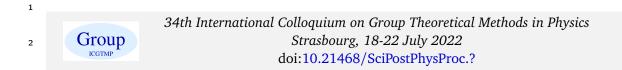
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Abstract 3

Dominant shapes naturally emerge in atomic nuclei from first principles, thereby es-4 tablishing the shape-preserving symplectic $Sp(3,\mathbb{R})$ symmetry as remarkably ubiquitous 5 and almost perfect symmetry in nuclei. We discuss the critical role of this emergent 6 symmetry in enabling machine-learning descriptions of heavy nuclei, ab initio modeling 7 of α clustering and collectivity, as well as tests of beyond-the-standard-model physics. 8 In addition, the $Sp(3,\mathbb{R})$ and SU(3) symmetries provide relevant degrees of freedom 9 that underpin the *ab initio* symmetry-adapted no-core shell model with the remarkable 10 capability of reaching nuclei and reaction fragments beyond the lightest and close-to-11 spherical species. 12

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Introduction 1 15 Emergent symmetries in nuclei: $Sp(3, \mathbb{R})$ and SU(3)2 16 2.1 SU(3) scheme 17 2.2 $Sp(3,\mathbb{R})$ scheme 18 Ab initio symmetry-adapted no-core shell model 2.3

Critical Role of Symmetries for Studies and Predictions of Nuclear Properties 3 20 3.1 Machine learning pattern recognition with the SA-NCSM 21 Probing clustering and physics beyond the standard model 3.2 22 Optical potential in the symmetry-adapted framework for nuclear reactions 3.3 23

Conclusion 24

Contents

11

2

3

3

4

7

8

8

9

10

25 References

26 27

Submission

28 1 Introduction

Dominant shapes, often very few in number, naturally emerge in atomic nuclei. This remark-29 able result has been recently shown by large-scale nuclear simulations from first principles [1]. 30 Indeed, each nuclear shape respects an exact symmetry, namely, the symplectic $Sp(3,\mathbb{R})$ sym-31 metry [2, 3]. Thereby the outcome of these simulations establishes the symplectic $Sp(3,\mathbb{R})$ 32 symmetry as remarkably ubiquitous and almost perfect symmetry in nuclei up through the 33 calcium region (anticipated to hold even stronger in heavy nuclei [4]). This outcome also 34 exposes for the first time the fundamental role of the $Sp(3,\mathbb{R})$ symmetry and suggests that its 35 origin is rooted in the strong nuclear force, in the low-energy regime. 36

This builds upon a decades-long research, starting with the pivotal work of Draayer [5,3,37 (6,7) and that of Rowe and Rosensteel [2,8,4,9], who have successfully harnessed group the-38 ory as a powerful tool for understanding and computing the intricate structure of nuclei. This 39 pioneering work has been instrumental in designing the theory that underpins many highly 40 ordered patterns unveiled amidst the large body of experimental data [10, 11, 12]. In addi-41 tion, it has explained phenomena observed in energy spectra, E2 transitions and deformation, 42 giant resonances (GR), scissor modes and M1 transitions, electron scattering form factors, as 43 well as the interplay of pairing with collectivity. The new developments and insights have 44 provided the critical structure raised upon the very foundation laid by Elliott [13, 14, 15] 45 and Hecht [16, 17], and opened the path for large-scale calculations feasible today on super-46 computers. And while these earlier algebraic models have been very successful in explaining 47 dominant nuclear patterns, they have assumed symmetry-based approximations and have of-48 ten neglected symmetry mixing. This establishes Sp(3, \mathbb{R}) as an effective symmetry¹ for nuclei, 49 which may or may not be badly broken in realistic calculations. It is then imperative to probe 50 if this symmetry naturally arises within an *ab initio* framework, which will, in turn, establish 51 its fundamental role. 52

Indeed, within an *ab initio* framework without *a priori* symmetry assumptions, the symmetryadapted no-core shell model (SA-NCSM) [19, 20, 7] with chiral effective field theory (EFT) interactions [21, 22, 23] has recently confirmed the goodness of the symplectic Sp(3, ℝ) symmetry that is only slightly broken. With no parameters to adjust, the SA-NCSM is capable then not only to explain but also to predict the emergence of nuclear shapes and collectivity across nuclei, even in close-to-spherical nuclear states without any recognizable rotational properties.

Within an *ab initio* framework, the emergent symmetries play a critical role, as they can 60 inform relevant degrees of freedom. In particular, a symmetry-adapted many-body basis can 61 be employed, as in the SA-NCSM, thereby providing solutions for drastically reduced sizes of 62 the spaces in which particles reside (referred to as "model spaces") compared to the corre-63 sponding ultra-large model spaces, without compromising the accuracy of results for various 64 nuclear observables. By exploiting symplectic symmetry, ab initio descriptions of spherical 65 and deformed nuclei up through the calcium region are now possible without the use of effec-66 tive charges [20, 24, 25, 7, 26]. This allows the SA-NCSM to accommodate even larger model 67

¹ A familiar example for an effective symmetry is SU(3). While the Elliott model with a single SU(3) irrep explains ground-state rotational states in deformed nuclei, the SU(3) symmetry is, in general, largely mixed, mainly due to the spin-orbit interaction (nonetheless, SU(3) has been shown to be an excellent quasi-dynamical symmetry, that is, each rotational state has almost the same SU(3) content [18]).

spaces and to reach heavier nuclei, such as ²⁰Ne [1], ²¹Mg [27], ²²Mg [28], ²⁸Mg [29], as
 well as ³²Ne and ⁴⁸Ti [30].

