

Experimental validation of TRIDYN self-sputtering simulations

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Abstract

In the case of high-fluence implantations, the approximation that every new incoming particle interacts with a pristine substrate material no longer holds. Dynamical changes to the substrate can induce different phenomena, one of which is self-sputtering. Self-sputtering occurs when incoming ions remove previously implanted ions from the implantation substrate. This phenomenon is significant in target production for nuclear structure studies and medical radionuclide separation, where self-sputtering limits can be reached during isotope implantation. Self-sputtering can be modeled using TRIDYN simulations in order to guide implantations. This work benchmarks the reliability of TRIDYN in regions relevant to both fundamental and medical research. Our findings indicate that TRIDYN predicts general dependencies reasonably well. However, it is important to carefully consider input parameters.

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1 Introduction

High-fluence effects in ion beam implantation have become increasingly significant in various branches of research. In the field of medical radionuclide production via radioactive ion mass separation and implantation, several isotope collections have shown limitations due to sputtering effects [1]. More specifically, due to self-sputtering, earlier implanted nuclides are removed from the foil upon implanting more nuclei until, eventually, the amount of nuclei of interest in the foil no longer increases. To address this issue, the MEDICIS facility at CERN (Medical Isotopes Collected from ISOLDE) [2] switched the implantation material from zinc to aluminum to mitigate self-sputtering on the premise that the effect would be less pronounced when using a substrate with a lower atomic number. Additionally, self-sputtering effects can be reduced by implementing beam sweeping in order to increase the implantation area and consequently reduce the fluence for the same amount of total collected ions. However, scaling up production to meet the growing demand for radionuclides necessitates careful consideration of sputtering. In fundamental research, several experiments, such as muonic atom spectroscopy [3] and neutron time-of-flight studies [4], require $\mathcal{O}(1 - 100) \mu\text{g}$ of target material

onto surfaces of $\mathcal{O}(1)\text{cm}^2$. Preparing such targets through implantation necessitates operating within the range where self-sputtering plays a significant role. Despite the diverse interests of these research fields, they share a common goal: implanting a large number of particles on a small surface area without significant loss due to sputtering.

Many simulations in the scope of implantations are performed using SRIM [5]. This software is a Monte Carlo-based simulation package that models implantation processes through the binary collision approximation. While SRIM provides sufficiently reliable estimates for most applications, it only considers a static pristine sample. However, when dynamical effects become important, the validity of SRIM breaks down. TRIDYN [6] is built around the same framework as SRIM, but allows for dynamic simulations, such as self-sputtering. Additionally, different implantation conditions can be applied either simultaneously or sequentially through layered simulations. These simulations can predict the retained fluence (number of particles per unit area) as a function of the incoming fluence, helping to determine the optimal stopping point for implantation and/or when to switch to a new sample.

Experimental validation of these simulations is sparse due to the long machine times required for high-fluence implantations [7, 8]. However, the need for systematic investigations became apparent during single implantations for both muonic atom research (gold implantations) [9] and implantations for medical applications at MEDICIS [10]. In both cases, clear signs of self-sputtering were observed [1, 9], which motivated a thorough investigation of retained fluence curves and a subsequent comparison with corresponding simulation results. Different implantations were performed: 1) Ytterbium (Yb, as a proxy for all lanthanides) was implanted into aluminum (Al) and zinc (Zn), which are the typical substrate materials at medical isotope collection facilities, 2) potassium (K) was implanted into pyrolytic graphite and 3) a previous gold (Au) implantation in carbon (C) [9] was revisited.

1 Methods

1.1 TRIDYN

Simulations of the ion implantations were performed using TRIDYN version 2022 [6] (most recent version at the time of writing). Key parameters for the simulations include the initial target composition and thickness, the total implanted fluence, irradiation conditions, and the surface binding energy matrix. A general description of these parameters can be found in Ref. [11]. Among these parameters, we direct our focus towards the surface binding energy, as it plays a crucial role in the systematic study that was performed. For this, we employ the zero bulk binding energy approximation, as recommended for TRIDYN [12].

The surface binding energy matrix of a material (X_nY_m) is given by

$$sbe = \begin{pmatrix} SBE_{YY} & SBE_{YX} \\ SBE_{XY} & SBE_{XX} \end{pmatrix}. \quad (1)$$

These matrix elements represent the interaction energies between materials X and Y and are crucial in quantifying the sputtering behavior. Specifically, they quantify the contributions from phenomena such as sublimation, formation, and dissociation of the compounds, which determine the bonding behavior at the surface.

