516/2021/03/086, 2010.13257.

[25] N. F. Bell, G. Busoni, T. F. Motta, S. Robles, A. W. Thomas and M. Virgato, *Nucleon Structure and Strong Interactions in Dark Matter Capture in Neutron Stars*, Phys. Rev. Lett. **127**(11), 111803 (2021), doi:10.1103/PhysRevLett.127.111803, 2012.08918.

[26] J. Bramante, A. Delgado and A. Martin, *Multiscatter stellar capture of dark matter*, Phys. Rev. **D96**(6), 063002 (2017), doi:10.1103/PhysRevD.96.063002, 1703.04043.

[27] C. Ilie, J. Pilawa and S. Zhang, *Comment on "Multiscatter stellar capture of dark matter"*, Phys. Rev. D **102**(4), 048301 (2020), doi:10.1103/PhysRevD.102.048301, 2005.05946.

[28] B. Dasgupta, A. Gupta and A. Ray, *Dark matter capture in celestial objects: Improved treatment of multiple scattering and updated constraints from white dwarfs*, JCAP **1908**, 018 (2019), doi:10.1088/1475-7516/2019/08/018, 1906.04204.

[29] T. W. Baumgarte and S. L. Shapiro, *Neutron Stars Harboring a Primordial Black Hole: Maximum Survival Time*, Phys. Rev. D **103**(8), L081303 (2021), doi:10.1103/PhysRevD.103.L081303, 2101.12220.

[30] C. B. Richards, T. W. Baumgarte and S. L. Shapiro, *Accretion onto a small black hole at the center of a neutron star*, Phys. Rev. D **103**(10), 104009 (2021), doi:10.1103/PhysRevD.103.104009, 2102.09574.

[31] S. C. Schnauck, T. W. Baumgarte and S. L. Shapiro, *Accretion onto black holes inside neutron stars with piecewise-polytropic equations of state: Analytic and numerical treatments*, Phys. Rev. D **104**(12), 123021 (2021), doi:10.1103/PhysRevD.104.123021, 2110.08285.

[32] P. Giffin, J. Lloyd, S. D. McDermott and S. Profumo, *Neutron Star Quantum Death by Small Black Holes* (2021), 2105.06504.

[33] C. Kouvaris and P. Tinyakov, *Constraining Asymmetric Dark Matter through observations of compact stars*, Phys. Rev. D **83**, 083512 (2011), doi:10.1103/PhysRevD.83.083512, 1012.2039.

[34] P. Madau and M. Dickinson, *Cosmic Star Formation History*, Ann. Rev. Astron. Astrophys. **52**, 415 (2014), doi:10.1146/annurev-astro-081811-125615, 1403.0007.

[35] R. Abbott *et al.*, *Population Properties of Compact Objects from the Second LIGO-Virgo Gravitational-Wave Transient Catalog*, Astrophys. J. Lett. **913**(1), L7 (2021), doi:10.3847/2041-8213/abe949, 2010.14533.

[36] Z.-C. Chen and Q.-G. Huang, *Merger Rate Distribution of Primordial-Black-Hole Binaries*, Astrophys. J. **864**(1), 61 (2018), doi:10.3847/1538-4357/aad6e2, 1801.10327.

[37] M. Raidal, C. Spethmann, V. Vaskonen and H. Veermäe, *Formation and Evolution of Primordial Black Hole Binaries in the Early Universe*, JCAP **02**, 018 (2019), doi:10.1088/1475-7516/2019/02/018, 1812.01930.

[38] M. Sasaki, T. Suyama, T. Tanaka and S. Yokoyama, *Primordial Black Hole Scenario for the Gravitational-Wave Event GW150914*, Phys. Rev. Lett. **117**(6), 061101 (2016), doi:10.1103/PhysRevLett.117.061101, [Erratum: Phys.Rev.Lett. 121, 059901 (2018)], 1603.08338.

[39] Y. Ali-Haïmoud, E. D. Kovetz and M. Kamionkowski, *Merger rate of primordial black-hole binaries*, Phys. Rev. D **96**(12), 123523 (2017), doi:10.1103/PhysRevD.96.123523, 1709.06576.

[40] M. Sasaki, T. Suyama, T. Tanaka and S. Yokoyama, *Primordial black holes—perspectives in gravitational wave astronomy*, Class. Quant. Grav. **35**(6), 063001 (2018), doi:10.1088/1361-6382/aaa7b4, 1801.05235.

[41] S. R. Taylor and J. R. Gair, *Cosmology with the lights off: standard sirens in the Einstein Telescope era*, Phys. Rev. D **86**, 023502 (2012), doi:10.1103/PhysRevD.86.023502, 1204.6739.

[42] C. Porciani and P. Madau, *On the Association of gamma-ray bursts with massive stars: implications for number counts and lensing statistics*, Astrophys. J. **548**, 522 (2001), doi:10.1086/319027, astro-ph/0008294.

[43] J. F. Navarro, C. S. Frenk and S. D. M. White, *The Structure of cold dark matter halos*, Astrophys. J. **462**, 563 (1996), doi:10.1086/177173, astro-ph/9508025.

[44] J. F. Navarro, C. S. Frenk and S. D. M. White, *A Universal density profile from hierarchical clustering*, Astrophys. J. **490**, 493 (1997), doi:10.1086/304888, astro-ph/9611107.

[45] M. Evans *et al.*, *A Horizon Study for Cosmic Explorer: Science, Observatories, and Community* (2021), 2109.09882.

[46] M. Maggiore *et al.*, *Science Case for the Einstein Telescope*, JCAP **03**, 050 (2020), doi:10.1088/1475-7516/2020/03/050, 1912.02622.

[47] T. Nakamura *et al.*, *Pre-DECIGO can get the smoking gun to decide the astrophysical or cosmological origin of GW150914-like binary black holes*, PTEP **2016**(9), 093E01 (2016), doi:10.1093/ptep/ptw127, 1607.00897.