In this paper, we briefly outline the SU(3) and Sp($3, \mathbb{R}$) schemes utilized by the *ab initio* SA-NCSM. We overview the critical role of the emergent Sp($3, \mathbb{R}$) symmetry in enabling machine-learning descriptions of heavy nuclei [31], *ab initio* modeling of α clustering and collectivity, along with tests of beyond-the-standard-model physics [32]. In addition, we show that with the help of the SA-NCSM, which expands *ab initio* applications up to medium-mass nuclei by using the dominant symmetry of nuclear dynamics, one can provide solutions to reaction processes in this region, with a focus on elastic neutron scattering.

2 Emergent symmetries in nuclei: $Sp(3,\mathbb{R})$ and SU(3)

78 2.1 SU(3) scheme

It is well known that SU(3) [13, 33, 5, 34, 17] is the symmetry group of the spherical har-79 monic oscillator (HO) that underpins the valence-shell model and the valence-shell SU(3) 80 (Elliott) model [13, 14, 15] (for technical details of SU(3), see Ref. [35]). The Elliott model 81 has been shown to naturally describe rotations of a deformed nucleus without the need for 82 breaking rotational symmetry. But even beyond the valence shell, the SU(3) scheme pro-83 vides a classification of the complete shell-model space in multiple shells, and is related to 84 the LS-coupling and *j*-coupling schemes via a unitary transformation. It divides the space 85 into basis states of definite $(\lambda \mu)$ quantum numbers of SU(3) that are linked to the intrinsic 86 quadrupole deformation according to the established mapping [36, 37, 38]. For example, the 87 simplest cases, (00), $(\lambda 0)$, and (0μ) , describe spherical, prolate, and oblate deformation, 88 respectively², while a general nuclear state is typically a superposition of several hundred 89 various triaxially deformed configurations. Note that, in this respect, basis states can have 90 little to no deformation, and, e.g., about 60% of the ground state of the closed-shell 16 O is 91 described by a single SU(3) basis state, the spherical (00). 92

Specifically, in the SU(3) scheme, in place of the spherical quantum numbers $|\eta l m_l\rangle$, one 93 can consider the single-particle HO basis $|\eta_z \eta_x \eta_y\rangle$, the HO quanta in the three Cartesian directions, z, x, and y, with $\eta_x + \eta_y + \eta_z = \eta$ ($\eta = 0, 1, 2, ...$ for s, p, sd, ... shells). 94 95 For a given HO major shell, the complete shell-model space is then specified by all distin-96 guishable distributions of η_z , η_x and η_y . E.g., for $\eta = 2$, there are 6 different distributions, 97 $(\eta_z, \eta_x, \eta_y) = (2, 0, 0), (1, 1, 0), (1, 0, 1), (0, 2, 0), (0, 1, 1)$ and (0, 0, 2). The number of these 98 configurations is $\Omega_{\eta} = (\eta + 1)(\eta + 2)/2$ (spatial degeneracy) and the associated symmetry is 99 described by the $U(\Omega_{\eta})$ unitary group. Each of these (η_z, η_x, η_y) configurations can be either 100 unoccupied or has maximum of two particles with spins $\uparrow\downarrow$. 101

As a simple example for an SU(3)-scheme basis state, consider A = 2 protons in the *sd* shell ($\eta = 2$) with a particle in the (2,0,0) level with spin \uparrow and another in the (1,1,0) level with spins \uparrow . The total number of quanta in each direction is $(\eta_z^{\text{tot}}, \eta_x^{\text{tot}}, \eta_y^{\text{tot}},) = (3,1,0)$, or equivalently, $\eta^{\text{tot}}(\lambda\mu) = 4(21)$, where $\eta^{\text{tot}} = \eta_x^{\text{tot}} + \eta_y^{\text{tot}} + \eta_z^{\text{tot}}$, together with $\lambda = \eta_z^{\text{tot}} - \eta_x^{\text{tot}}$ and $\mu = \eta_x^{\text{tot}} - \eta_y^{\text{tot}}$ labeling an SU(3) irrep, in addition to the total intrinsic spin and its projection SM_S. For given $(\lambda\mu)$, the quantum numbers κ , L and M_L are given by Elliott [13,14], according to the SU(3) $\stackrel{\kappa}{\supset}$ SO(3)_L \supset SO(2)_{M_L}, where the label κ distinguishes multiple occurrences of the same orbital momentum L in the parent irrep $(\lambda\mu)$. For our example, $(\lambda\mu) = (21)$ with $\kappa = 1$, L = 1, 2, 3, and $M_L = -L, -L + 1, \dots, L$. Hence, the set $\{\eta^A(\lambda\mu)\kappa(LS)JM\}$