The surface binding energy values are modeled depending on the phase of matter of the involved compounds; SBE_{X-X} is assumed to be 0 eV for gases and equal to the sublimation enthalpy (ΔH^s) in solids. For X a solid and Y a gas with molecular fractions n and m , respectively,

X	ΔH_X^s	Ref.
C	4.5 eV	[13]
Au	3.8 eV	[11]
Al	3.36 eV	[14]
Yb	1.74 eV	[11]
K	0.93 eV	[11]
XY	ΔH_{XY}^f	Ref.
AuC	1.03 eV	[15]
Al ₂ O ₃	3.36 eV	[14]
Yb ₂ O ₃	3.36 eV	[14]
YbAl ₂	0.7588 eV	[16]
YbZn	0.338 eV	[17, 18]
Y	ΔH_Y^{diss}	Ref.
O ₂	5.16 eV	[14]

Table 1: Overview of the used formation and sublimation enthalpies and formation energy used in this work.

the matrix element, $SBE_{X,Y}$, is calculated as [11]

$$SBE_{X,Y} = \frac{1}{2} \Delta H_X^s + \frac{n+m}{2nm} \Delta H_{XY}^f + \frac{n+m}{4n} \Delta H_Y^{\text{diss}},$$

with ΔH_X^s the sublimation enthalpy, ΔH^f the formation enthalpy per molecule of the compound and ΔH^{diss} the dissociation energy of the gas molecule Y [11]. For two solids with molecular fractions n and m , the surface binding energy matrix element is given by [11]:

$$SBE_{X,Y} = \frac{\Delta H_X^s + \Delta H_Y^s}{2} + \frac{n+m}{2mn} \Delta H_{XY}^f. \quad (2)$$

A summary of the sublimation enthalpies, formation enthalpies and dissociation energy used in the remainder of this work is given in Table 1.

1.2 Experiments

The samples produced for this work were prepared at two different facilities: potassium implantations were performed at the 40 kV Ion Implanter at Helmholtz Zentrum Dresden Rossendorf (HZDR) [19]; ytterbium implantations were performed at the High Current Ion Implanter in the Ion and Molecular Beam Laboratory (IMBL) at KU Leuven [20]. In all of these cases, beam sweeping was employed to ensure a uniform profile of incoming fluences. Small samples, approximately 5 mm × 5 mm, were implanted with varying incoming fluences. To optimize machine time, multiple samples were implanted simultaneously. After the implantations, Rutherford backscattering spectrometry (RBS) was performed on site to characterize the samples. Besides identifying the elements, RBS provides information about the absolute number of particles of a specific species per unit area. The number of particles per unit area of a certain element is (in first order) proportional to the integral of its corresponding peak in the spectrum. Hence the retained fluence (ψ_{retained}) in the foils can be determined using

$$\psi_{\text{retained}} = \psi_{\text{cal}} \frac{I_{\text{RBS}}}{I_{\text{cal}}} \frac{Q_T(\text{cal})}{Q_T(\text{exp})}. \quad (3)$$

Here, ψ_{cal} corresponds to the fluence calculated from the peak of interest simulated in the calibration spectrum (RBS on AuCo₃/SiO₂/Si). I_{cal} and I_{RBS} are the integrals over the peak

of interest in the simulated peak from the calibration measurement and measurement of the implanted samples, respectively. Lastly, $Q_T(\text{cal})$ and $Q_T(\text{exp})$ correspond to the total collected charge on the substrate during the calibration measurement and sample measurement, respectively.

2 Results

2.1 Reassessing Au implantations in carbon

The need for systematic investigations became apparent during singular implantations for muonic atom research, where the retained fluence of Au ions was significantly lower than predicted by basic TRIDYN simulations [9]. These simulations have since been performed with an updated surface binding energy matrix element for carbon, which deviates from the default value assumed by TRIDYN.

$$sbe = \begin{pmatrix} SBE_{C-C} & SBE_{C-Au} \\ SBE_{Au-C} & SBE_{Au-Au} \end{pmatrix} = \begin{pmatrix} 4.5 \text{ eV} & 5.18 \text{ eV} \\ 5.18 \text{ eV} & 3.8 \text{ eV} \end{pmatrix}. \quad (4)$$

Here, the values from Table 1 were used. By properly assigning the off-diagonal elements in the binding energy matrix, better agreement was achieved with the experimental data, as illustrated in Figure 1. Despite this improvement, a significant deviation with the experimental data remains for the 90 keV implantation, which we attribute to the porosity of glassy carbon [9].

