Sparks in the Dark

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Abstract

This study presents a novel method for the definition of signal regions in searches for new physics at collider experiments. By leveraging multi-dimensional histograms with precise arithmetic and utilizing the SparkDensityTree library, it is possible to identify high-density regions within the available phase space, potentially improving sensitivity to very small signals. Inspired by a search for dark mesons at the ATLAS experiment, CMS open data is used for this proof-of-concept intentionally targeting an already excluded signal. Signal regions are defined based on density estimates of signal and background. These preliminary regions align well with the physical properties of the signal while effectively rejecting background events.

1

² Contents

11

¹² 1 Introduction

 Collider experiments in high-energy physics often deal with large amounts of experimental data. The two general-purpose experiments at CERN's Large Hadron Collider (LHC), ATLAS and CMS, record about 10 PB of data per year. These data are then analysed for, e.g., consistency with different theoretical models, which involves both isolating a small signal from large background and data-driven corrections to background estimates. A pre-selection of data is performed based on the particles involved in the experimental signature of the signal. Subsequently, the resulting dataset is explored with the objective to create a phase-space region enriched in signal events. This enriched region allows for a statistical analysis that is sensitive to the signal. Optimising the region involves using theoretical knowledge of the signatures and kinematic behaviour of the signal and background processes to define new variables, and a tedious process of exploring the data using 1D or 2D histograms. Machine learning classifiers are also commonly used at this stage, which both hone in on the region without the same need for manual optimisation and utilise complex relationships between variables. The downside of these methods is that the interdependence of the variables is never made explicit, and the analysis becomes harder to understand than one defined in terms of intervals in each variable. This matters not only for the understanding of the individual physicist, but also matters for reinterpretations of the results. This paper is a proof-of-concept of a new method which has the potential to produce a more sensitive signal region in a shorter time than manual optimisation, while keeping the analysis and interpretability as simple as possible.

 This work builds on multi-dimensional histograms as implemented in the SparkDen- sityTree library [\[1\]](#page-11-1), following [\[2–](#page-11-2)[4\]](#page-11-3). SparkDensityTree has the following advantages com-pared to other density estimation methods.

 Firstly, unlike most density estimation methods, including various regularization and Bayesian methods based on the likelihood, the minimum distance estimate (MDE) re- turned by SparkDensityTree as a multidimensional histogram is guaranteed to be within an *L*¹ distance or integrated absolute distance bound from the unknown density *f* for any given sample size *n*, no matter what the underlying density *f* happens to be, i.e., $_{41}$ any density in L_1 , the space of Lebesgue integrable functions, and is thus said to have *universal performance guarantees* [\[3\]](#page-11-4).

 Secondly, the method scales to arbitrarily large sample sizes in high dimensions due to a scalable implementation with sparse binary trees for representing the data. A sparse binary tree can represent only the existing data in its leaves by implicitly encoding the unrepresented leaves without data as zero akin to sparse vectors and matrices.

 Thirdly, SparkDensityTree provides various further statistical insights from the MDE. In particular, calculating the coverage or highest density regions of the MDE histogram of the signal and background data allows for finding the region of phase space with the largest probability density in the signal and background. The highest density region covering the 51 sample space for a given probability $1 - \alpha$, should have the smallest possible volume such that every point inside the region should have a probability density at least as large as every point outside the region. The method takes measured or simulated data for signal or background processes as input and returns the highest density region of its density estimate (MDE histogram). The signal region is given as a union of intervals, rectangles, cuboids and hyper-cuboids over the domain of the input variables.

 The current proof-of-concept is largely inspired by a search for dark mesons in ATLAS data [\[5\]](#page-11-5). This search explores prompt decays of dark pions and dark rho mesons into stan- dard model particles in LHC data. The data and simulation used in the following sections, as well as the selections applied, loosely follow the analysis. The full ATLAS analysis is however quite complex, and so, comparing directly with this work is not completely pos- sible. The signal point chosen in this study has already been excluded by ATLAS [\[5\]](#page-11-5), and so the data will be used as background.

⁶⁴ 2 Datasets and event selection

 The dark sector signals searched by ATLAS [\[5\]](#page-11-5) produce two final states: *tttb* and *ttbb*. The one lepton final state is the most sensitive and it is characterized by events with one lepton and from 6 to 8 jets where at least 4 are identified as coming from the decay of a b-quark.