² Following this mapping, quadrupole moments of (00), (λ 0), and (0 μ) configurations – in a simple classical analogy to rotating spherical, prolate, and oblate spheroids in the lab frame [39] – are zero, negative, and positive, respectively.

completely labels a 2-proton SU(3)-scheme basis state (with $\eta^{\text{tot}} = A\eta$). A basis state in this scheme for a 2-particle system is given by, $\{a_{(\eta\,0)st_z}^{\dagger} \times a_{(\eta'0)s't'_z}^{\dagger}\}^{(\lambda\mu)\kappa(LS)JM}|0\rangle$, which is an SU(3)-coupled product, provided that a^{\dagger} is a proper SU(3) tensor; incidentally, the SU(3) tensor a^{\dagger} of rank $(\lambda\mu) = (\eta\,0)$ coincides with the familiar particle creation operator, $a_{(\eta\,0)lms\sigma t_z}^{\dagger} \equiv a_{\eta lms\sigma t_z}^{\dagger}$, while the particle annihilation SU(3) tensor of rank $(\lambda\mu) = (0\,\eta)$ is given as $\tilde{a}_{(0\,\eta)l-ms-\sigma t_z} = (-1)^{\eta+l-m+s-\sigma}a_{\eta lms\sigma t_z}$. Note that for $\eta = \eta' = 2$, e.g., there are only a few 2-proton configurations $(\lambda\mu) = (40)$ with L = 0, 2, 4, (21) with L = 1, 2, 3, and (02)with L = 0, 2. Furthermore, these basis states are related to *LS*-coupled basis states (similarly, to *jj*-coupled basis states) via a simple unitary transformation,

$$\{a_{(\eta\,0)st_{z}}^{\dagger} \times a_{(\eta'0)s't_{z}'}^{\dagger}\}^{(\lambda\,\mu)\kappa(LS)JM} |0\rangle = \sum_{l,l'} \langle (\eta\,0)l; (\eta'0)l' \| (\lambda\,\mu)\kappa L \rangle \{a_{\eta lst_{z}}^{\dagger} \times a_{\eta'l's't_{z}'}^{\dagger}\}^{(LS)JM} |0\rangle,$$
(1)

where $\langle ...; ... || ... \rangle$ is the SU(3) analog of the familiar reduced Clebsch-Gordan coefficient [note that there is no dependence on the particle orbital momenta, *l* and *l'*, in the SU(3)scheme basis states].

An important feature of the SU(3) scheme is that all possible configurations within a major HO shell η (for protons or neutrons) are not constructed using the tedious procedure of coupling of creation operators referenced above, but are readily available based on the $U(\Omega_{\eta})$ unitary group of the many-body three-dimensional HO. In particular, the basis construction is implemented according to the reduction [40]

with SU(3)_{$(\lambda_{\eta}\mu_{\eta})$} $\stackrel{\kappa_{\eta}}{\supset}$ SO(3)_{L_{η}} \supset SO(2)_{$M_{L_{\eta}}$} [13, 14], where a multiplicity index α_{η} distinguishes multiple occurrences of an SU(3) irrep ($\lambda_{\eta}\mu_{\eta}$) in a given U(Ω_{η}) irrep labeled by Young tableaux, [**f**] = [$f_1, f_2, \ldots, f_{\Omega_{\eta}}$], with $f_1 \ge f_2 \ge \cdots \ge f_{\Omega_{\eta}}$ and $f_i = 0$ (unoccupied), 1 (occupied by a particle), or 2 (occupied by 2 particles of spins $\uparrow\downarrow$). An illustrative example for 4 particles in the pf shell ($\eta = 3$) is shown in Table 1.

133 **2.2** Sp $(3, \mathbb{R})$ scheme

The key role of deformation in nuclei and the coexistence of low-lying quantum states in a single nucleus characterized by configurations with different quadrupole moments [10] makes the quadrupole moment a dominant fundamental property of the nucleus. Hence, the quadrupole moment Q (or deformation) and the monopole moment r^2 (or "size" of the nucleus), along with nuclear masses, establishes the energy scale of the nuclear problem. Indeed, the nuclear monopole and quadrupole moments underpin the essence of symplectic Sp(3, \mathbb{R}) symmetry.