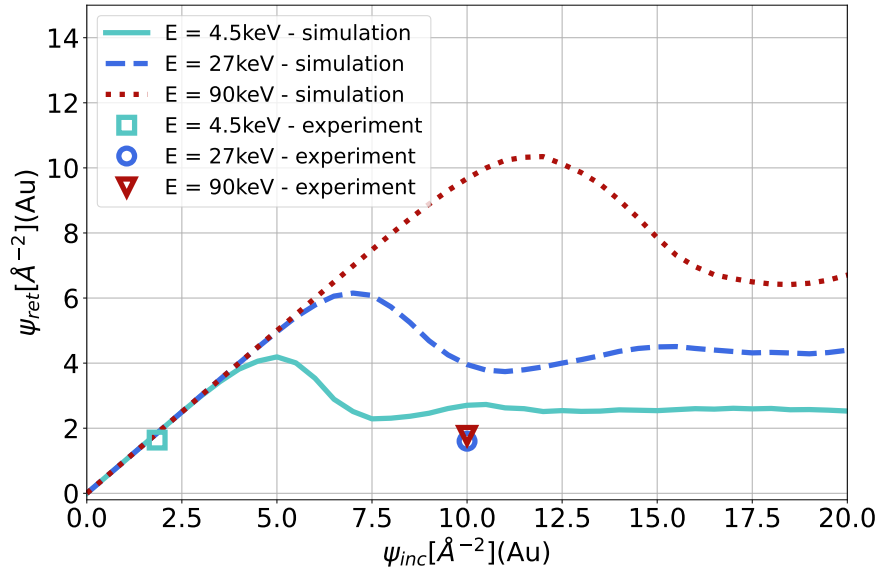


Figure 1: Experimental datapoints for the retained fluence (ψ_{ret}) as a function of the incoming fluence (ψ_{inc}) compared to the simulation for gold implantations in glassy carbon at different energies.

2.2 Systematic study with Yb

For systematic investigation of the validity of TRIDYN in the lanthanide region, implantations of Yb in Al and Zn were performed at 60keV for implantation fluences ranging from 0.26 \AA^{-2} to 6.0 \AA^{-2} . For each set of these implantations, two different TRIDYN simulations were performed. The first simulation models implantation in bulk Al_2O_3 or ZnO , while the second models implantation in bulk Al or Zn with a layer of Al_2O_3 or ZnO on top. The thickness of this layer is determined from the thickness of the native layer, given by 3.0 nm [21] and 1.5 nm [22] for Al_2O_3 and ZnO , respectively. The surface binding energy for implantation of Yb in Al_3O_2 was determined as follows:

$$\begin{aligned} sbe_{\text{Al}} &= \begin{pmatrix} SBE_{\text{Yb-Yb}} & SBE_{\text{Yb-Al}} & SBE_{\text{Yb-O}} \\ SBE_{\text{Al-Yb}} & SBE_{\text{Al-Al}} & SBE_{\text{Al-O}} \\ SBE_{\text{O-Yb}} & SBE_{\text{O-Al}} & SBE_{\text{O-O}} \end{pmatrix} \\ &= \begin{pmatrix} 1.74 \text{ eV} & 3.1191 \text{ eV} & 11.93 \text{ eV} \\ 3.1191 \text{ eV} & 3.36 \text{ eV} & 12.155 \text{ eV} \\ 11.93 \text{ eV} & 12.155 \text{ eV} & 0 \text{ eV} \end{pmatrix}. \end{aligned} \quad (5)$$

Similarly, the surface binding energy matrix for implantation of Yb in ZnO is given by:

$$\begin{aligned} sbe_{\text{Zn}} &= \begin{pmatrix} SBE_{\text{Yb-Yb}} & SBE_{\text{Yb-Zn}} & SBE_{\text{Yb-O}} \\ SBE_{\text{Zn-Yb}} & SBE_{\text{Zn-Zn}} & SBE_{\text{Zn-O}} \\ SBE_{\text{O-Yb}} & SBE_{\text{O-Zn}} & SBE_{\text{O-O}} \end{pmatrix} \\ &= \begin{pmatrix} 1.74 \text{ eV} & 1.883 \text{ eV} & 11.93 \text{ eV} \\ 1.883 \text{ eV} & 1.35 \text{ eV} & 6.885 \text{ eV} \\ 11.93 \text{ eV} & 6.885 \text{ eV} & 0 \text{ eV} \end{pmatrix}. \end{aligned} \quad (6)$$

The used enthalpies and energies are presented in Table 1.