 $\begin{aligned} \n\mathcal{L}_{\mathcal{B}} \text{ is a } \text{P-dual}.\n\end{aligned}$ $\begin{aligned} \n\mathcal{L}_{\mathcal{B}} \text{ is a } \text{P-dual}.\n\end{aligned}$ the CMS experiment [\[6\]](#page-11-6) in 2015 to model the background to the dark meson signal. The analysed data correspond to the SingleElectron [\[7\]](#page-11-7) and SingleMuon [\[8\]](#page-11-8) datasets released on the CERN Open Data portal [\[9\]](#page-11-9). Only events in the list of validated runs [\[10\]](#page-11-10) are retained for the study. A total of about 110 million single electron and 70 million single muon *pp* events are available for analysis.

 The datasets are provided in the CMS miniAOD format, which contains high-level reconstructed objects that can be used for analysis [\[11\]](#page-11-11). This study is based on such re- constructed electrons, muons and jets. The data is accessed and processed using the CMS analysis code provided with the CMS open data [\[12\]](#page-12-0). Within this framework, jets are 79 reconstructed using the anti- k_t algorithm [\[13\]](#page-12-1) with a fixed radius parameter $R = 0.4$ and are tagged as containing a bottom hadron (b-tagged) based on the Combined Secondary Vertex (CSV) tagging algorithm. In a complete data analysis, the fact that b-tagging efficiencies can differ significantly between data and simulation, has to be taken into ac- count. This is however not critical for this study and so, no dedicated strategy has been implemented to address this.

 The matrix element calculation for the dark meson production is performed at next- to-leading order (NLO) in QCD based on the model described in Ref. [\[14\]](#page-12-2), using the corre- sponding UFO model files [\[15\]](#page-12-3). A signal sample is simulated using MadGraph5_aMC@NLO 3.5.1 [\[16\]](#page-12-4) interfaced with Pythia 8.306 [\[17\]](#page-12-5) for the modeling of parton showering, hadroniza- tion and underlying event with the A14 set of tuned parameters [\[18\]](#page-12-6) and the NNPDF2.3lo [\[19\]](#page-12-7) set of parton distribution functions (PDF). Fast simulation of the detector is done with Delphes 3.5.0 [\[20\]](#page-12-8) using the standard CMS detector card.

 Within Delphes, jets are determined with the FastJet 3.3.4 [\[21\]](#page-12-9) software package and 93 the anti- k_t algorithm [\[13\]](#page-12-1). The default *b*-tagging of the CMS Delphes card is used to 94 identify *b*-jets. The dark pion mass is set to $m_{\pi_D} = 500 \text{ GeV}$ and the dark rho mass 95 to $m_{\rho D} = 2 \text{ TeV}$. The signal cross-section is extracted from MadGraph5_aMC@NLO 2.9.9 [\[16\]](#page-12-4) and amounts to 18*.*9 fb. As previously mentioned, this signal point has been excluded by the ATLAS collaboration [\[5\]](#page-11-5). A total of 50k signal events are simulated and the sample is normalized to the integrated luminosity of the data sample.

 Events are further selected for the study based on kinematic and quality criteria im- posed on the reconstructed leptons and jets. In the MC events, any electron or muon 101 with transverse momentum $p_T > 28$ GeV is considered as a signal lepton. In data events, the signal lepton must additionally pass the *Tight* selection criteria [\[22,](#page-12-10) [23\]](#page-12-11). Only events containing exactly one signal lepton are retained for the study.

104 All jets are required to have a transverse momentum $p_T > 20 \text{ GeV}$ and to satisfy $|\eta| < 2.5$. In addition, any jet is required to have an angular distance $\Delta R > 0.4$ from the signal lepton in the event, in order to resolve any reconstruction ambiguities between the lepton and jets. If these requirements are not met, the jet is discarded. Events are ¹⁰⁸ eventually required to have at least four jets, out of which at least two must be *b*-tagged. ¹⁰⁹ Events passing all requirements listed here are selected for analysis. A total of 120k ¹¹⁰ and 6.47 events pass this baseline selection in data and signal respectively.

