## Referee report on Bethe vectors and recurrence relations for twisted Yangian based models, by Vidas Regelskis

The author has answered to most of the questions I raised. It remains one point (see point 4) that should be clarified. I also added some other remarks that I leave to the author.

- 1. On line 110, the letter u, v, w.. are said to correspond to complex numbers or formal parameters, but the first use of w is for the partial transposition (lines 132 and 137). At least a change of font for the partial transposition would be nice. In general transposition is indicated by a symbol  $(...)^t$ , but it seems that the author does not want to use it, although it would clarify things for the reader.
- 2. In eq. 2.15, indicate the range of summation for i, j
- 3. Still around eq. (2.15) the notion of "overlapping" (which I do not find very enlightening, although understandable) could be circumvented using  $\hat{n} = \left[\frac{N+1}{2}\right]$  and  $\hat{n}' = \left[\frac{N}{2}\right]$  such that  $\hat{n} + \hat{n}' = N$ . I believe that what the author means is that A is a  $\hat{n}' \times \hat{n}'$  matrix, B is a  $\hat{n}' \times \hat{n}$  matrix, C is a  $\hat{n} \times \hat{n}'$  matrix and D is a  $\hat{n} \times \hat{n}$  matrix (whatever the parity of N). That would avoid the discussion on overlapping, but I understand that this imply a lot of changes, so I leave it to the author.
- 4. The notation explained in line 400 is very confusing: the notion that un-mentioned (sub)sets are considered as empty is very delicate to employ. For instance, on eq. (4.2), from line 400, I would conclude that  $\boldsymbol{v}^{(1...n)} = \emptyset$ , which seems not to be the case. This occurs several times. I think that the author cannot avoid to be more precise, for instance in eq. following line 401 to use  $\sum_{\substack{|\boldsymbol{u}^{(r)}|=0\\r< i}} \sum_{\substack{|\boldsymbol{u}^{(r)}|=k\\i< r}} \inf_{i< r}$  or to add a text after the equation to specify which subsets are empty.

I think this point has to be clarified (in a way or another) before publication.

5. There is a typo in the second line of the eq. following line 418:  $u_{II}^{(s)}$  should be  $v_{II}^{(s)}$