The corresponding experimental results, inferred from the RBS spectra, as well as the simulation results are shown in Figure 2 and 3.

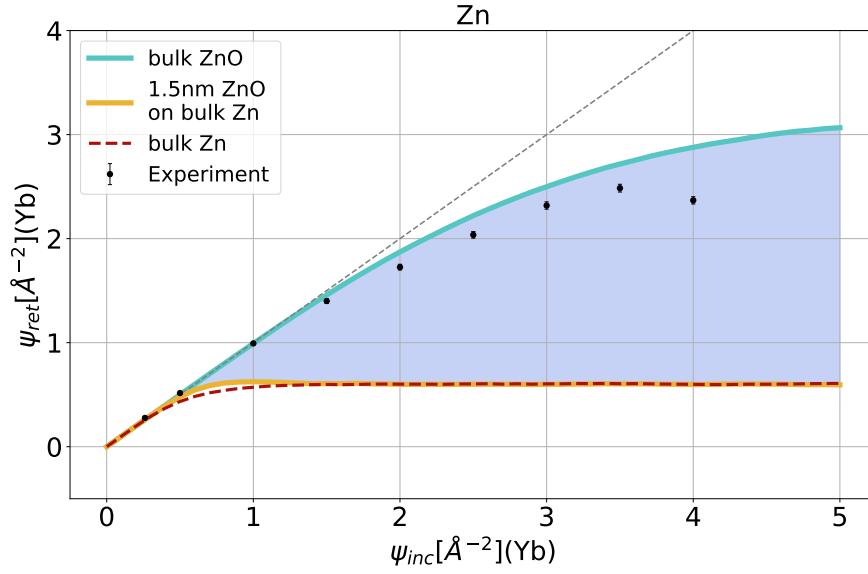


Figure 2: Experimental data for the retained fluence (ψ_{ret}) as a function of the incoming fluence (ψ_{inc}) compared to the simulation of bulk ZnO and the simulation of bulk Zn with a native layer of 1.5nm ZnO on top. For reference, the simulation for implantation in bulk Zn is shown in red (dashed).

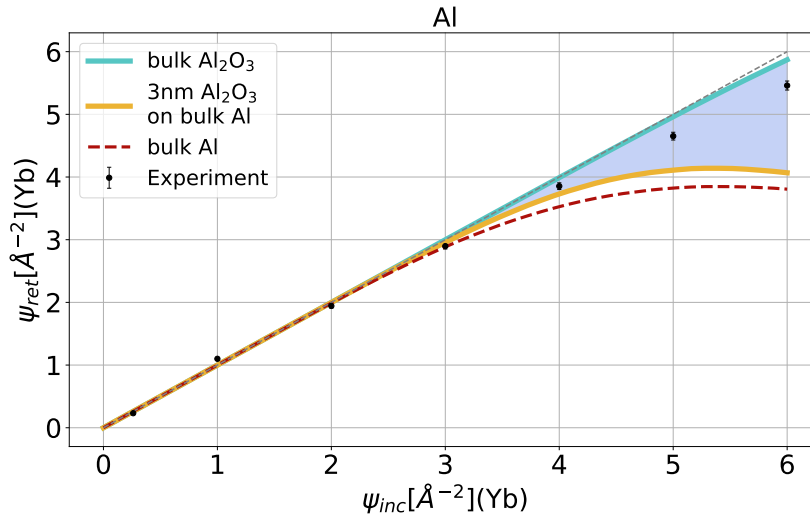


Figure 3: Experimental data for the retained fluence (ψ_{ret}) as a function of the incoming fluence (ψ_{inc}) compared to the simulation of bulk Al_2O_3 and the simulation of bulk Al with a native layer of 3nm Al_2O_3 on top. For reference, the simulation for implantation in bulk Al is shown in red (dashed).