Specifically, for *A* particles in three-dimensional space, the complete basis for the shell model is described by Sp(3*A*, \mathbb{R})×U(4) [9], where Sp(3*A*, \mathbb{R}) is the group of all linear canonical transformations of the 3*A*-particle phase space and Wigner's supermultiplet group U(4) describes the complementary spin-isospin space. A complete translationally invariant shell-

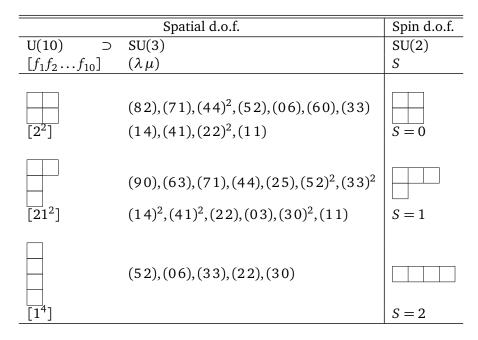


Table 1: $SU(3) \times SU(2)_S$ configurations for 4 protons (neutrons) in the *pf* shell $(\eta = 3 \text{ with } \Omega_\eta = 10)$. Note that a spatial symmetry represented by a Young tableau $[f_1, \ldots, f_{\Omega_\eta}]$ is uniquely determined by its complementary spin symmetry of a given intrinsic spin S_η (conjugate Young tableaux) ensuring the overall antisymmetrization of each $U(\Omega_\eta) \times SU(2)_{S_\eta}$ configuration with respect to spatial and spin degrees of freedom (d.o.f.) [40].

¹⁴⁵ model basis is classified according to (see, e.g., [4,9]),

$$\begin{array}{rcl} \operatorname{Sp}(3(A-1),\mathbb{R}) & \times & \operatorname{U}(4) \\ & & \cup & & \\ \operatorname{Sp}(3,\mathbb{R}) \times \operatorname{O}(A-1) & & \operatorname{SU}(2)_S \times \operatorname{SU}(2)_T \end{array}$$
(3)

The Sp $(3, \mathbb{R})$ scheme utilizes the symplectic group Sp $(3, \mathbb{R})$. It consists of all *particle-independent* linear canonical transformations of the single-particle phase-space observables, the positions

¹⁴⁸ \vec{r}_i and momenta \vec{p}_i (with particle index i = 1, ..., A and spacial directions $\alpha, \beta = x, y, z$)

$$r'_{i\alpha} = \sum_{\beta} A_{\alpha\beta} r_{i\beta} + B_{\alpha\beta} p_{i\beta}$$
(4)

$$p'_{i\alpha} = \sum_{\beta} C_{\alpha\beta} r_{i\beta} + D_{\alpha\beta} p_{i\beta}$$
(5)

that preserve the Heisenberg commutation relations $[r_{i\alpha}, p_{j\beta}] = i\hbar \delta_{ij} \delta_{\alpha\beta}$ [4, 41, 7]. Gen-149 erators of these transformations, symbolically denoted as matrices A, B, C, and D, are con-150 structed as "quadratic coordinates" in phase space, $\vec{r_i}$ and $\vec{p_i}$, and, most importantly, sum 151 over all the particles and act on the space orientation. Hence, the generators include phys-152 ically relevant operators: the total kinetic energy $(\frac{p^2}{2} = \frac{1}{2}\sum_i \vec{p}_i \cdot \vec{p}_i)$, the monopole moment 153 $(r^2 = \sum_i \vec{r_i} \cdot \vec{r_i})$, the quadrupole moment $(Q_{2M} = \sqrt{16\pi/5} \sum_i r_i^2 Y_{2M}(\hat{r_i}))$, the orbital momen-154 tum ($\vec{L} = \sum_{i} \vec{r}_{i} \times \vec{p}_{i}$), and the many-body harmonic oscillator Hamiltonian ($H_{0} = \frac{p^{2}}{2} + \frac{r^{2}}{2}$). 155 In addition, other generators describe multi-shell collective vibrations and vorticity degrees of 156 freedom for a description from irrotational to rigid rotor flows. 157

On the contrary, the generators of the complementary O(A) sum over the three spatial 158 directions and act on the particle index, with a growing complexity with increasing parti-159 cle number. One can then organize the A-particle model space according to the dual group 160 O(A-1), with $O(A) \supset O(A-1) \supset S_A$. The O(A) is the group of orthogonal transformations that 161 act on the "particle-index" space (transformations of nucleon coordinates, $r_{i\alpha} \rightarrow \sum_{j=1}^{A} r_{j\alpha} P_{ji}$, 162 that leave the O(A) scalars $r_{\alpha} \cdot r_{\beta} = \sum_{i=1}^{A} r_{i\alpha} r_{i\beta}$ invariant for $\alpha, \beta = x, y, z$). This scheme is reviewed in detail in Refs. [4,9]. O(A - 1) is the subgroup of O(A) which leaves center-of-163 164 mass coordinates invariant (note that center-of-mass coordinates are symmetric with respect 165 to nucleon indices and, therefore, invariant under S_A permutations) and has as a subgroup 166 the permutation group S_A , which permutes the spatial coordinates of a system of A particles. 167 The Sp $(3, \mathbb{R})$ scheme utilizes an important group reduction to classify many-particle basis 168 states $|\sigma n \rho \omega \kappa L M\rangle$ of a symplectic irrep, 169

$$\begin{array}{lll} \operatorname{Sp}(3,\mathbb{R}) &\supset & U(3) \,\supset \, \operatorname{SO}(3) \,\supset \, \operatorname{SO}(2) \\ \sigma & n\rho & \omega & \kappa & L & M \end{array}, \tag{6}$$

