Report on manuscript "Non-Chiral Vertex Operator Algebra Associated To Lorentzian Lattices And Narain CFTs by Ranveer Kumar Singh, Madhav Sinha

In this paper, the authors introduce the concept of *non-chiral VOA*, which gives a mathematical definition of conformal field theory, derive its basic properties, and mathematically construct a family of conformal field theories called Narain CFT. However, as pointed out below, a great number of definitions, propositions, and main theorems have **already been written** in the previous work [1] (submitted to arXiv in 2020).

In [1], Moriwaki introduced the notion of *full VOA* and showed that a full VOA admits exactly marginal deformations if the full VOA has Heisenberg VOA as a subalgebra. In particular, he constructed the Narain CFT as a concrete example of such a deformation family [1, Section 6.3].

However, this paper **only mentions a single sentence** in the introduction about prior work, and re-proves the same proposition and theorem in essentially the same way, without proper **citation**. This paper should be properly rewritten to show what is new and what is an existing result.

(Several comments)

The novelty of this paper lies in the following points, for example:

- The definition of non-chiral VOA in this paper differs from that in [1]. In [1], full VOA is defined using bootstrap equation, but in this paper, it is defined using locality of multi-point correlation functions. In particular, it is not fully checked in [1] that Narain CFT constructed in [1] satisfies the axiom of non-chiral VOA in the sense of this paper.
- Note that If it is a non-chiral VOA, then it is a full VOA in the sense of [1] (Proposition 2.2 in this paper). Although most of the pages of this paper overlap with [1], the referee believes that it is appropriate to take the form of a citation for these overlapping propositions, and that it is appropriate to recapitulate only the new parts as a new paper.

Some examples that require citation:

- Lemma 2.1, Lemma 2.2, Lemma 2.3, Prop 2.1, Prop 2.2 can be found in [1, Prop 3.7 and Section 4.3]
- Definition of chiral vector (def 2.2) can be found [1, Section 3.2] and modules [1, Section 3.1].
- Theorem 2.1 can be found in [1, Lemma 3.11]
- Construction of Narain CFT as full VOA can be found in [1, Section 4.4, Prop 4.10]
- Double coset description [1, Theorem 6.5] with example for Narain CFT [1, Section 6.3]
- [1] Two-dimensional conformal field theory, full vertex algebra and current-current deformation, Adv. Math, **427**, 2023