From comparison of these simulations with the experimental data, it is concluded that the bulk oxide simulations and the native layer simulations provide an upper and lower boundary for the experimental data, respectively. This can be explained through the implantation procedure which started from a bulk Al (Zn) plate with a native layer of Al_2O_3 (ZnO). Subsequently, ytterbium is implanted and part of the oxygen is sputtered from the foil, which gradually in-

creases the Z-value of the foil as well as the self-sputtering yield. After the first implantation step, all foils are extracted from the vacuum to remove the first foil. At this point, a new native oxide layer is formed prior to the next Yb implantation step. As such, the oxide layer systematically rebuilds upon removal from the vacuum. Due to the lower Z of oxygen compared to aluminum and zinc, self-sputtering is reduced. As a result, the experimental retained fluence is larger than the simulation of a bulk Al (Zn) plate with a native layer of Al_2O_3 (ZnO) foil on top. On the other hand, the native thickness of the oxygen layer that is rebuilt is considerably smaller than the implantation depth, thereby decreasing the retained fluence compared to the bulk Al_2O_3 (ZnO) simulations. Furthermore, as illustrated in Figure 4, which shows the retained oxide layer as a function of the incoming Yb fluence, the incoming Yb fluence at which the oxide layer is sputtered away is of the same order of magnitude as the incoming fluence in one implantation step ($0.25 \text{ \AA}^{-2} - 1 \text{ \AA}^{-2}$). This is also clear from a back-of-the-envelope calculation of the thickness of the sputtered layer from a fully oxidized substrate, which equals 1.28 nm and 4.02 nm for implantation of 0.5 \AA^{-2} of Yb in bulk Al_2O_3 and ZnO, respectively (see Appendix A). This indicates that the oxide layer is significantly sputtered away in each implantation step. Subsequently, upon removal of the foils, a combined ytterbium oxide and aluminum oxide (zinc oxide) native layer is reformed. The detailed formation of this combined oxide layer is beyond the scope of this publication.

Note also that the self-sputtering for implantation in Zn is stronger than in Al, because of the higher proton-number of Zn. The full impact of self-sputtering across different implantation foils and implantation materials will be discussed in a subsequent paper, specifically focusing on medically relevant cases.

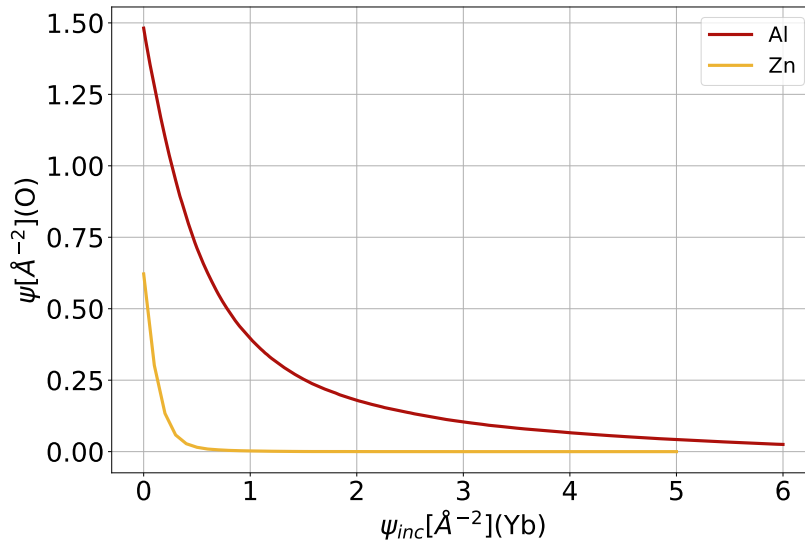


Figure 4: Simulated oxygen fluence in the substrate for implantation of Yb in Al (Zn) with a native layer of Al_2O_3 (ZnO) on top.

2.3 Systematic study with K

For muonic atom spectroscopy, carbon is a convenient backing material. It is easy to handle, non-toxic, and does not contribute substantially to background during those measurements. As an added benefit, the low proton number of carbon results in sputtering effects that only occur at relatively high fluences. For these implantations, a beam energy of 30 keV was used with fluences ranging from 5 to 50 \AA^{-2} . The surface binding energy matrix used for the simulations

140 was calculated to be:

$$\begin{aligned}
 sbe &= \begin{pmatrix} SBE_{C-C} & SBE_{C-K} \\ SBE_{K-C} & SBE_{K-K} \end{pmatrix} \\
 &= \begin{pmatrix} 4.5 \text{ eV} & 2.715 \text{ eV} \\ 2.715 \text{ eV} & 0.93 \text{ eV} \end{pmatrix}.
 \end{aligned} \tag{7}$$

141 For SBE_{K-C} , the ΔH^f term was neglected as no consistent literature value is available,
 142 while the other enthalpies and energies are available in Table 1. Figure 5 shows a comparison
 143 between the experimental results and the simulations. While the general trend is reproduced,
 144 it seems that the maximal retained fluence is nearly a factor two lower than the simulations.