where $\sigma \equiv N_{\sigma} (\lambda_{\sigma} \mu_{\sigma})$ labels the Sp(3, \mathbb{R}) irrep, $n \equiv N_n (\lambda_n \mu_n)$, $\omega \equiv N (\lambda_{\omega} \mu_{\omega})$, and $N = N_{\sigma} + N_n$ is the total number of HO quanta (ρ and κ are multiplicity labels) [4]. The relation of these symplectic basis states to *M*-scheme states of the NCSM is provided in Ref. [42]. Importantly, a single-particle Sp(3, \mathbb{R}) irrep spans *all* positive-parity (or negative-parity) states for a particle in a three-dimensional spherical or triaxial (deformed) harmonic oscillator. The translationally invariant (intrinsic) symplectic Sp(3, \mathbb{R}) generators can be written as

¹⁷⁵ SU(3) tensor operators in terms of the harmonic oscillator raising, $b_{i\alpha}^{\dagger(10)} = \frac{1}{\sqrt{2}}(r_{i\alpha} - ip_{i\alpha})$, ¹⁷⁷ and lowering $b^{(01)}$ dimensionless operators (with **r** and **p** the laboratory-frame position and ¹⁷⁸ momentum coordinates and $\alpha = 1, 2, 3$ for the three spatial directions),

$$A_{\mathfrak{L}M}^{(20)} = \frac{1}{\sqrt{2}} \sum_{i=1}^{A} \{b_i^{\dagger} \times b_i^{\dagger}\}_{\mathfrak{L}M}^{(20)} - \frac{1}{\sqrt{2}A} \sum_{s,t=1}^{A} \{b_s^{\dagger} \times b_t^{\dagger}\}_{\mathfrak{L}M}^{(20)}$$

$$C_{\mathfrak{L}M}^{(11)} = \sqrt{2} \sum_{i=1}^{A} \{b_i^{\dagger} \times b_i\}_{\mathfrak{L}M}^{(11)} - \frac{\sqrt{2}}{A} \sum_{s,t=1}^{A} \{b_s^{\dagger} \times b_t\}_{\mathfrak{L}M}^{(11)},$$
(7)

$$H_{00}^{(00)} = \sqrt{3} \sum_{i} \{b_{i}^{\dagger} \times b_{i}\}_{00}^{(00)} - \frac{\sqrt{3}}{A} \sum_{s,t} \{b_{s}^{\dagger} \times b_{t}\}_{00}^{(00)} + \frac{3}{2}(A-1),$$
(8)

together with $B_{\mathcal{L}M}^{(02)} = (-)^{\mathcal{L}-M} (A_{\mathcal{L}-M}^{(20)})^{\dagger}$ ($\mathcal{L} = 0, 2$), where the sums run over all *A* particles of the system. Equivalently, the symplectic generators, being one-body-plus-two-body operators 179 180 can be expressed in terms of the fermion creation operator $a^{\dagger}_{(\eta \, 0)}$ and its SU(3)-conjugate annihilation operator, $\tilde{a}_{(0 \, \eta)}$. This is achieved by using the known matrix elements of the 181 182 position and momentum operators in a HO basis, and hence, e.g., the first sum of $A_{\mathfrak{M}}^{(20)}$ in Eq. (7) becomes, $\sum_{\eta} \sqrt{\frac{(\eta+1)(\eta+2)(\eta+3)(\eta+4)}{12}} \left\{ a_{(\eta+20)}^{\dagger} \times \tilde{a}_{(0\eta)} \right\}_{\mathfrak{M}}^{(20)}$ [43]. Note that this operator describes excitations of a nucleon from the η shell to the $\eta + 2$ shell, which corresponds 183 184 185 to creating two single-particle HO excitation quanta, as manifested in the first term of Eq. 186 (7). The eight $0\hbar\Omega$ operators $C_{\mathcal{L},M}^{(11)}$ ($\mathcal{L} = 1,2$) generate the SU(3) subgroup of Sp(3, \mathbb{R}). 187 They realize the angular momentum operator (dimensionless), $L_{1M} = C_{1M}^{(11)}$, and the Elliott 188 "algebraic" quadrupole moment tensor $Q_{2M}^a = \sqrt{3}C_{2M}^{(11)}$. The many-body basis states of an Sp(3, \mathbb{R}) irrep are built over a bandhead $|\sigma\rangle$ (defined by 189

¹⁹⁰ The many-body basis states of an Sp(3, \mathbb{R}) irrep are built over a bandhead $|\sigma\rangle$ (defined by ¹⁹¹ the usual requirement that the symplectic lowering operators $B_{\mathcal{L}M}^{(02)}$ annihilate it) by $2\hbar\Omega$ 1p-¹⁹² 1h monopole or quadrupole excitations, realized by the first term in $A_{\mathfrak{L}M}^{(20)}$ of Eq. (7), together with a smaller $2\hbar\Omega$ 2p-2h correction for eliminating the spurious center-of-mass (CM) motion, realized by the second term in $A_{\mathfrak{LM}}^{(20)}$:

$$|\sigma n\rho\,\omega\kappa(LS_{\sigma})JM\rangle = \sum_{M_{L}M_{S}} \langle LM_{L}; S_{\sigma}M_{S}|JM\rangle \{\{A^{(20)} \times A^{(20)} \cdots \times A^{(20)}\}^{n} \times |\sigma; S_{\sigma}M_{S}\rangle\}_{\kappa LM_{L}}^{\rho\omega}.$$
(9)