¹¹¹ 3 Discriminating variables

¹¹² The method is demonstrated on four event-level quantities that are suitable as discrimi-113 nating variables. The first three are; $\Delta R(l, b_2)$, defined as the angle between the lepton and the second closest *b*-jet; $m_{bb_{\Delta R_{min}}}$, defined as the invariant mass of the two *b*-jets in 115 the event that are closest to each other; and H_T , defined as the scalar sum of the p_T of the 116 jets in the event. The final variable is based on $R = 1.2$ jets reclustered from the $R = 0.4$ 117 jets using the anti- k_t algorithm with a fixed radius parameter of $R = 1.2$ [\[24\]](#page-12-12). The lepton 118 is added to the $R = 0.4$ jet collection before the reclustering and the highest- p_T large- R jet containing the lepton is referred to as \mathbb{J}^{lep} while the highest- p_T fully hadronic large-*R* jet ¹²⁰ is referred to as \mathbb{J}^{had} . The sum of the masses of these two jets is used as a discriminating ¹²¹ variable and is denoted by $m_{\mathbb{J}^{had}} + m_{\mathbb{J}^{lep}}$. Distributions of the discriminating variables in ¹²² data and signal are shown in Fig. [1](#page-3-1) for events passing the baseline selection described in the previous section.

Figure 1: Distributions of the discriminating variables in data and signal for selected events, normalized to 1. (Top, Left): $\Delta R(l, b_2)$; (Top, Right): $m_{bb_{\Delta R_{min}}}$; (Bottom, Left): H_T ; and (Bottom, Right): $m_{\text{J}^{\text{had}}} + m_{\text{J}^{\text{lep}}}$.

123

4 Method

 The SparkDensityTree library is a library of statistical methods, with the base class being a multi-dimensional density estimator that for any sample generated from an unknown density returns an optimally smoothed histogram. The optimally smoothed histogram is taken to be the one that, per estimation, minimizes the L_1 distance to the true underlying distribution, using the MDE method. The statistical methods on these MDE histograms include arithmetic operations, conditional densities, coverage regions, and marginal den- sities. Recall that the marginal probability density of a subset of variables is obtained by integrating out all other variables in the joint probability density of all the variables.

 The histogram object is represented as a binary tree in which each node represents a bisection of the phase space, and the leaves contain the event count in the finest resolution boxes thus obtained. The histogram construction begins with the definition of the root 136 box, ideally the smallest hypercube containing all data points. From the root box, \mathbf{x}_ρ , the support is iteratively bisected until a stopping criterion is reached, as visualized in Fig. [2.](#page-5-1) The underlying the tree structure [\[2\]](#page-11-2) allows for giving each box in the splitting a unique address. The combination of the leaf address and the counts is defined as the label of the 140 box, $(\rho v, \# x_{\rho v}).$

 The MDE histogram is described in [\[3\]](#page-11-4), and is taken as the optimal density estimate 142 in this work. This quantity, $f_n(x)$, is defined as following [\[3\]](#page-11-4):

$$
f_n(x) = \frac{1}{n} \sum_{\rho v \in \mathbb{L}(s)} \frac{\#\mathbf{x}_{\rho v}}{\text{vol}(\mathbf{x}_{\rho v})} \mathbb{I}_{\mathbf{x}_{\rho v}}(x),\tag{1}
$$

143 where the volume of a *d*-dimensional box is defined in detail in [\[2\]](#page-11-2), \mathbb{L} corresponds to the full set of leafs, and *n* is the amount of data points in the root box *s*. This quantity is found by an adaptive search in sequentially coarser histograms, starting at the one obtained by the splitting.

 The splitting is an inherently sequential process, but a distributed solution was devel- oped in [\[4,](#page-11-3)[25\]](#page-12-13). This requires an initial splitting of the root box down to the finest resolution that might be needed instantaneously – possibly to the point that each leaf only has a count of one – and then merged again. This is accomplished by only representing the leaves with at least one data point using sparse binary trees.

 In the distributed method, therefore, an additional step is added between the splitting and the MDE, which consists of merging the cells to a stopping criterion on the counts in each box, effectively representing the initial histogram for finding the MDE.

155 For a more in-depth explanation of the steps, the reader is referred to $[2-4,25,26]$ $[2-4,25,26]$ $[2-4,25,26]$ $[2-4,25,26]$. The procedure is sketched below:

Stage 1: Find the root box containing all the data points.