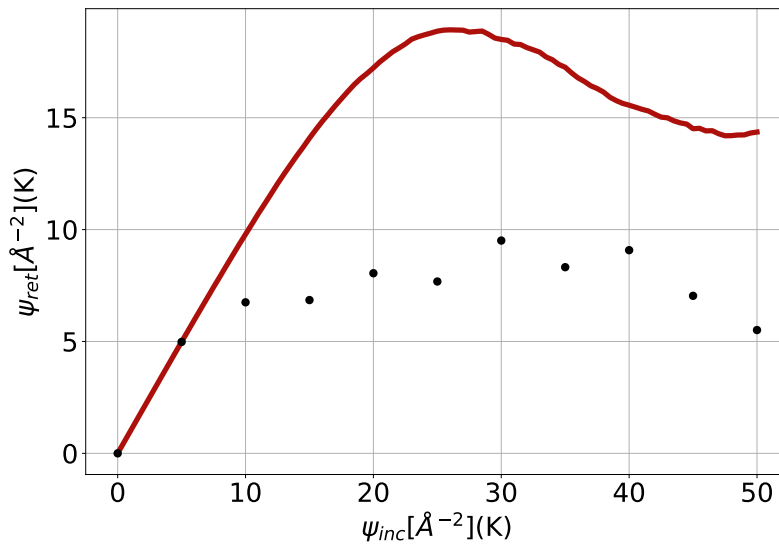


Figure 5: Experimental datapoints for the retained fluence (ψ_{ret}) as a function of the incoming fluence (ψ_{inc}) compared to a TRIDYN simulation for 30 keV ^{39}K in pyrolytic graphite.

145 The RBS spectrum, shown in Figure 6, gives an indication of two potential causes of this
 146 discrepancy. First, the potassium peak has a long low-energy tail, indicating that the distribu-
 147 tion of potassium extends deep into the material. This is likely caused by thermal diffusion
 148 and/or the high reactivity of elemental potassium, which may be affected by the porosity of
 149 the substrate material. Second, a large oxygen peak is present, closely mirroring the struc-
 150 ture in potassium. Similar to the ytterbium implantations, we suspect that this oxygen most
 151 likely enters the substrate between implantation steps, where the samples are taken out of
 152 the vacuum. This may lead to a changing surface binding energy, and hence, changes in the
 153 retained fluence curve. Both of these aspects limit the conclusions that can be drawn from
 154 these experimental tests with potassium. The pristine sample shows some oxygen in the sam-
 155 ple, though substantially less than in the implanted sample. Additionally, a minor background
 156 can be seen above 600 keV, though not enough to explain the low energy tail visible in the
 157 implanted sample. A simulation for implantation in CO was also performed but did not show
 158 significant changes.

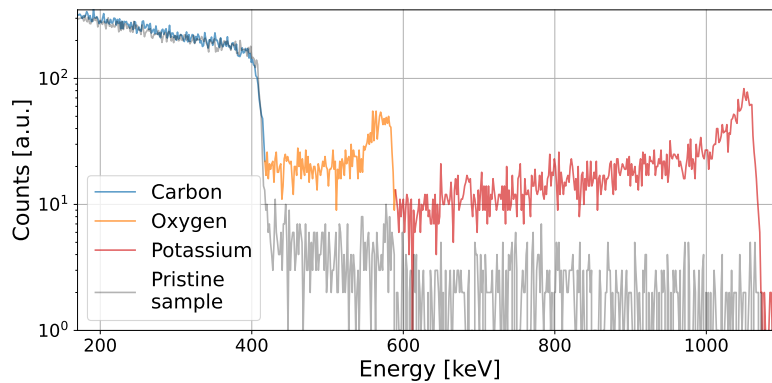


Figure 6: RBS spectrum for a pristine pyrolytic graphite sample (grey) and implanted ^{39}K target (color). The spectrum was obtained using an incident $1.57\text{ MeV } ^4\text{He}^+$ beam and a detector placed at a scattering angle of 162° .