States within a symplectic irrep have the same spin value, which are given by the spin S_{σ} 195 of the bandhead $|\sigma; S_{\sigma}\rangle$. Symplectic basis states span the entire shell-mode space. A com-196 plete set of labels includes additional quantum numbers $|\{\alpha\}\sigma\rangle$ that distinguish different 197 bandheads with the same $N_{\sigma}(\lambda_{\sigma}\,\mu_{\sigma})$. Remarkably, these Sp(3, $\mathbb R$) basis states are in one-198 to-one correspondence with a coupled product of the states of the Bohr vibrational model 199 (realized in terms of giant monopole-quadrupole resonance states with irrotational flows), 200 $\{\{A^{(20)} \times A^{(20)} \cdots \times A^{(20)}\}^n \times |N_{\sigma}(00)\rangle\}^{(\lambda_n \mu_n)}$, and $(\lambda_{\sigma} \mu_{\sigma})$ deformed states of an SU(3) 201 model [41]. 202

203 2.3 Ab initio symmetry-adapted no-core shell model

Not surprisingly, the symplectic Sp(3, R) symmetry, the underlying symmetry of the symplectic rotor model [2,4], has been found to play a key role across the nuclear chart – from the lightest systems [44,45], through intermediate-mass nuclei [3,46,7], up to strongly deformed nuclei of the rare-earth and actinide regions [4, 47, 48, 18]. The results agree with experimental evidence that supports formation of enhanced deformation and clusters in nuclei, as well as vibrational and rotational patterns, as suggested by energy spectra, electric monopole and quadrupole transitions, radii and quadrupole moments [10, 28, 49].

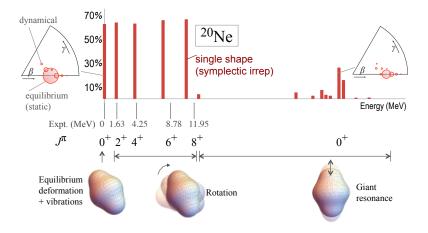


Figure 1: Emergence of almost perfect symplectic $Sp(3, \mathbb{R})$ symmetry in nuclei from first principles, enabling *ab initio* descriptions of collectivity and clustering. Figure adapted from [1].

210

The symmetry-adapted no-core shell model [19, 7, 1] capitalizes on these findings and presents solutions in terms of a physically relevant basis of nuclear shapes. It exploits both the SU(3) and Sp(3, \mathbb{R}) schemes. Indeed, since the symplectic symmetry does not mix nuclear shapes, the novel nuclear feature provides important insight from first principles into the physics of nuclei and their low-lying excitations as dominated by only a few (typically one or two) collective shapes – equilibrium shapes with their vibrations – that rotate (Fig. 1).

By exploiting this almost perfect symmetry, the SA framework resolves the scale explosion problem in nuclear structure calculations, *i.e.*, the explosive growth in computational resource demands with increasing number of particles and model spaces size. We note that the SA-NCSM uses the complete model space (that is, all possible shapes) as usually done in conventional shell models, but expands, in a prescribed way, only for those deformed configurations with vibrations that lie outside of the complete model space. This is critical for enhanced prolate deformation, since spherical and less deformed or oblate shapes easily develop in comparatively small model-space sizes.

The SA-NCSM, when combined with a high-precision realistic inter-nucleon interaction, 225 provides ab initio predictions of nuclear observables. We often adopt the NNLO_{opt} chiral 226 potential [50] that is used without 3N forces, which have been shown to contribute minimally 227 to the 3- and 4-nucleon binding energy [50]. Chiral potentials are typically parameterized 228 by two-nucleon (and three-nucleon) data, whereas the parameters, called the low-energy 229 constants (LECs), remain unchanged and are not adjusted from one many-body system to 230 another. This ensures a predictive power. At the next-to-next-to-leading order (NNLO), there 231 are 14 LECs that enter into the chiral nucleon-nucleon (NN) potential. Our recent findings 232 reveal the remarkable result that the chiral potential parameterizations have no significant 233 effect on the dominant nuclear features, such as nuclear shape and the associated $Sp(3,\mathbb{R})$ 234 symmetry, along with cluster formation (Fig. 2), but only slightly vary details in the nuclear 235 wave functions, such as the contributions of the equilibrium deformation and its vibrations 236 within the predominant nuclear shape (Fig. 2, left, inset) [51].