Stage 2: Define a stopping criterion for the splitting, such as a maximum box size. The root box is split until this criterion is reached, giving the *finest resolution histogram*. In this work, the finest splitting is determined by the stopping criterion that no leaf-box has any side length longer than the parameter finestResSideLength.

Stage 3: Merge leaves such that the counts are maximized, while not going higher than some limit minimumCountLimit and keeping the leaf depth as small as possible.

Stage 4: Starting from the histogram obtained in stage 3, find the optimally smoothed his-togram using MDE as described in [\[25,](#page-12-13) [26\]](#page-12-14).

 Additionally, two user-defined parameters concerning the distributed aspect of the 167 method are available: **numTrainingPartitions** and **sampleSizeHint**. Respectively, they correspond to how many times the training data is partitioned, related to distribution of work among computing nodes, and an initial guess of points connected to the size of the node batches [\[27\]](#page-12-15).

 The value of this method for data exploration in high-energy physics lies in the next step. When the MDE histogram is obtained, the highest density regions can be extracted by calculating the pdf coverage regions; and accordingly the highest and lowest density ¹⁷⁴ regions.

¹⁷⁵ For simplicity, marginal densities are considered in this work, but the method can be ¹⁷⁶ extended to take the full density into account simultaneously.

 The marginal densities for all unique pairs of the variables can be obtained from the ¹⁷⁸ 4-dimensional MDE histogram. In this paper, $\binom{4}{2} = 6$ unique pairs of variables are chosen ₁₇₉ and these six combinations are what the highest density regions are computed from. This is done separately for signal and background. The signal and background highest density regions can be defined independently of each other, and can, crucially, be flipped around to allow for finding the least dense region in the background density. From here, the user has to consider the best ways to use these marginal densities, and an example is given ¹⁸⁴ below.

Figure 2: A sequence of splittings along the first widest coordinate, starting from the root box in two dimensions. Obtained from [\[2\]](#page-11-2).

185 5 Results

 The results presented in this work are documented in a Github repository [\[28\]](#page-12-16). All compu- tations for the upcoming results have been performed on Virtual Machines (VMs) hosted by Google as a part of a dataproc cluster. The cluster contains three VM instances, all of which run four Intel Skylake vCPUs and has 15 GB of RAM; all in order to utilize the distributed aspect of the method.

 Figure [3](#page-6-0) shows a comparison between a 2D frequency or count histogram of the data over a uniform grid and that over the optimally smoothed nonuniform partition corre- sponding to the MDE histogram of this method. All distributions considered in this work have been compared in this way to ensure sensible density estimates are returned by the ¹⁹⁵ method.

¹⁹⁶ The density estimate is presented at three different highest density regions for back-ground in Fig. [4,](#page-7-0) and for signal in Fig. [5](#page-8-0) for the $m_{\text{J}^{\text{had}}} + m_{\text{J}^{\text{dep}}}$ vs. $\Delta R(l, b_2)$ combination.

Figure 3: Comparison between a regular 2D histogram representation (Left) and the distribution obtained in this method (Right) of $m_{\text{J}^{\text{had}}} + m_{\text{J}^{\text{dep}}}$ vs. $\Delta R(l, b_2)$ in background from data.

¹⁹⁸ Comparisons between signal and background distributions can also be made at different 199 levels. Figure [6](#page-9-0) shows the 3D and 2D combinations, together with the highest 50% density r_{1} regions for m_{1} _{*had*} + m_{1} ^{*lep*} and H_{T} .

201 The density estimates for signal and background are combined to form $X_{\text{sig}} \otimes \overline{Y}_{\text{bkg}}$ 202 density regions, where X_{sig} indicates the $X\%$ highest signal density region and $\overline{Y}_{\text{bkg}}$ indi- cates the complement of the *Y* % highest background density region. These combinations are used to design kinematic regions corresponding to the most dense signal and the least dense background. The regions are achieved from the *X*% highest signal density region and the *Y* % highest background density region using a bounding box around the density region in each pair of variables. From the bounding box, the sensitive interval of each variable is taken as the projection of the box onto that axis. The intersection of the signal interval and the complement of the background interval forms the final interval of inter- est for each variable pair. Each variable is associated with exactly three intervals from its participation in three variable pairs. In this work, the final region is defined by the 212 union of these intervals in each variable. Three combinations are presented: $50\% \otimes 50\%$, 213 90% ⊗ $\overline{20}$ % and 90% ⊗ $\overline{10}$ %. As an example, the obtained intervals for the 90% ⊗ $\overline{10}$ % combination are:

$$
\Delta R(l, b_2) : [0.6, 1.1] \qquad H_T : [625, 2172] \text{ GeV}
$$

\n
$$
m_{bb_{\Delta R_{min}}} : [312, 634] \text{ GeV} \qquad m_{\text{J}^{\text{had}}} + m_{\text{J}^{\text{lep}}} : [552, 996] \text{ GeV}
$$

 When compared to the one-dimensional distributions in Fig. [1](#page-3-1) it is clear that these corre- spond to regions with discrimination power between signal and background. While direct comparison with the ATLAS analysis [\[5\]](#page-11-5) cannot be done, since for example $m_{\mathbb{J}^{had}} + m_{\mathbb{J}^{lep}}$ is used as discriminant variable for the final fit, the intervals selected in this case are all fully contained in the signal region of the actual analysis.

²²⁰ The event selection corresponding to the intervals is applied to signal and data and ²²¹ the number of events passing the requirements are presented and compared in Table [I.](#page-10-1)

²²² The method results on less than one signal event on all tested scenarios and no back-²²³ ground events pass the selections in the most aggressive selection. Dark meson signals are ²²⁴ usually very small, and unlikely to be accessible in 2.3 fb^{-1} of data. It is possible however 225 to naively scale the 0.57 expected events in the $50\% \otimes \overline{50\%}$ scenario to, e.g. the full Run 226 2 data set collected by ATLAS, containing 140 fb^{-1} , to more than 30 events, a reasonable ²²⁷ signal for a new physics search.

Figure 4: Full background density estimate of the $m_{\text{J}^{\text{had}}} + m_{\text{J}^{\text{dep}}}$ vs. $\Delta R(l, b_2)$ combination in 3D (Top Left) and 2D (Top Right) together with the highest 75% density region (Bottom Left) and the highest 50% density region (Bottom Right).

Figure 5: Full signal density estimate of the $m_{\text{J}^{\text{had}}} + m_{\text{J}^{\text{lep}}}$ vs. $\Delta R(l, b_2)$ combination in 3D (Top Left) and 2D (Top Right) together with the highest 75% density region (Bottom Left) and the highest 50% density region (Bottom Right).

Figure 6: Full density estimate of the $m_{\mathbb{J}^{had}} + m_{\mathbb{J}^{lep}}$ vs. $H_{\mathbb{T}}$ combination in 3D (Top), 2D (Middle) and the highest 50% density region (Bottom) for signal (Left) and background (Right).

 The method could further be developed to identify the highest density region directly in the 4D histogram, and then project this onto the four axes. The SparkDensityTree library allows for defining arithmetic on the histograms, and it might be possible to combine the signal and background histograms and find the densest region in, e.g., number of signal events divided by number of background events, or the difference between the histograms. Finally, scalability is a very powerful aspect of this approach. This study did not delve into it, but as mentioned in [\[4,](#page-11-3) [25,](#page-12-13) [26\]](#page-12-14), the original method has been tested on several terabytes of simulations, and great decreases in computational time can be seen with the increase of cores. In this work, for example, the time required (averaged over 5 runs) to run over the CMS open data was 42.9 seconds, while the time require to run over the signal was 26.9 seconds.

 This is something of interest for the field of high-energy physics, as it would be straight-forward to run directly on the full collision datasets from the LHC.

²⁴¹ 6 Conclusion and Outlook

 This paper introduces a scalable method, originally formulated in a purely mathemati- cal context, applied for the first time in a high-energy setting. The approach relies on optimally smoothed multi-dimensional histograms with universal performance guarantees through scalable sparse binary tree arithmetic, incorporated in the SparkDensityTree li- brary. It enables a rigorous definition of phase space regions enriched in signal, using multiple variables at a time. This method suggests promising avenues for the exploration of new physics phenomena at the LHC.

 A large number of additional options is available from the SparkDensityTree library. This library contains several arithmetic operations and statistical methods (not covered here) that can be advantageous for studies on histograms, naturally interesting in a high-energy physics context.

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