Conclusion

In this study, we have investigated the performance of TRIDYN in modeling self-sputtering for implantations relevant to the target-making for fundamental nuclear structure studies and medical isotope collections. The retained fluence was measured experimentally for varying implantation fluences and the results were compared to the simulations. Our experimental results indicate that while TRIDYN effectively models the general trends of implantation and sputtering, careful consideration of input parameters is crucial, and the results should be interpreted with caution.

The ytterbium measurements showed reasonable agreement with the simulations. However, dynamic changes to the oxide layer between different implantation steps can significantly affect the retained fluence. For potassium the simulations deviated substantially from the experimental trend, likely due to a combination of thermal diffusion and the strong reactivity of potassium. These variances suggest that while TRIDYN can serve as a valuable predictive tool, it has limitations, especially under conditions where dynamic changes to the oxide layers are significant.

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Author contributions B.C., R.H., U.K., G.M. and Q.Z. were involved in the experiment (implantations + RBS). M.D. and M.H. performed the simulations. M.D., M.H., G.M. were involved in the data-analysis and T.E.C., M.D., M.H., W.M., L.P., A.V. and W.W. were involved in the discussion of the results. M.H. and M.D. wrote the manuscript and all co-authors reviewed it. We would also like to thank K. van Stiphout for the valuable discussions.

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A Calculation of the thickness of the sputtered layer

In this appendix, a back-of-the-envelope calculation to determine the thickness of the sputtered layer from a fully oxidized substrate is presented. These calculations hold under the assumption that the sputtered species leave the foil as molecules, which is a first-order approximation. These calculations rely on the sputtering yield of oxygen, which is outputted by TRIDYN.

A.1 Al

The simulation for implantation in bulk Al_2O_3 shows a sputtering yield for O of $Y_{\text{sputtered, O}} = 1.79$. To calculate what thickness this corresponds to, the molecular density is determined:

$$n_{\text{molecule}} = \frac{\rho N_a}{M} = \frac{3.95 \frac{\text{g}}{\text{cm}^3} \cdot N_a}{101.96 \frac{\text{g}}{\text{mol}}} = 2.33 \cdot 10^{-2} \frac{\text{molecules}}{\text{\AA}^3}. \quad (\text{A.1})$$

Here, ρ is the mass density, N_a is Avogadro's constant, and M is the molar mass. Subsequently, the thickness of the sputtered layer (t) can be calculated as:

$$t = \frac{\psi_{\text{sputtered, O}}}{n_{\text{O}}} = \frac{\psi_{\text{inc}} \cdot Y_{\text{sputtered, O}}}{n_{\text{O}}} = \psi_{\text{inc}} \cdot 25.54 \text{\AA}^3. \quad (\text{A.2})$$

Here, $n_{\text{O}} = 3n_{\text{molecule}}$ is the atomic density and ψ_{inc} is the incoming Yb fluence. Hence, for incoming fluences of 0.5\AA^{-2} and 1\AA^{-2} , the thickness of the sputtered layer equals 12.77\AA and 25.54\AA , respectively.

A.2 Zn

For implantation in bulk ZnO , a sputtering yield for O of $Y_{\text{sputtered, O}} = 3.33$ is found. First, the molecular density is determined:

$$n_{\text{molecule}} = \frac{\rho N_a}{M} = \frac{5.61 \frac{\text{g}}{\text{cm}^3} \cdot N_a}{81.379 \frac{\text{g}}{\text{mol}}} = 4.15 \cdot 10^{-2} \frac{\text{molecules}}{\text{\AA}^3}. \quad (\text{A.3})$$

Now, the thickness of the sputtered layer (t) is calculated as:

$$t = \frac{\psi_{\text{sputtered, O}}}{n_{\text{O}}} = \frac{\psi_{\text{inc}} \cdot Y_{\text{sputtered, O}}}{n_{\text{O}}} = \psi_{\text{inc}} \cdot 80.36 \text{\AA}^3. \quad (\text{A.4})$$

Here, $n_{\text{O}} = n_{\text{molecule}}$ is used. For incoming fluences of 0.5\AA^{-2} and 1\AA^{-2} , the thickness of the sputtered layer equals 40.18\AA and 80.36\AA , respectively.

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