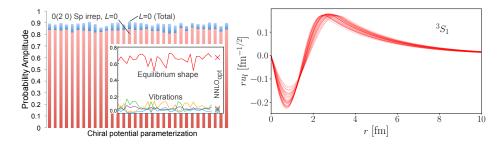


Figure 2: Chiral parameterization independence for nuclear shapes and cluster formation: (Left) Probability amplitude of the predominant Sp(3, \mathbb{R}) irrep $N_{\sigma}(\lambda_{\sigma} \mu_{\sigma}) = 0(20)$ (L = 0) in the ⁶Li 1⁺ ground state. Inset: Contributions from the equilibrium shape (symplectic bandhead) and its vibrations (the case for the NNLO_{opt} is also shown). (Right) $\alpha + d \, {}^{3}S_{1}$ -wave vs. the relative distance r. Calculated from the ⁶Li 1⁺ ground state, computed with the SA-NCSM in the Sp(3, \mathbb{R}) scheme with NNLO chiral potential for 10 HO shells and $\hbar\Omega$ =15 MeV. The ±10% variation in the LECs of the chiral potential is shown (left) on the horizontal axis and (right) by the spread of the curve. Figures adapted from [51].

237

²³⁸ 3 Critical Role of Symmetries for Studies and Predictions of Nu ²³⁹ clear Properties

240 3.1 Machine learning pattern recognition with the SA-NCSM

Machine learning approaches are ideal for pattern recognition, thereby providing a suitable framework to detect and utilize the highly organized patterns in atomic nuclei governed by the symplectic Sp $(3, \mathbb{R})$ symmetry.

Specifically, Ref. [31] introduces a novel machine learning approach to provide further insight into atomic nuclei and to detect orderly patterns amidst a vast data of large-scale calculations. The method utilizes a physics-informed neural network that is trained on *ab* *initio* results from the SA-NCSM for light nuclei. Indeed, the SA-NCSM, which expands *ab initio* applications up to medium-mass nuclei, can reach even heavier nuclei when coupled
with the machine learning approach. In particular, we find that a neural network trained on
probability amplitudes for *s*-and *p*-shell nuclear wave functions not only predicts dominant
configurations for heavier nuclei but in addition, when tested for the ²⁰Ne ground state, it
accurately reproduces the probability distribution (Fig. 3).

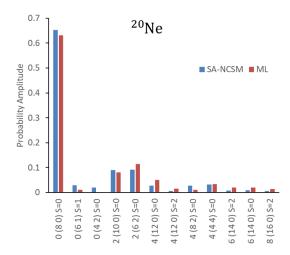


Figure 3: A novel machine learning approach coupled with the *ab initio* SA-NCSM is capable to detect orderly patterns amidst a vast data of large-scale calculations and to describe *sd*-shell nuclei, such as ²⁰Ne (shown), ²⁴Si, ⁴⁰Mg, and even the extremely heavy nuclei such as ^{166,168}Er and ²³⁶U, by training only on nuclei up to ¹⁶O. Figure from [31].

252

The nonnegligible configurations predicted by the network provide an important input to 253 the SA-NCSM for reducing ultra-large model spaces to manageable sizes that can be, in turn, 254 utilized in SA-NCSM calculations to obtain accurate observables. The neural network is ca-255 pable of describing nuclear deformation and is used to track the shape evolution along the 256 $^{20-42}$ Mg isotopic chain, suggesting a shape-coexistence that is more pronounced toward the 257 very neutron-rich isotopes [31]. Furthermore, the neural network provides first descriptions 258 of the structure and deformation of ²⁴Si and ⁴⁰Mg of interest to x-ray burst nucleosynthe-259 sis, and even of the extremely heavy nuclei such as ^{166,168}Er and ²³⁶U, that build upon first 260 principles considerations [31]. 261

262 3.2 Probing clustering and physics beyond the standard model

The left-handed vector minus axial-vector (V-A) structure of the weak interaction was postu-263 lated in late 1950's and early 1960's guided in large part by a series of beta-decay experiments, 264 and later was incorporated in the Standard Model of particle physics. However, in its most 265 general form, the weak interaction can also have scalar, tensor, and pseudoscalar terms as 266 well as right-handed currents. The β decay of ⁸Li to ⁸Be, which subsequently breaks up into 267 two α particles, has long been recognized as an excellent testing ground to search for new 268 physics (e.g. see [52]) due to the high decay energy and the ease of detecting the β and two α 269 particles. These experiments have achieved remarkable precision (e.g., see [53,54]) that now 270 requires confronting the systematic uncertainties that stem from the higher-order corrections 271 in nuclear beta decay that are difficult to measure experimentally. 272

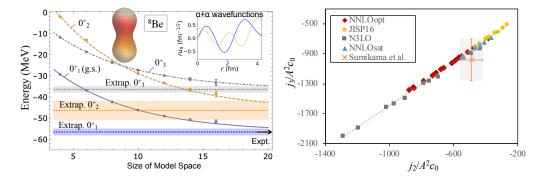


Figure 4: The *ab initio* SA-NCSM places unprecedented constraints on higher-(recoil-) order corrections $(j_2/A^2c_0 \text{ and } j_3/A^2c_0)$ in the β decay of ⁸Li \rightarrow ⁸Be by addressing the challenging $\alpha + \alpha$ structure of ⁸Be. The results are essential for largely improving the sensitivity of high-precision experiments that probe the weak interaction theory and test physics beyond the Standard Model. Calculations performed on the NERSC and Frontera systems. Figures from [32] & [54].

As a remarkable result, the *ab initio* SA-NCSM has recently determined the size of the recoil-order form factors in the β decay of ⁸Li (Fig. 4). It has shown that states of the $\alpha + \alpha$ system not included in the evaluated ⁸Be energy spectrum have an important effect on all $j_{2,3}/A^2c_0$, b/Ac_0 and d/Ac_0 recoil-order terms, and can explain the elusive $M_{\rm GT}$ discrepancy in the A = 8 systems common to all other *ab initio* approaches.

The SA-NCSM outcomes of Ref. [32] reduce – by over 50% – the uncertainty on these recoil-order corrections. These results help improve the sensitivity of high-precision β -decay experiments that probe the V–A structure of the weak interaction in the most stringent limit on tensor current contribution to the weak interaction theory to date, established in Ref. [54]. Furthermore, the SA-NCSM predicted b/Ac_0 and d/Ac_0 values are important for other investigations of the Standard Model symmetries, such as the conserved vector current hypothesis and the existence of second-class currents in the weak interaction.

285 3.3 Optical potential in the symmetry-adapted framework for nuclear reactions

In recent years there has been a significant interest in describing nuclear reactions from ab 286 *initio* approaches, and especially in constructing from first principles effective inter-cluster 287 interactions, often referred to as optical potentials. Ab initio optical potentials for elastic 288 scattering at low energy are of particular interest for experiments at rare isotope beams. To 289 utilize the efficacy of the symmetry-adapted basis, we combine the ab initio symmetry-adapted 290 no-core shell model with the Green's function technique (SANCSM/GF) and construct non-291 local optical potentials rooted in first principles [55,56]. Using the Green's function technique 292 ensures that all relevant cluster partitionings are included in the effective potential between 293 the two reaction fragments (clusters) that are typically in their ground state in the entrance 294 channel. With the view toward studying neutron and proton elastic scattering from deformed 295 and heavy targets, we first examine a target of 4 He (Fig. 5a), where the effect of the spurious 296 center-of-mass motion is most evident. 297

In a complementary symmetry-adapted resonating group method (SA-RGM) framework [58], one starts from an *ab initio* description of all particles involved and derives the effective potential for localized clusters, which are properly normalized and orthogonalized in the particle sector, which yields non-local effective nucleon-nucleus interactions for the cluster partitioning or channel under consideration. For a single channel, if the effects of the target excitations are neglected, the non-local effective nucleon-nucleus interaction can be calcu-

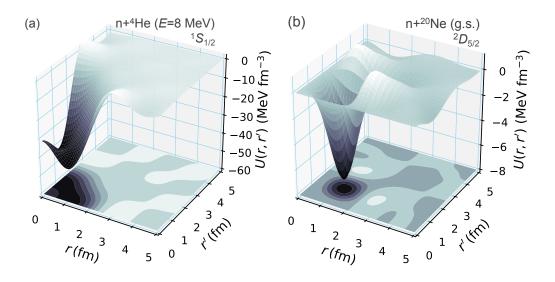


Figure 5: (a) Translationally invariant non-local optical potential for elastic neutron scattering for a ⁴He target at E = 8 MeV center-of-mass energy, calculated in the SA-NCSM with the Green's function technique (10 shells, $\hbar\Omega$ =17MeV). Figure from [55]. (b) Effective neutron-nucleus non-local potential (translationally invariant) for the ²⁰Ne ground state, where effects of the target excitations and antisymmetrization involving three nucleons are neglected (based on *ab initio* SA-NCSM calculations of ²⁰Ne with NNLO_{opt} in a model space of 11 shells and $\hbar\Omega$ =15 MeV inter-shell distance). Figure from [57].

lated for each partial wave, as illustrated for $n+{}^{20}Ne(0^+_{g.s.})$ with NNLO_{opt} in 11 shells (Fig. 5b). While these calculations limit the antisymmetrization to two nucleons only, this is a first step toward constructing effective nucleon-nucleus potentials for light and medium-mass nuclei for the astrophysically relevant energies [59, 60].

308 4 Conclusion

We have discussed the critical role of the emergent $Sp(3,\mathbb{R})$ symmetry in atomic nuclei and 309 the associated subgroup SU(3), which in turn underpin the Sp(3, \mathbb{R}) and SU(3) schemes. 310 By exploiting these schemes, the *ab initio* SA-NCSM has enabled machine-learning pattern 311 recognition and descriptions of heavy nuclei, *ab initio* modeling of α clustering and collectivity, 312 along with tests of beyond-the-standard-model physics. In addition, we show that with the 313 help of the SA-NCSM, which expands ab initio applications up to medium-mass nuclei by using 314 the dominant symmetry of nuclear dynamics, one can provide solutions to reaction processes 315 in this region, with a focus on elastic neutron scattering. 316

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